

# Introduction to MRI Physics

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# Overview

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- Basic Principles
  - Nuclear Magnetic Resonance
  - Excitation, Relaxation and Signal
  - Image contrast
  
- Advanced Concepts
  - Spatial Encoding in MRI
  - Image formation and k-space

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# Part I

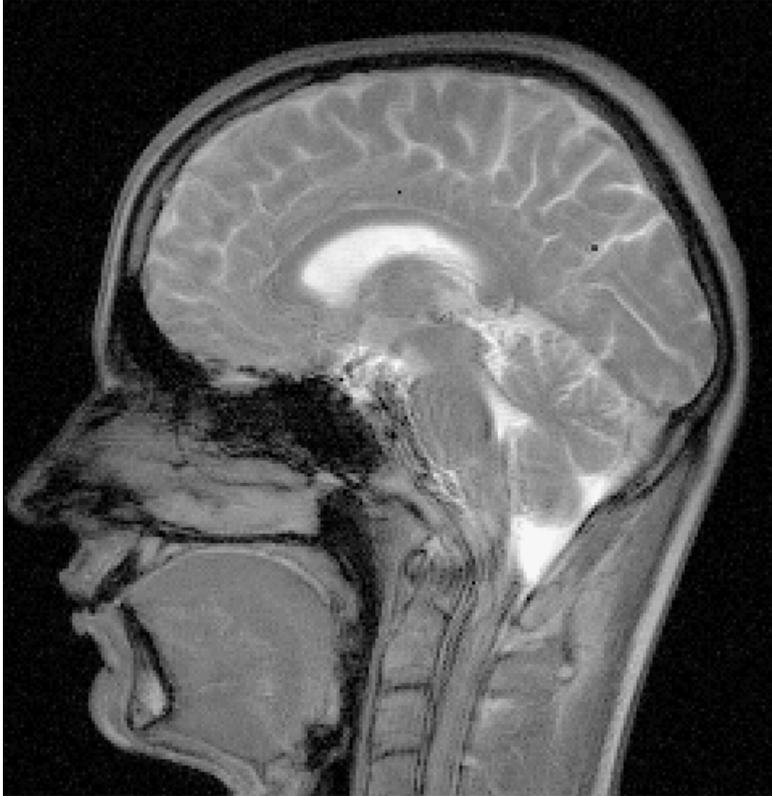
# Basic Principles

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# Nuclear Magnetic Resonance

# MR images: What do we see ?

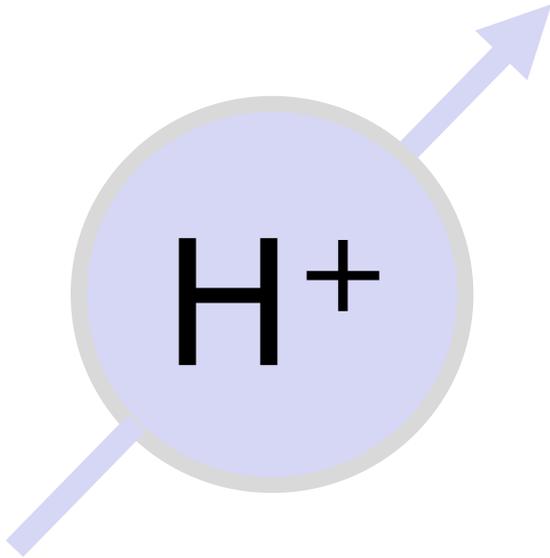
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- MRI images are usually based on the signal from protons
- A proton is the nucleus of the hydrogen atom
- Hydrogen is the most common element in tissue
- The signal from protons is due to their *spin*

# The Nuclear spin

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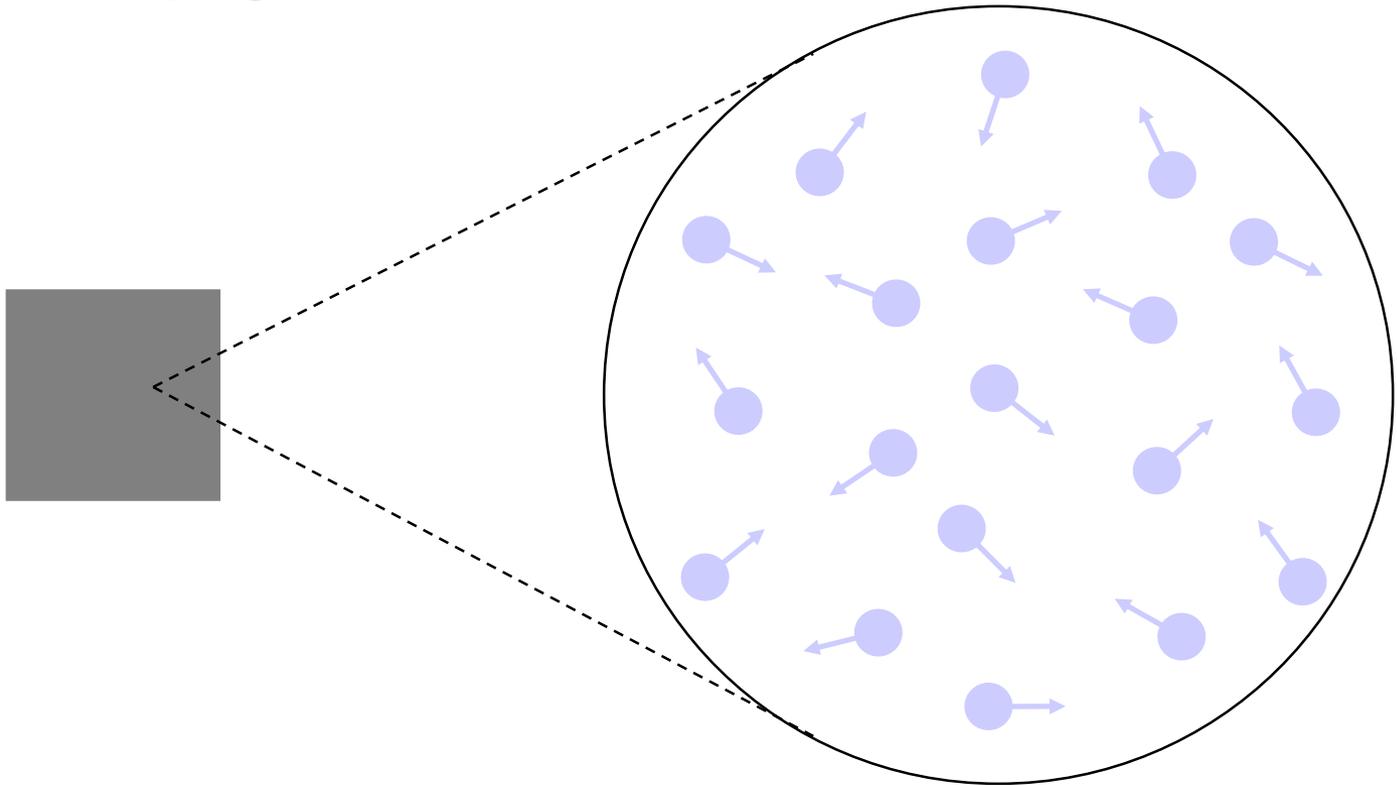


- Elementary property of an atomic nucleus
- Each spin carries an elementary magnetization
- Spins align in an external magnetic field (like a compass needle)

# Macroscopic sample

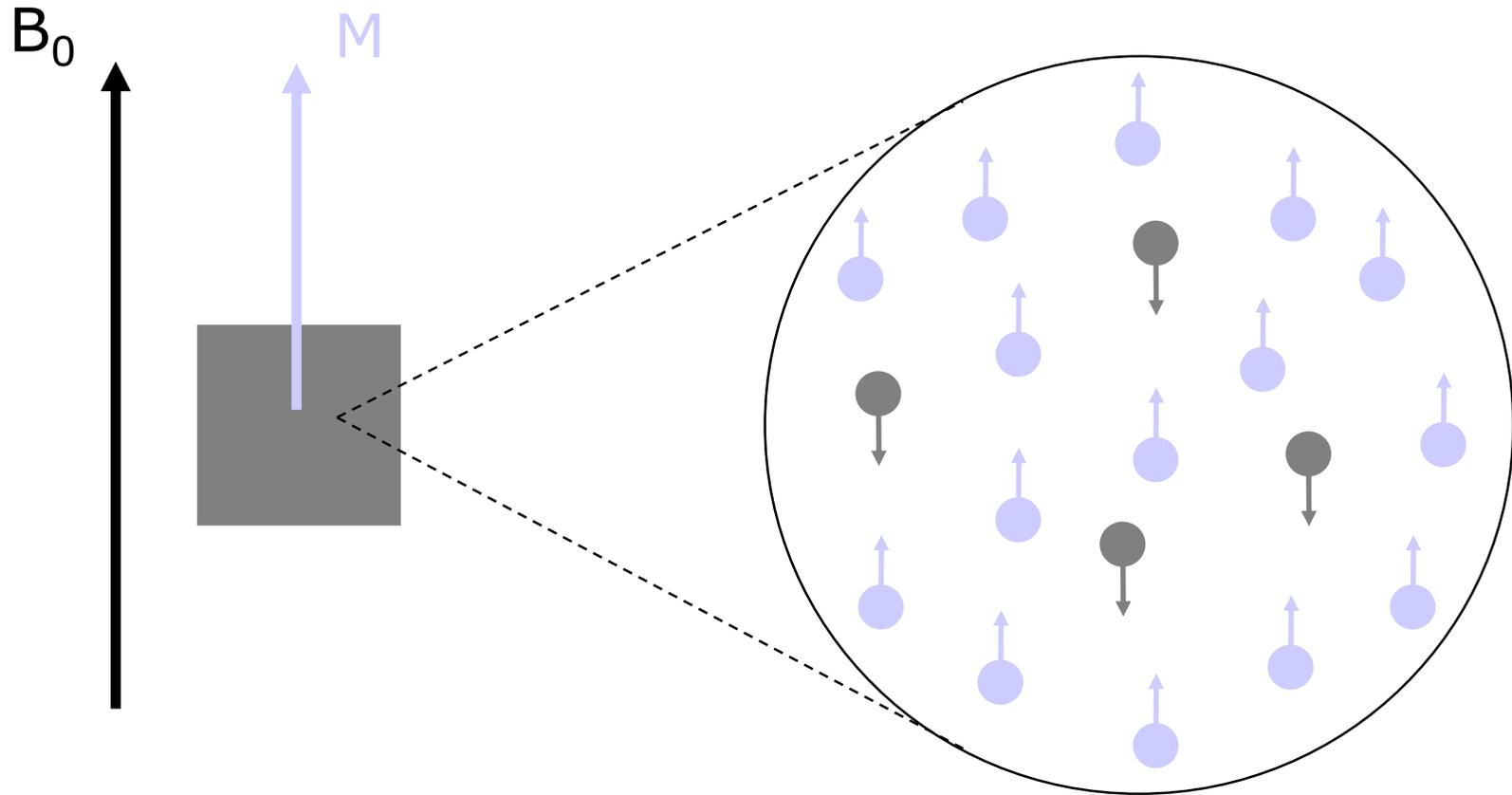
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$M=0$

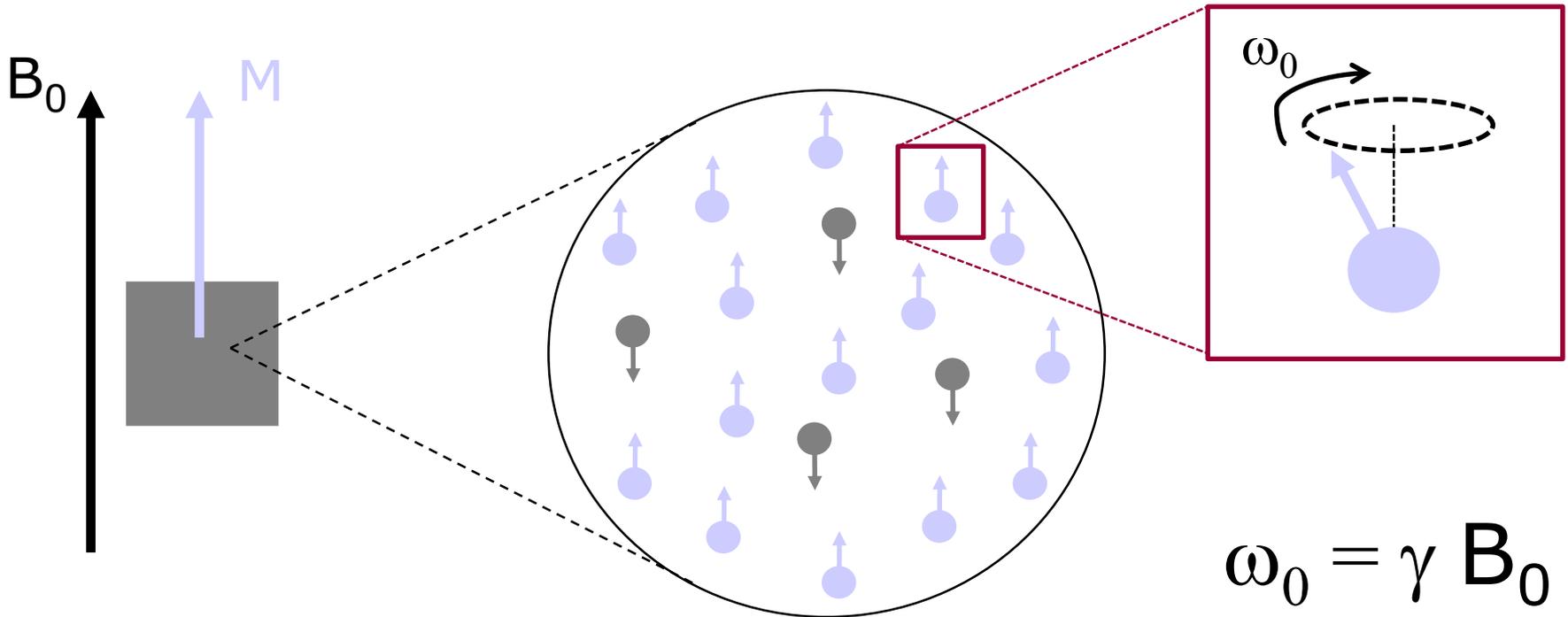


# Macroscopic sample

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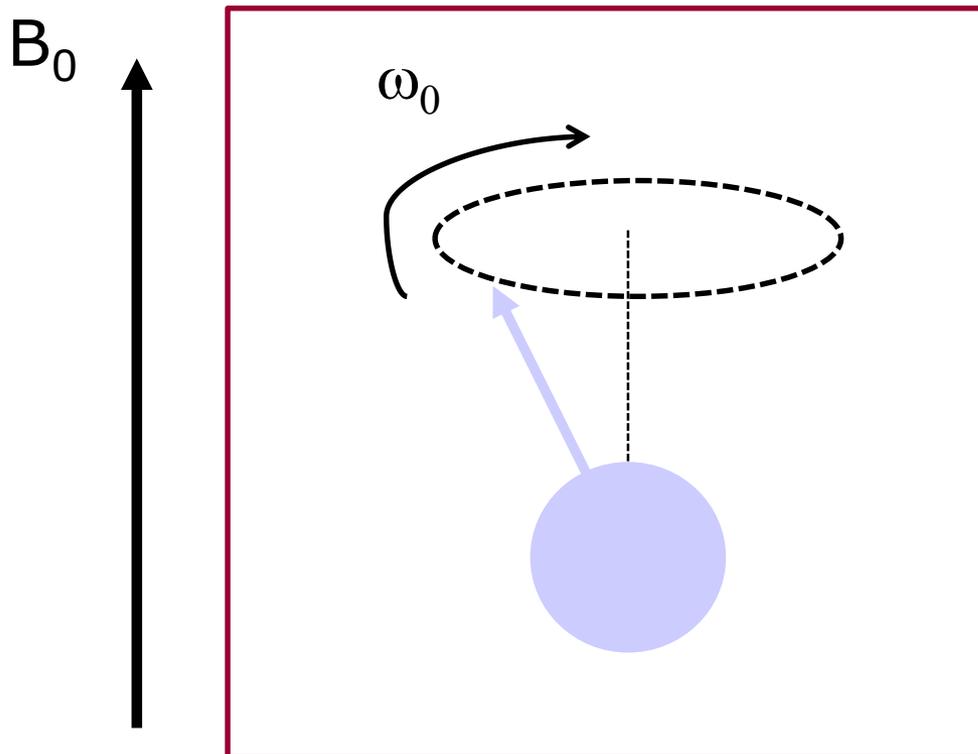


# Precession and Larmor Frequency



# Precession and Larmor Frequency

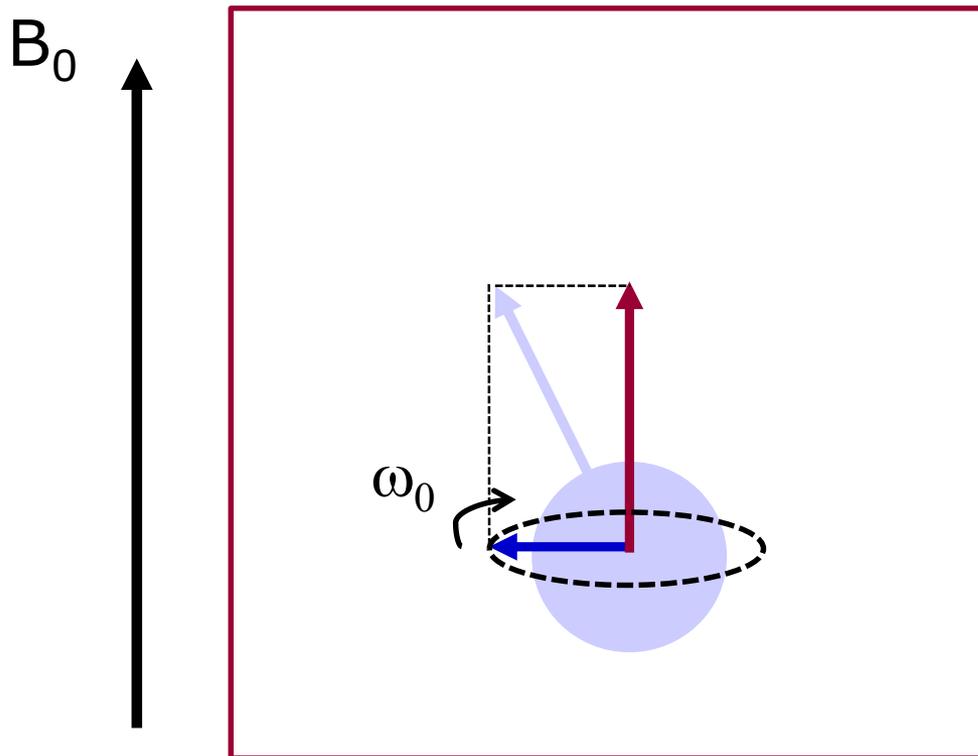
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$$\omega_0 = \gamma B_0$$

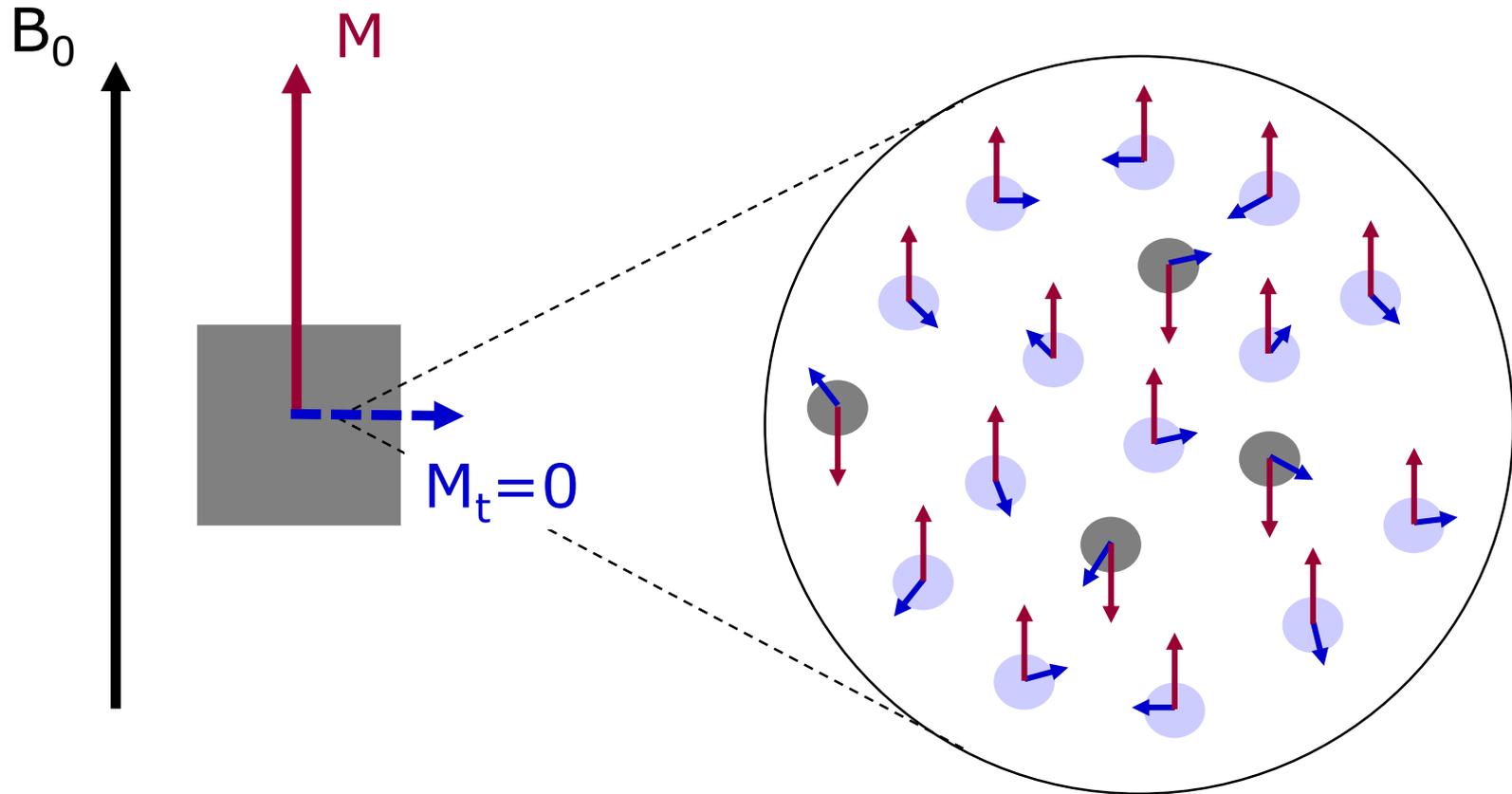
# Precession and Larmor Frequency

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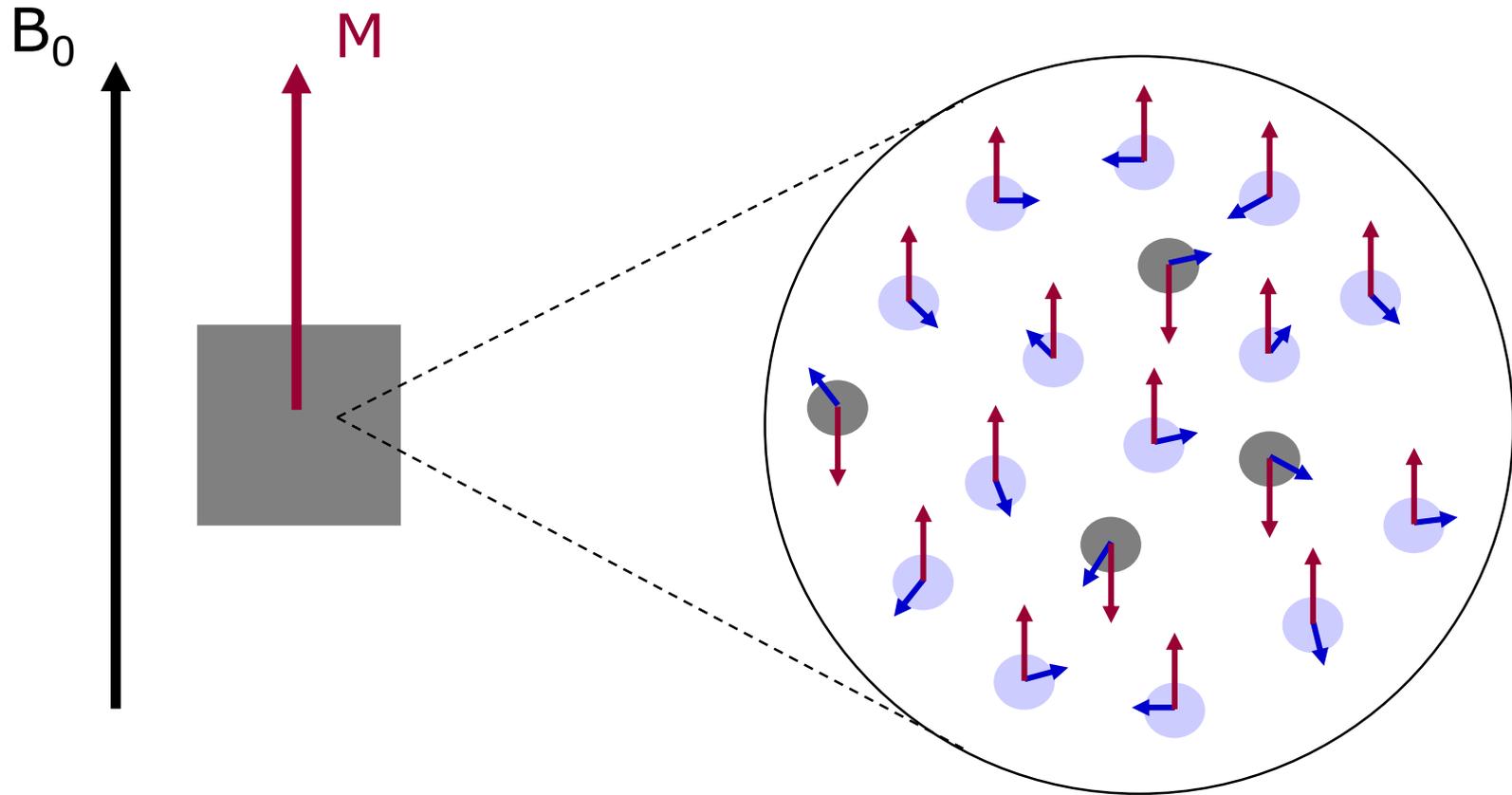
$$\omega_0 = \gamma B_0$$

# Macroscopic sample



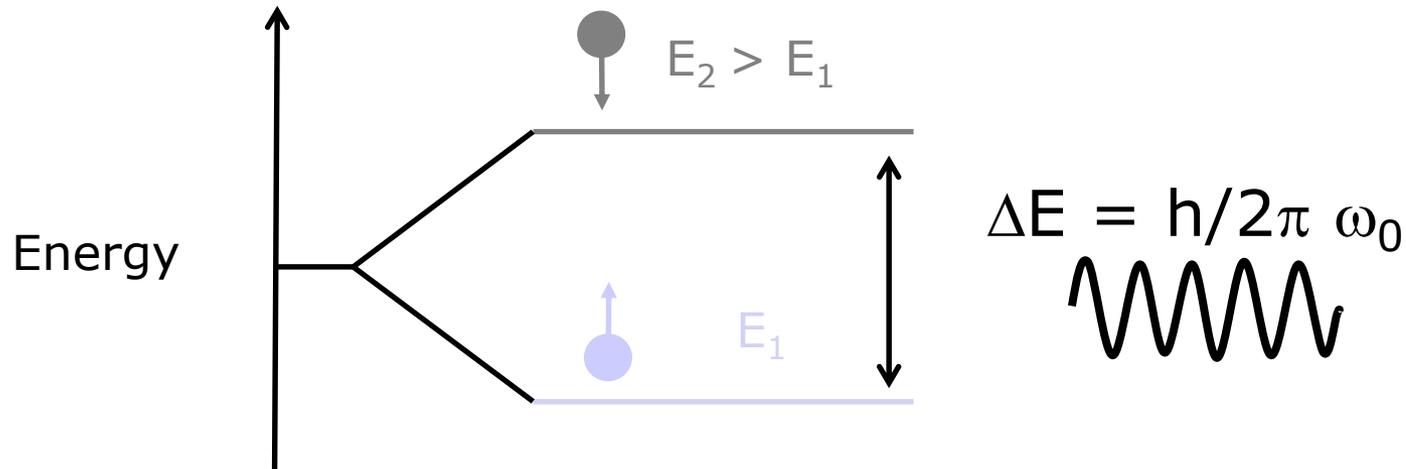
# Macroscopic sample

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# Magnetic Resonance

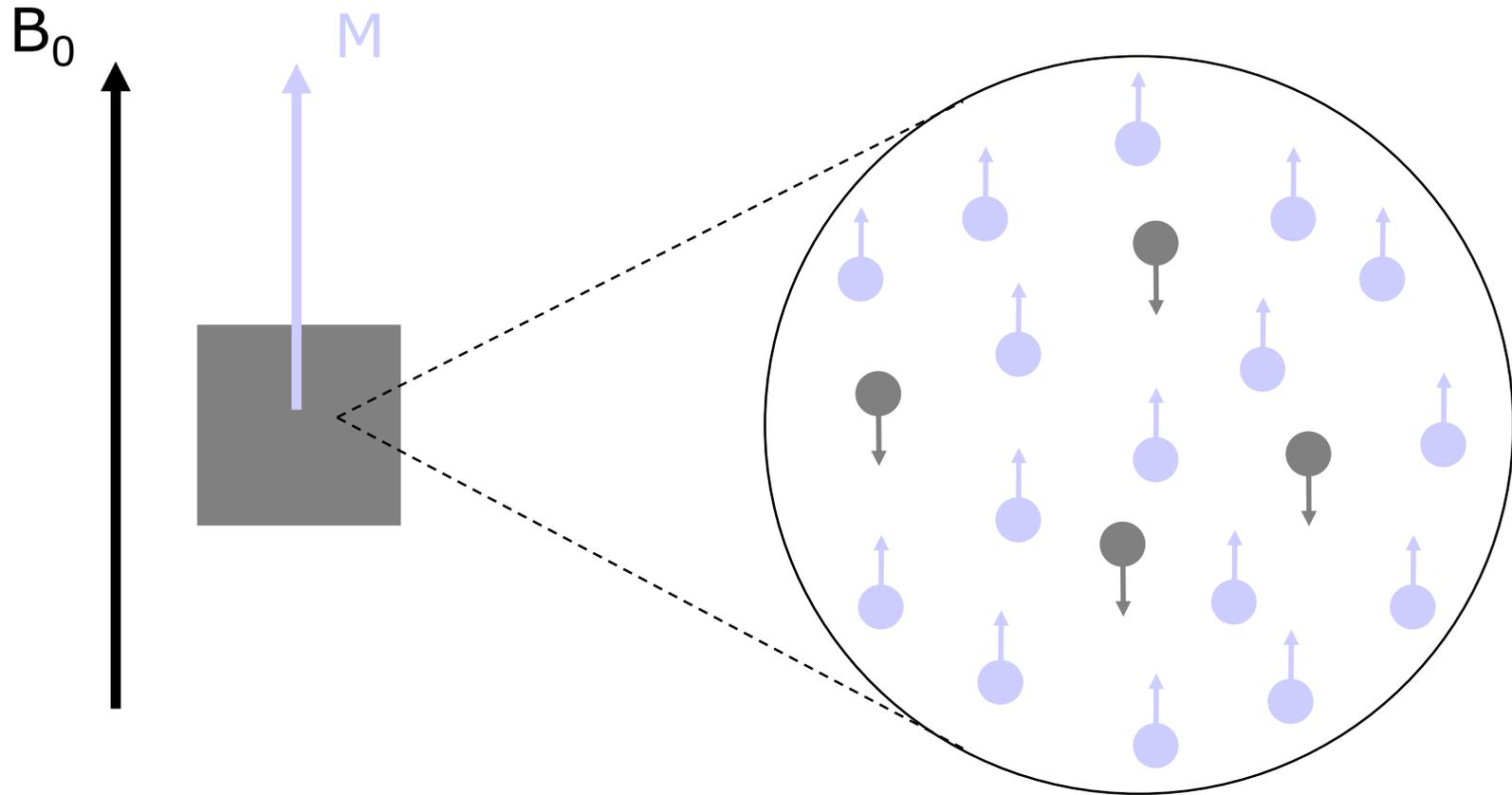
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- Exchange of energy between two systems at a specific energy is called **resonance**.
- **Magnetic resonance** corresponds to the energetic interaction between **spins** and **electromagnetic radiofrequency** (RF).
- Only protons that spin with the **same frequency** as the electromagnetic **RF pulse** will respond to that RF pulse.

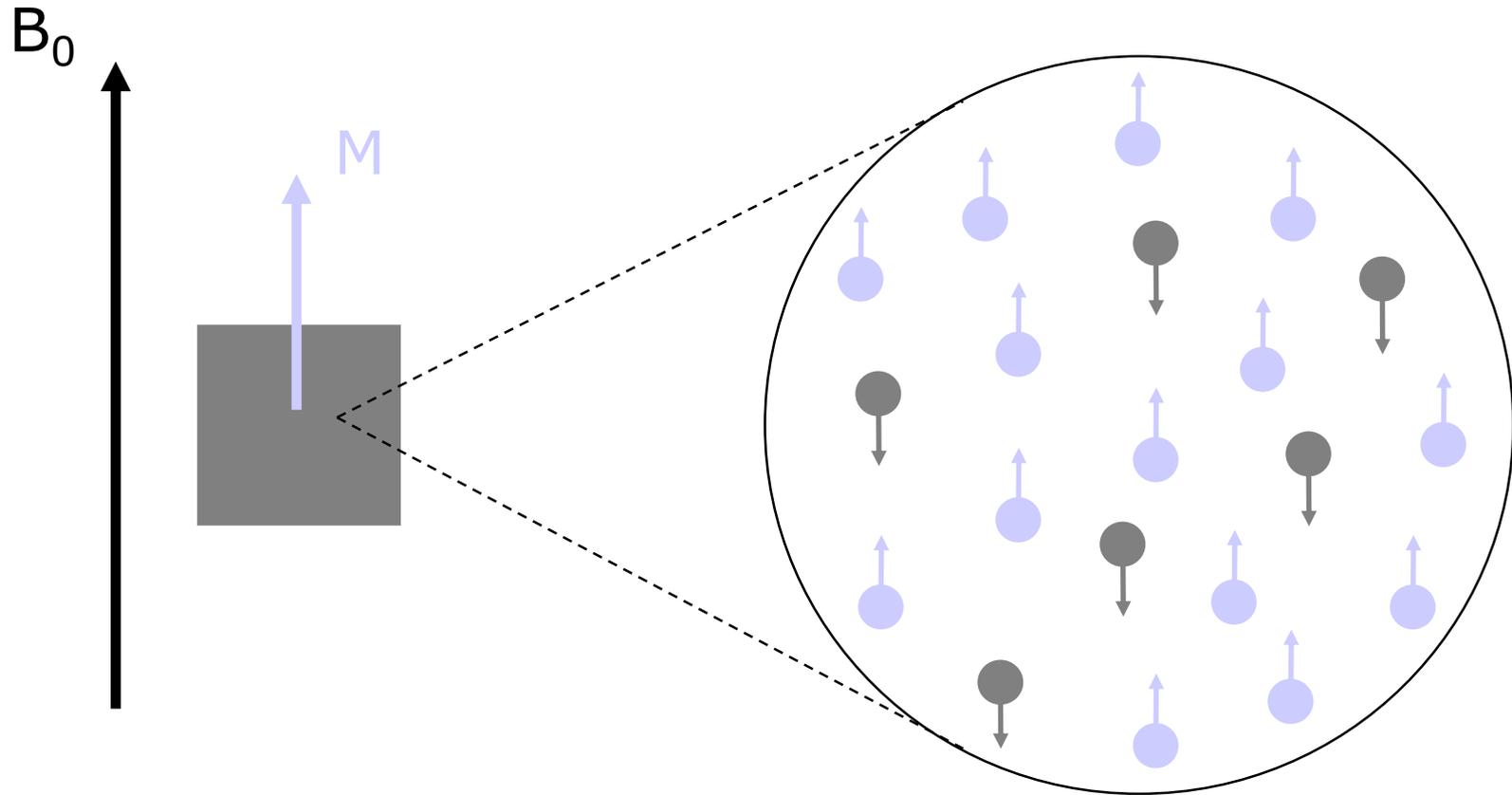
# Macroscopic sample + RF pulse (Energy)

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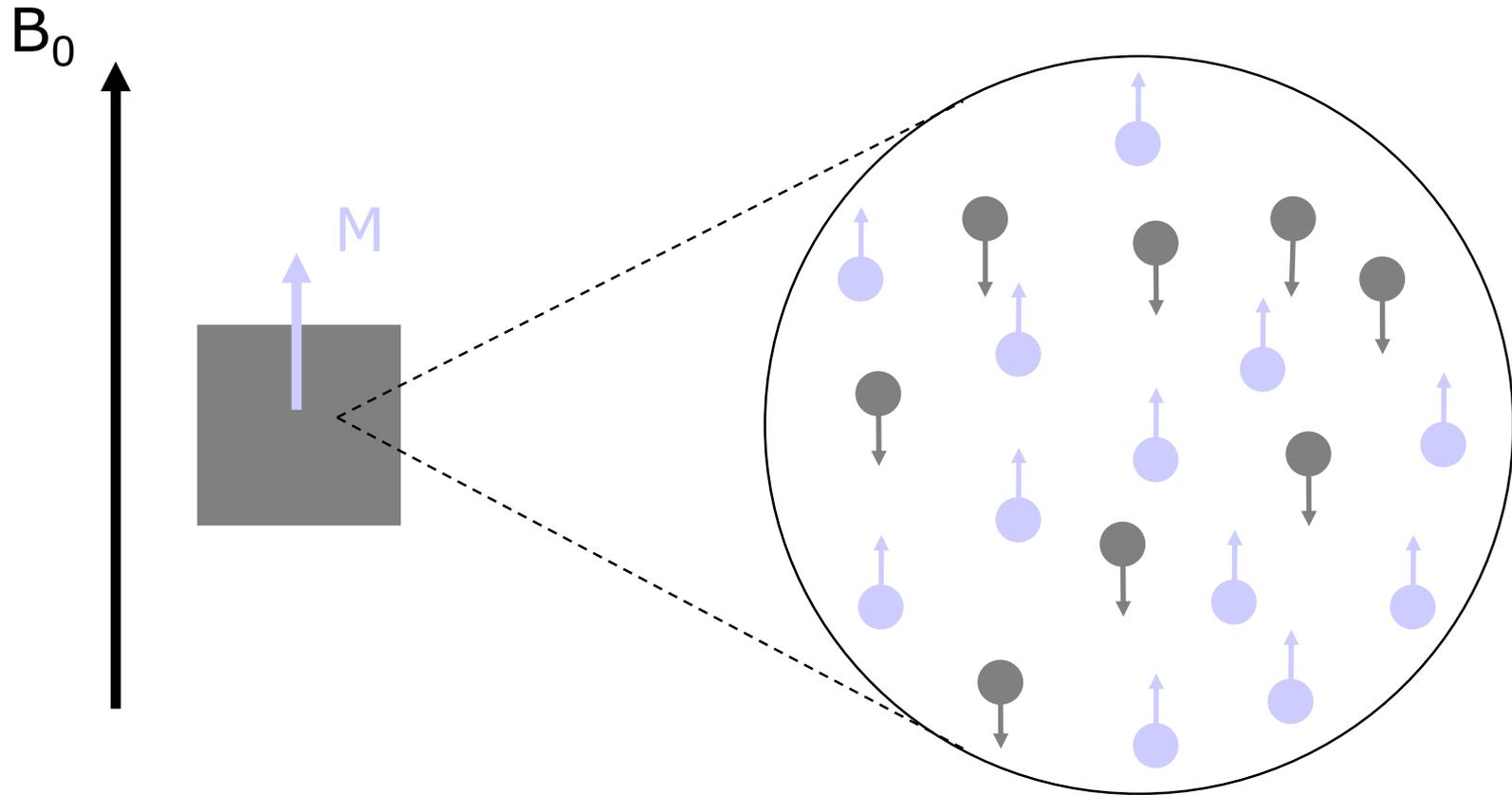
# Macroscopic sample + RF pulse (Energy)

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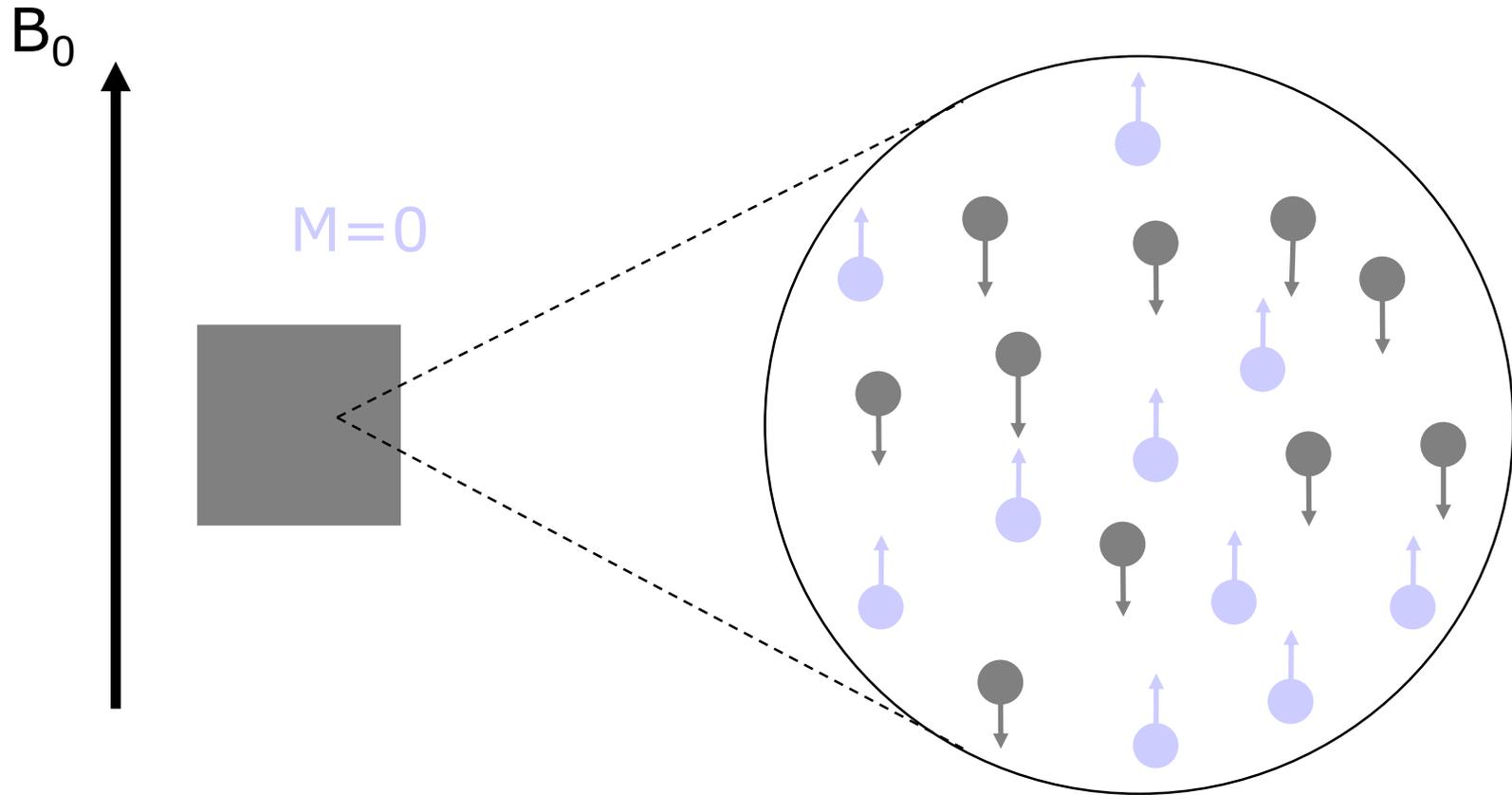
# Macroscopic sample + RF pulse (Energy)

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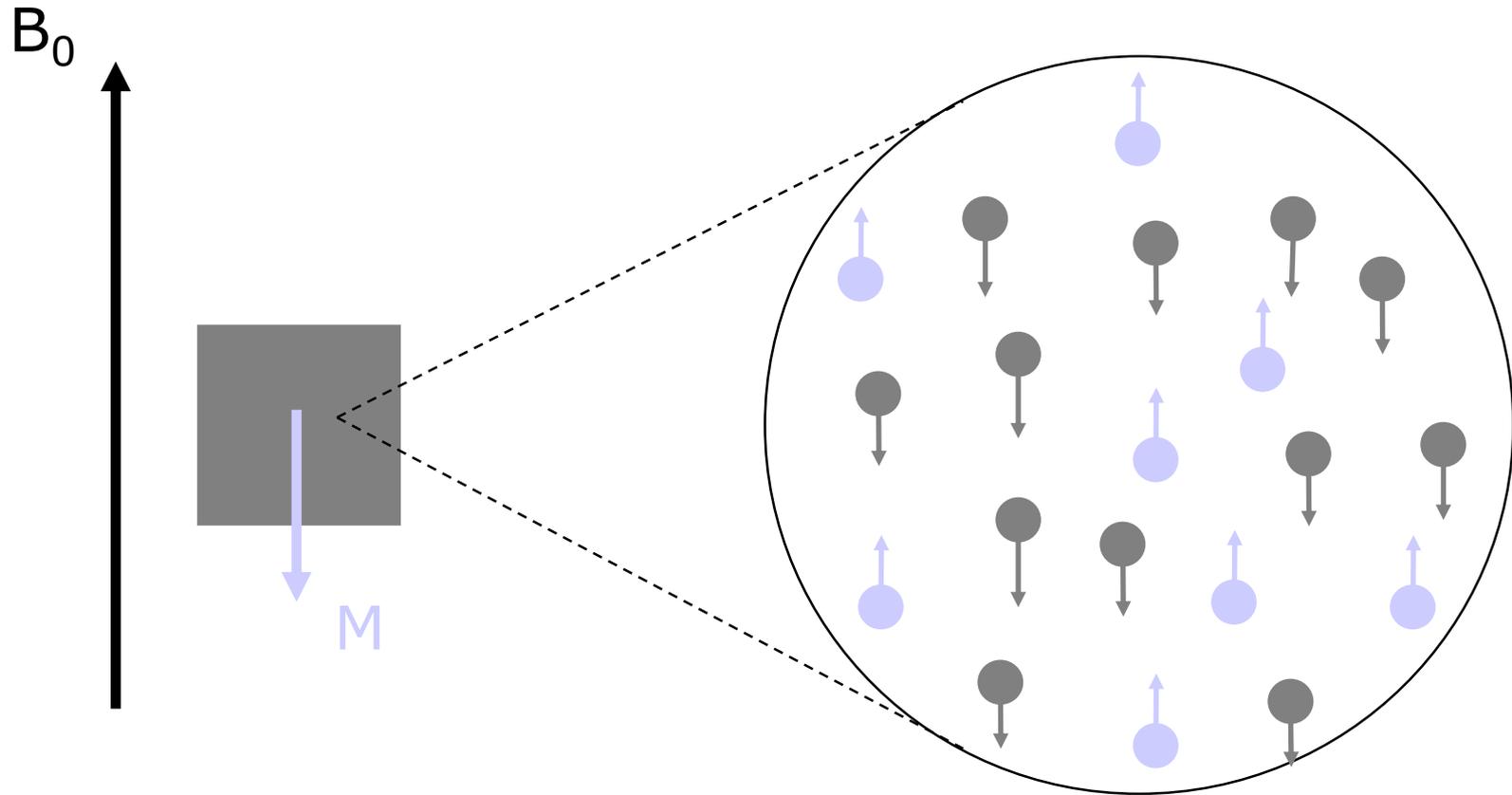
# Macroscopic sample + RF pulse (Energy)

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# Macroscopic sample + RF pulse (Energy)

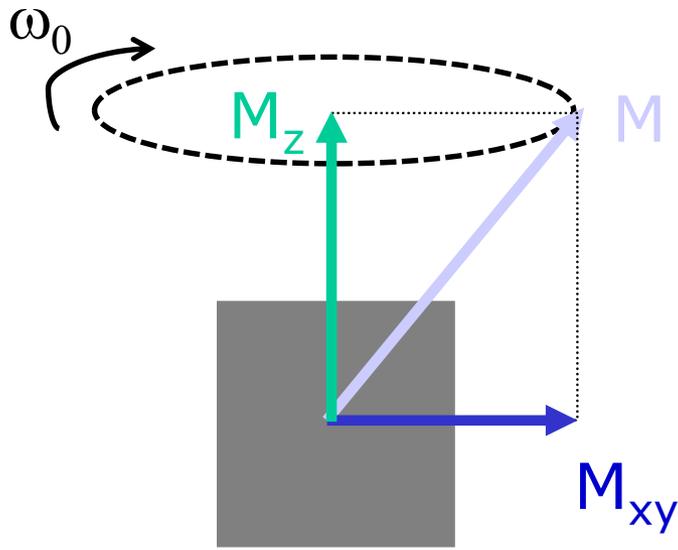
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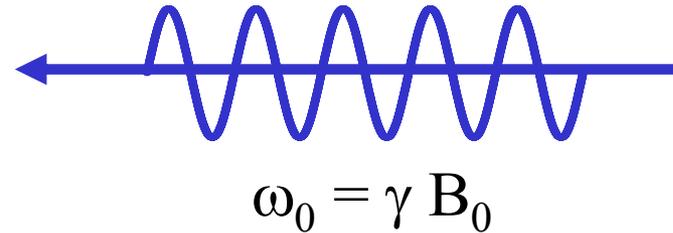
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# Excitation, Relaxation and Signal Formation

# Excitation

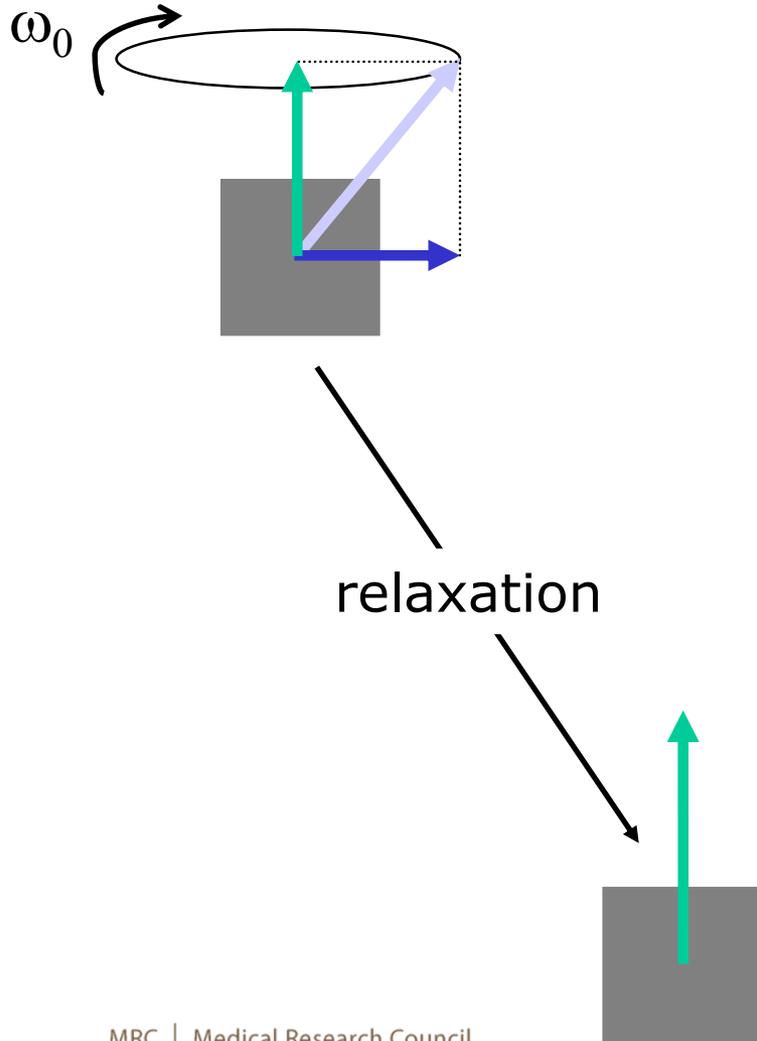


- During excitation, longitudinal magnetization decreases and a transverse magnetization appears.



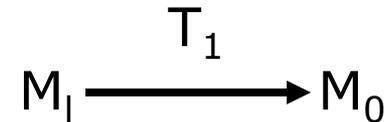
- Longitudinal magnetization is due to a difference in the number of spins in parallel and anti-parallel state.
- Transverse magnetization is due to spins getting into phase coherence.

# Relaxation

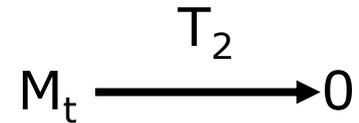


Two independent relaxation processes:

①



②

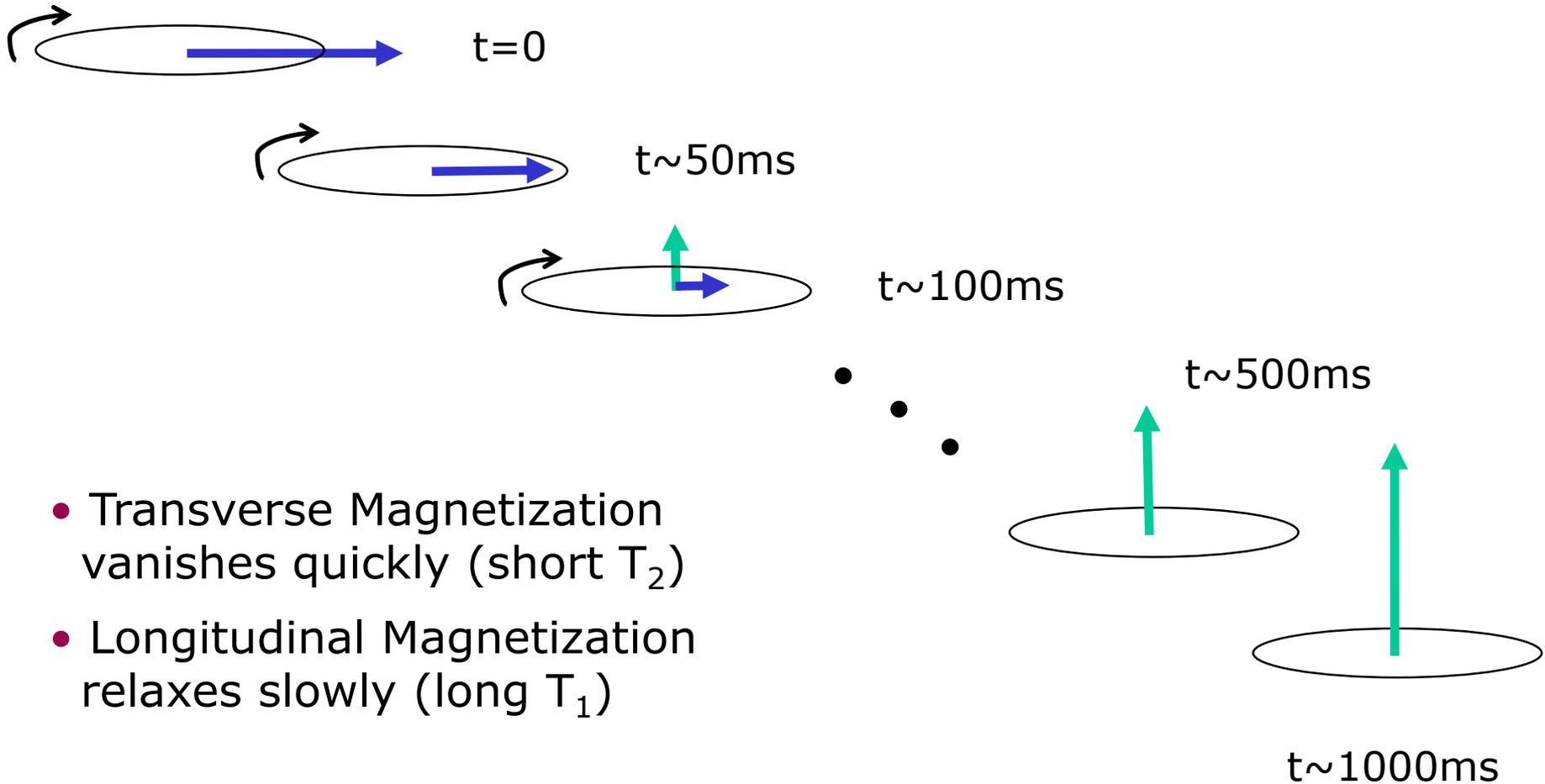


**$T_1$** : "longitudinal relaxation time"  
( $\approx 1$  s) - energy exchange between spins and their surroundings

**$T_2$** : "transverse relaxation time"  
( $\approx 100$  ms) - dephasing due to spin/spin interactions

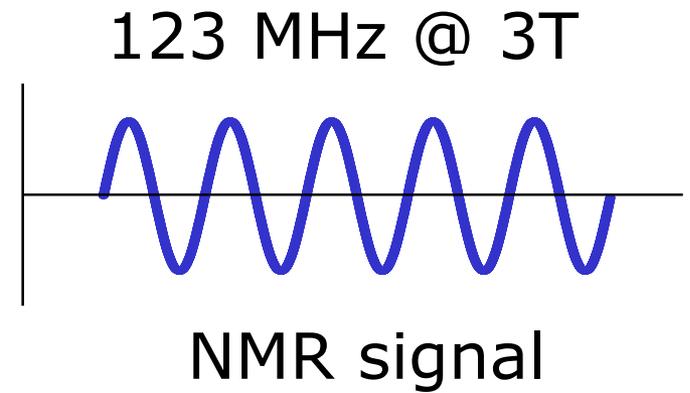
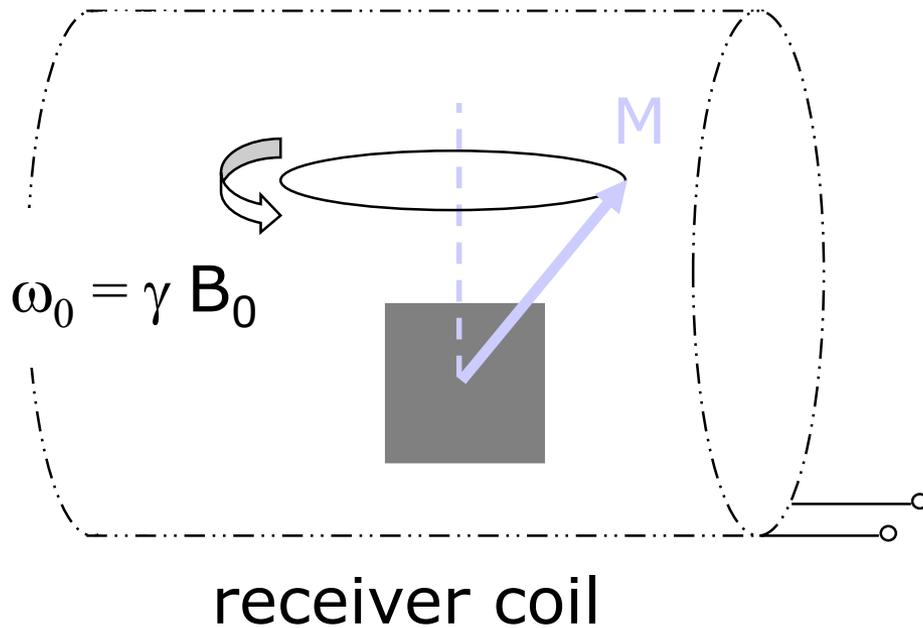
# Relaxation

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- Transverse Magnetization vanishes quickly (short  $T_2$ )
- Longitudinal Magnetization relaxes slowly (long  $T_1$ )

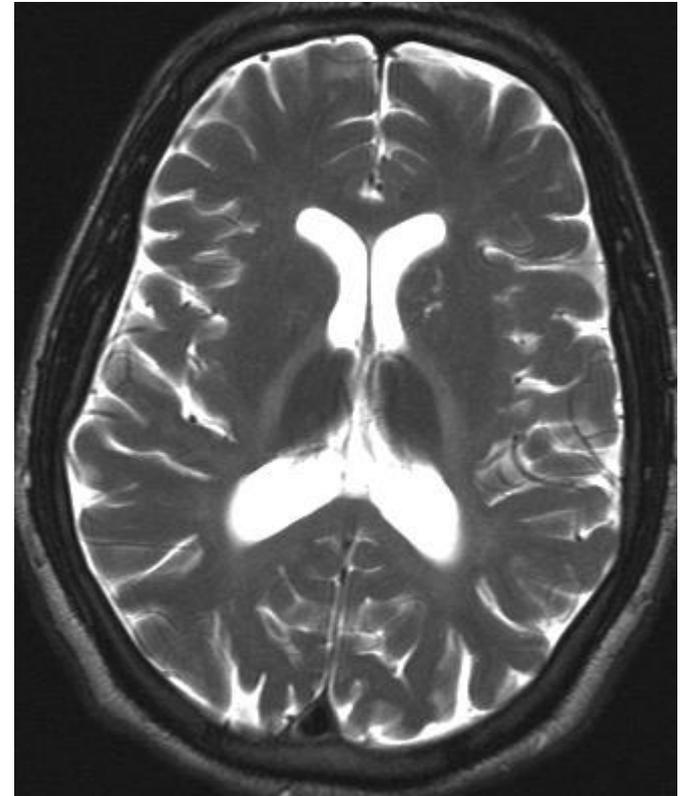
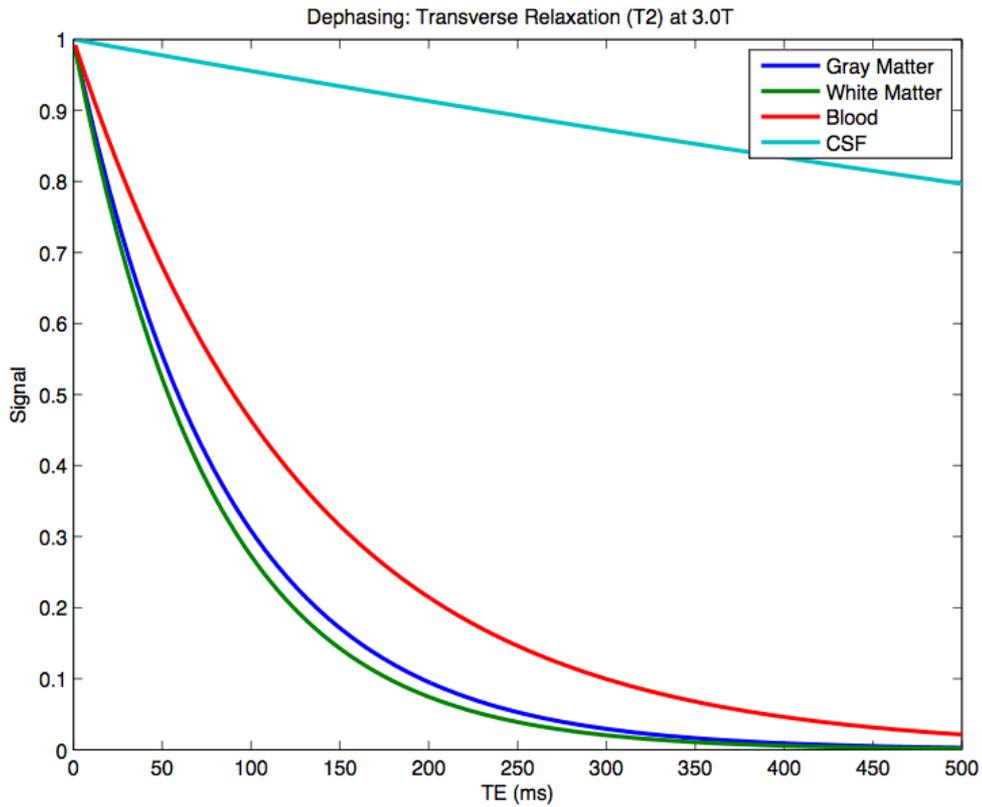
# Precession and signal induction



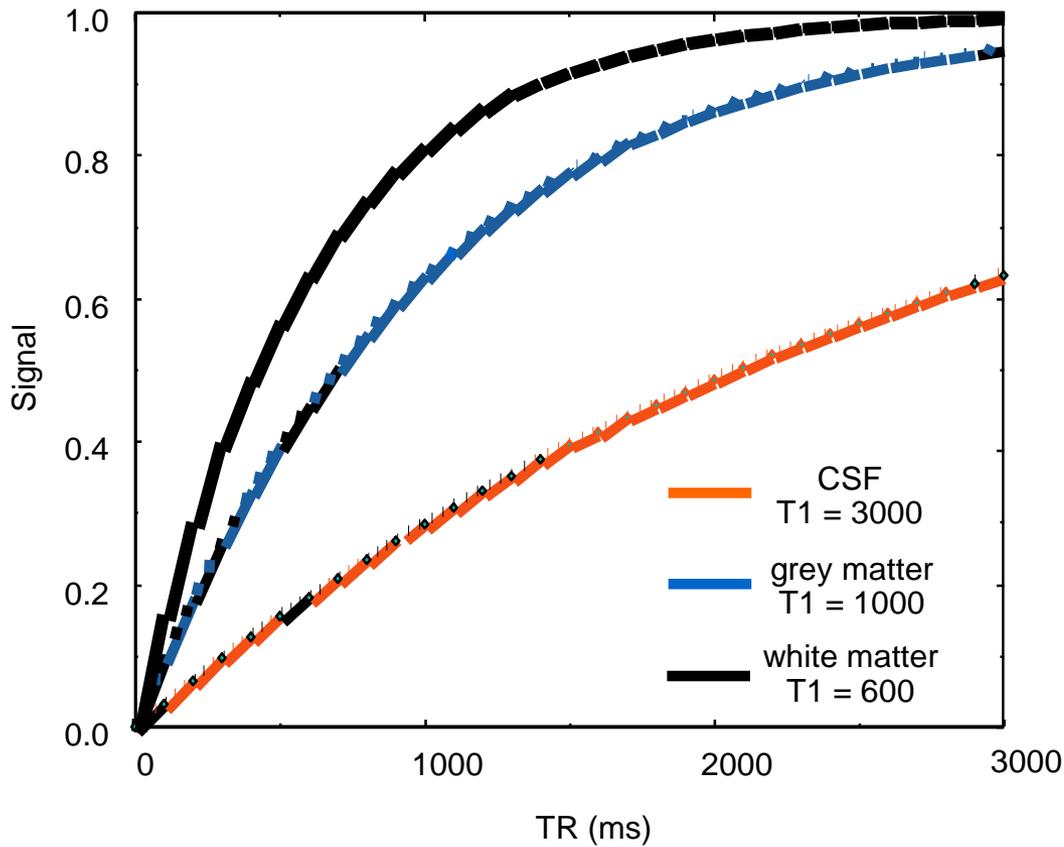
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# Image Contrast

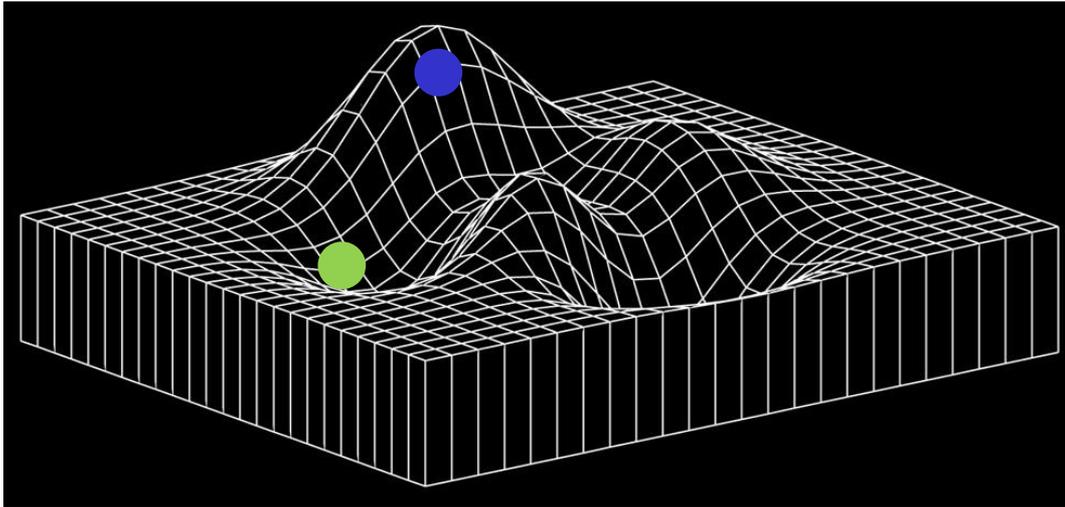
# T2-weighted contrast



# T1-weighted contrast

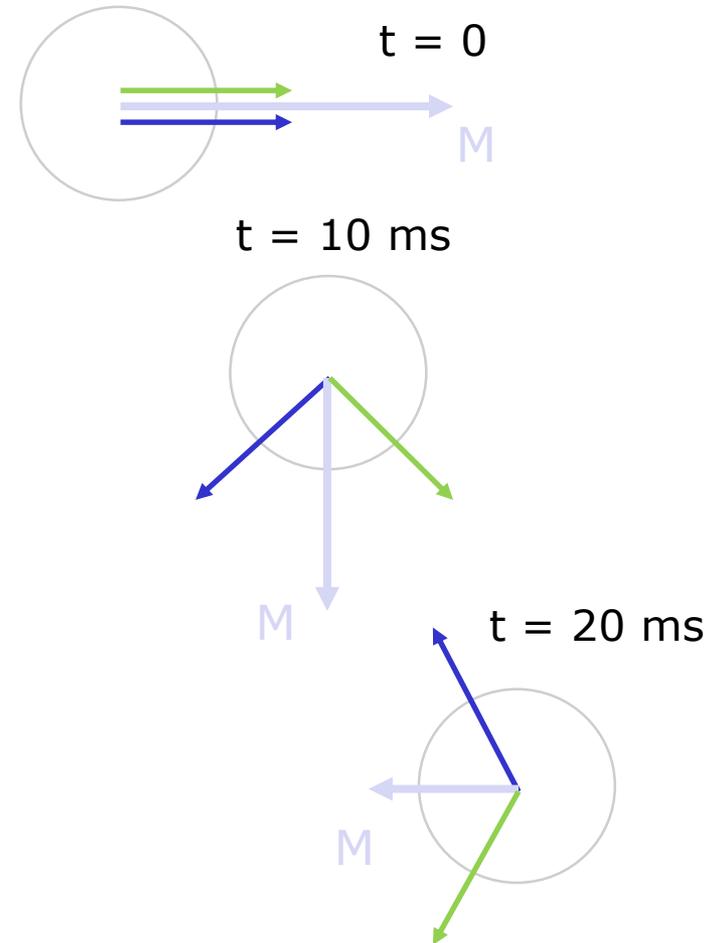


# Signal loss due to $B_0$ inhomogeneity



$$\omega_0 = \gamma B_0$$

● has higher frequency than ●



# Effective transverse relaxation ( $T_2^*$ )

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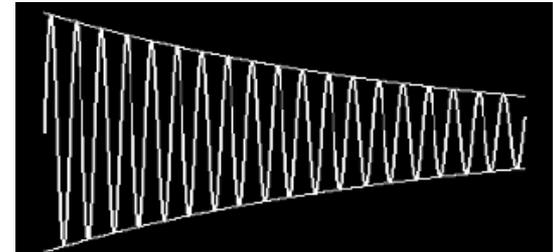
Transverse relaxation ( $T_2$ )

Spin dephasing as a result of magnetic field inhomogeneities

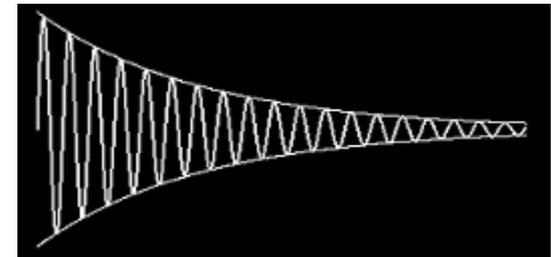
Effective transverse relaxation ( $T_2^* < T_2$ )

# Effective transverse relaxation ( $T_2^*$ )

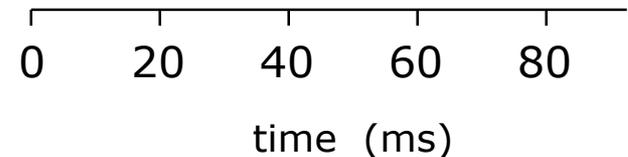
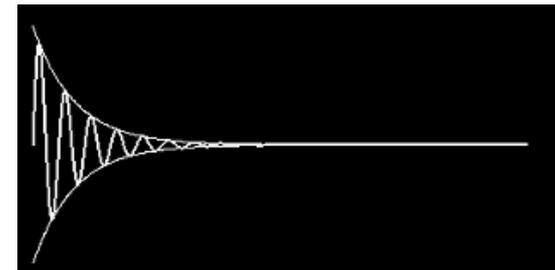
No inhomogeneities  
( $T_2^* = T_2 = 100$  ms)



Moderate inhomogeneities  
( $T_2^* = 40$  ms)

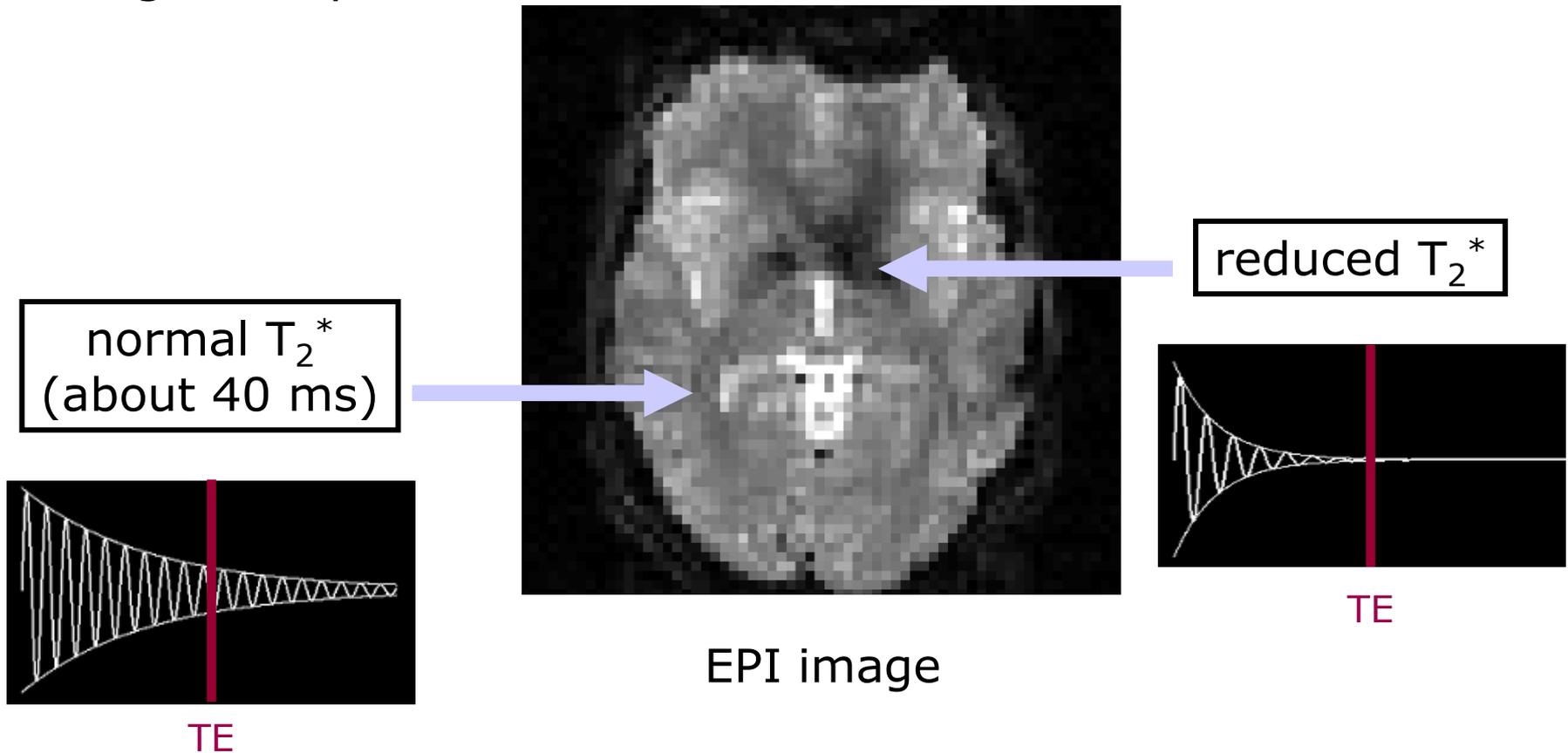


Strong inhomogeneities  
( $T_2^* = 10$  ms)



# $T_2^*$ related signal dropouts

$T_2^*$  reduction due to local field inhomogeneities  
⇒ signal dropouts



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# Part II

# Advanced Concepts

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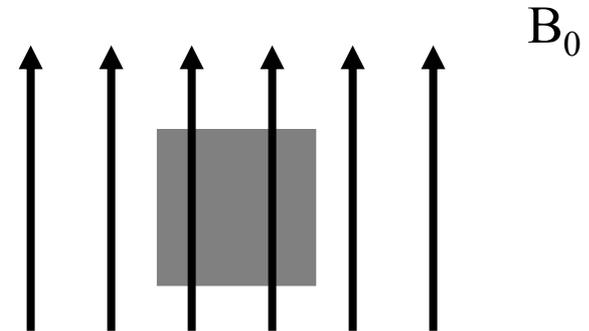
# Spatial Encoding in MRI

# The principles of MRI

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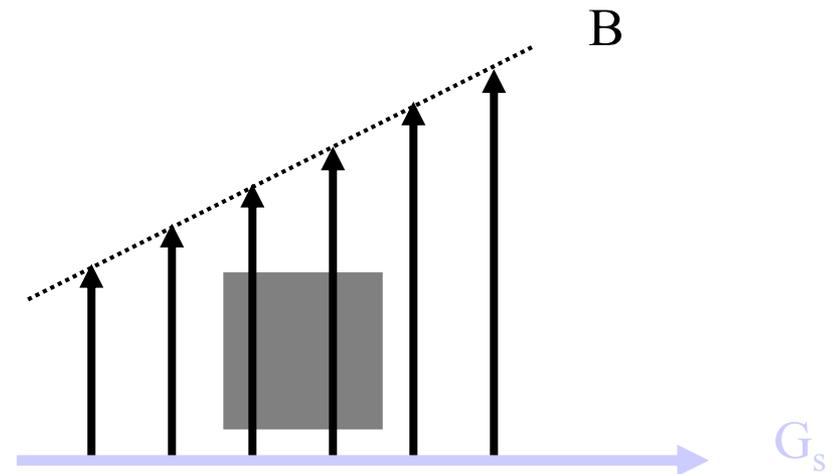
Homogeneous magnetic field

$$\omega_0 = \gamma B_0$$

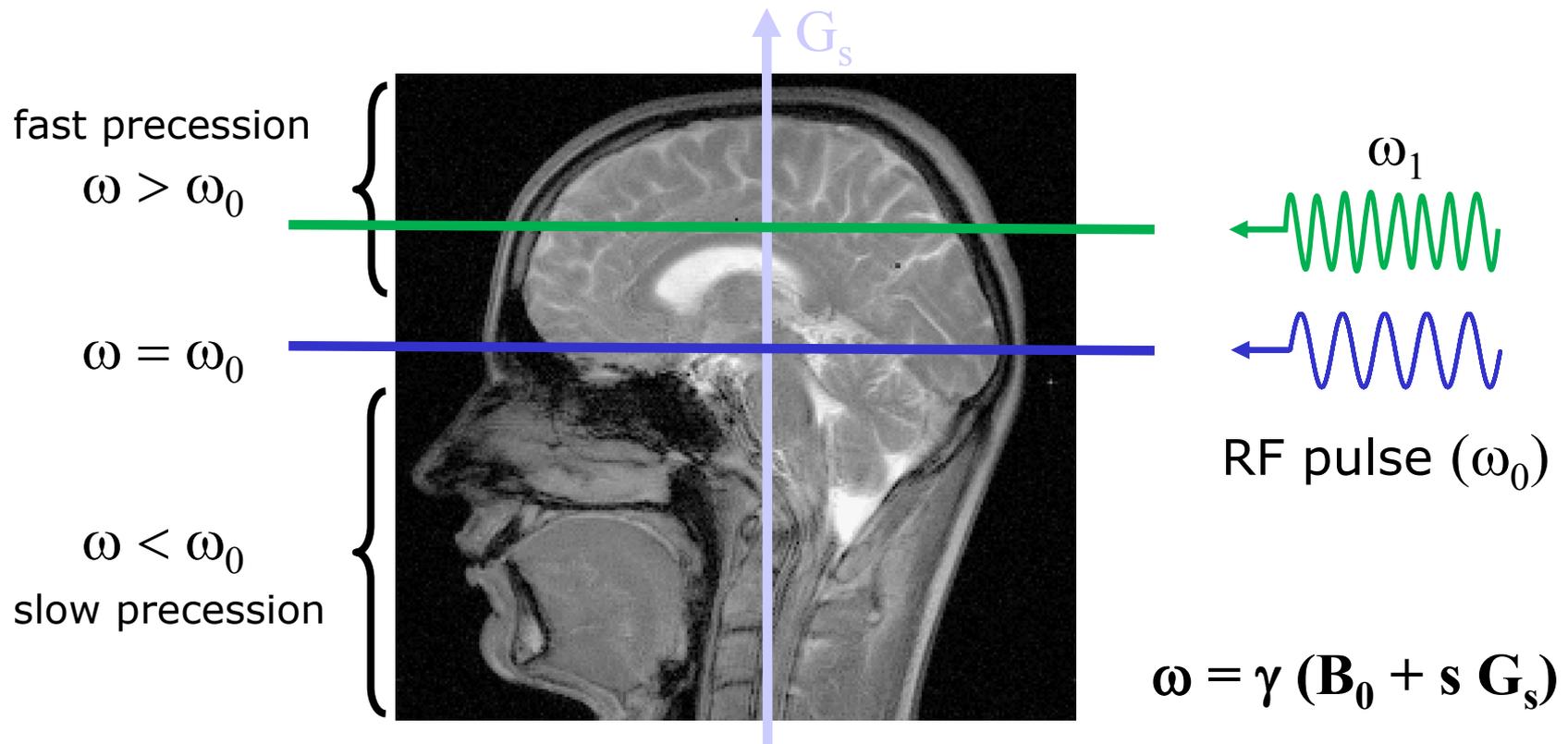


Add magnetic field gradient

$$\omega = \gamma (B_0 + s G_s)$$



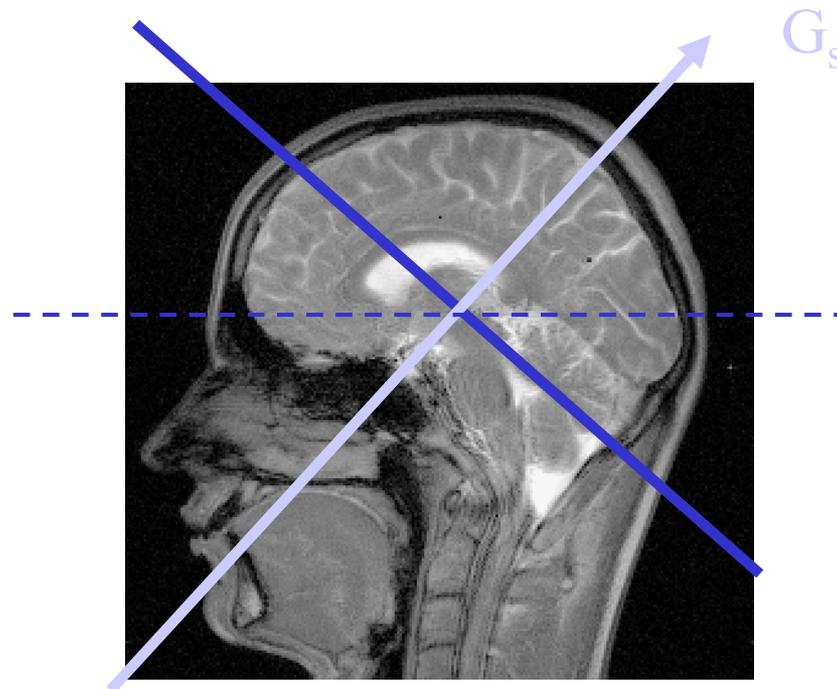
# Slice selective excitation



- Only spins in slice of interest have frequency  $\omega_0$
- RF pulse with frequency  $\omega_0$  excites only spins in slice of interest

# Slice orientation

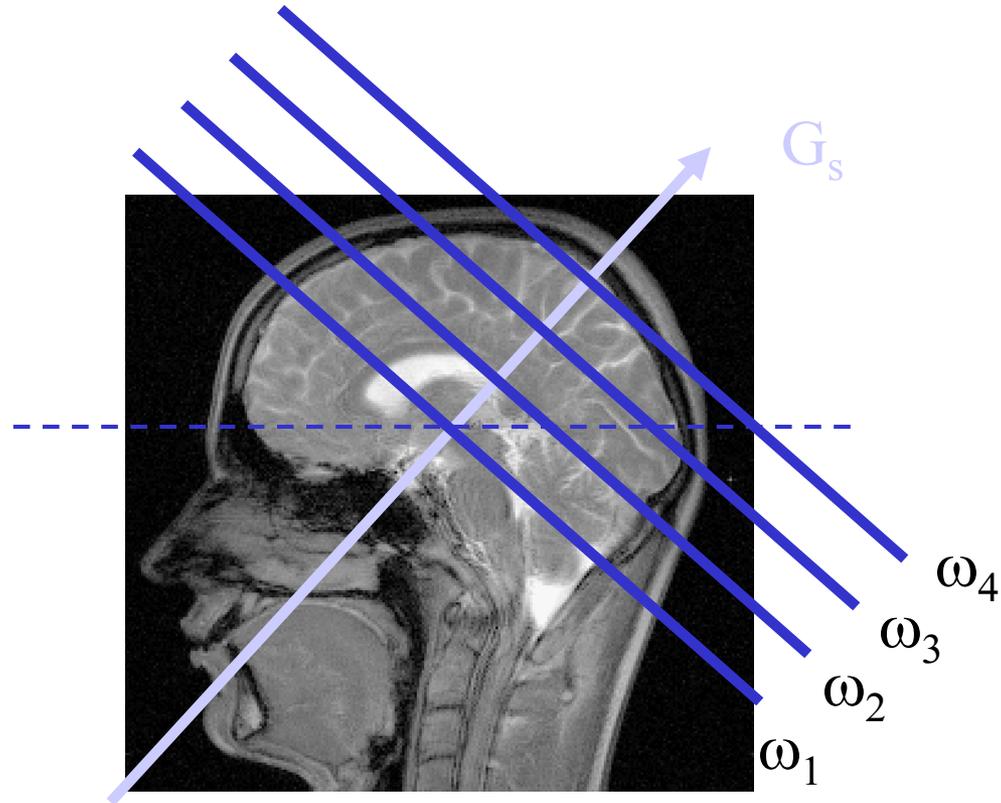
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$$\omega = \gamma (\mathbf{B}_0 + s \mathbf{G}_s)$$

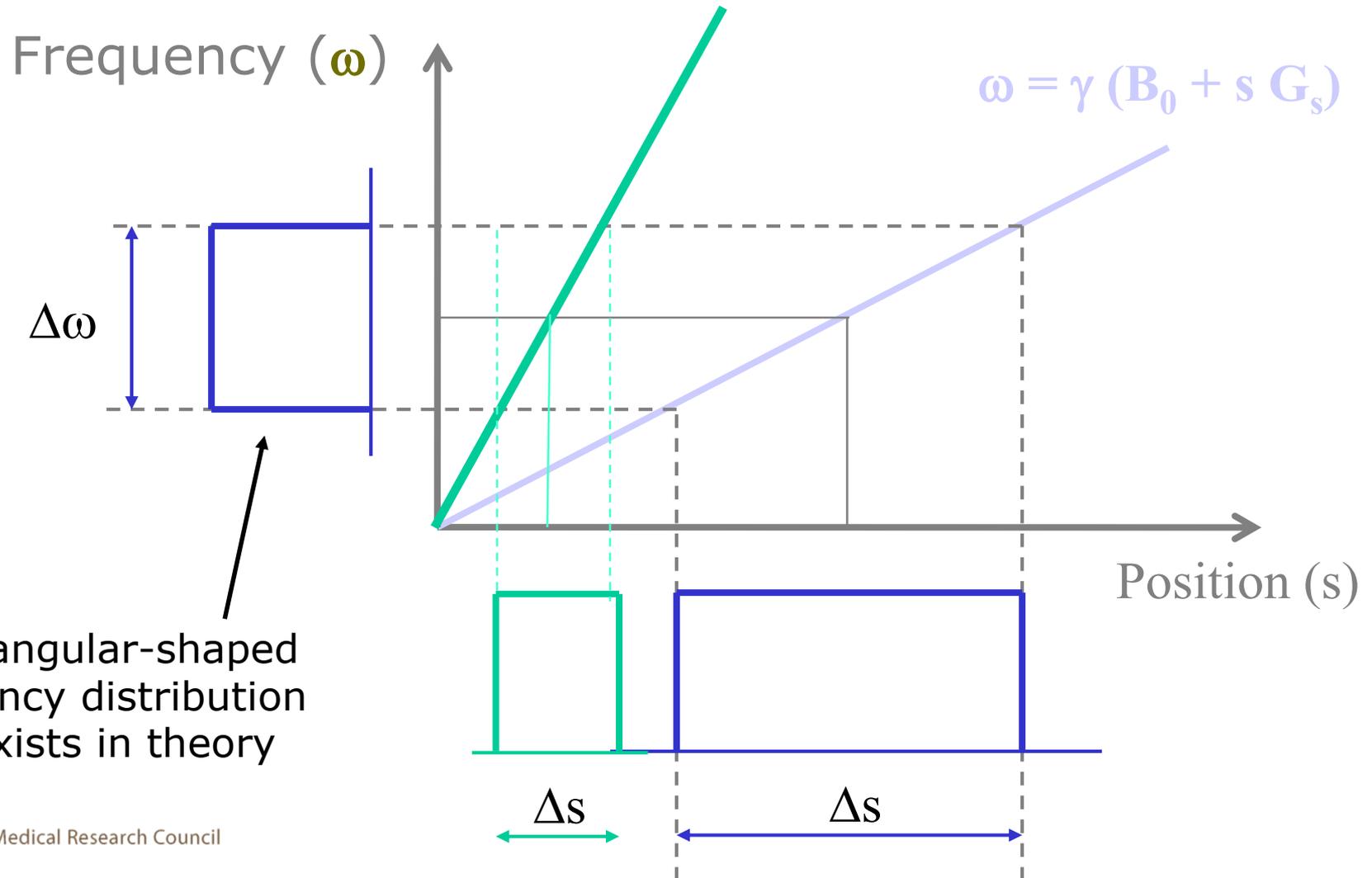
# Multi-slice MRI

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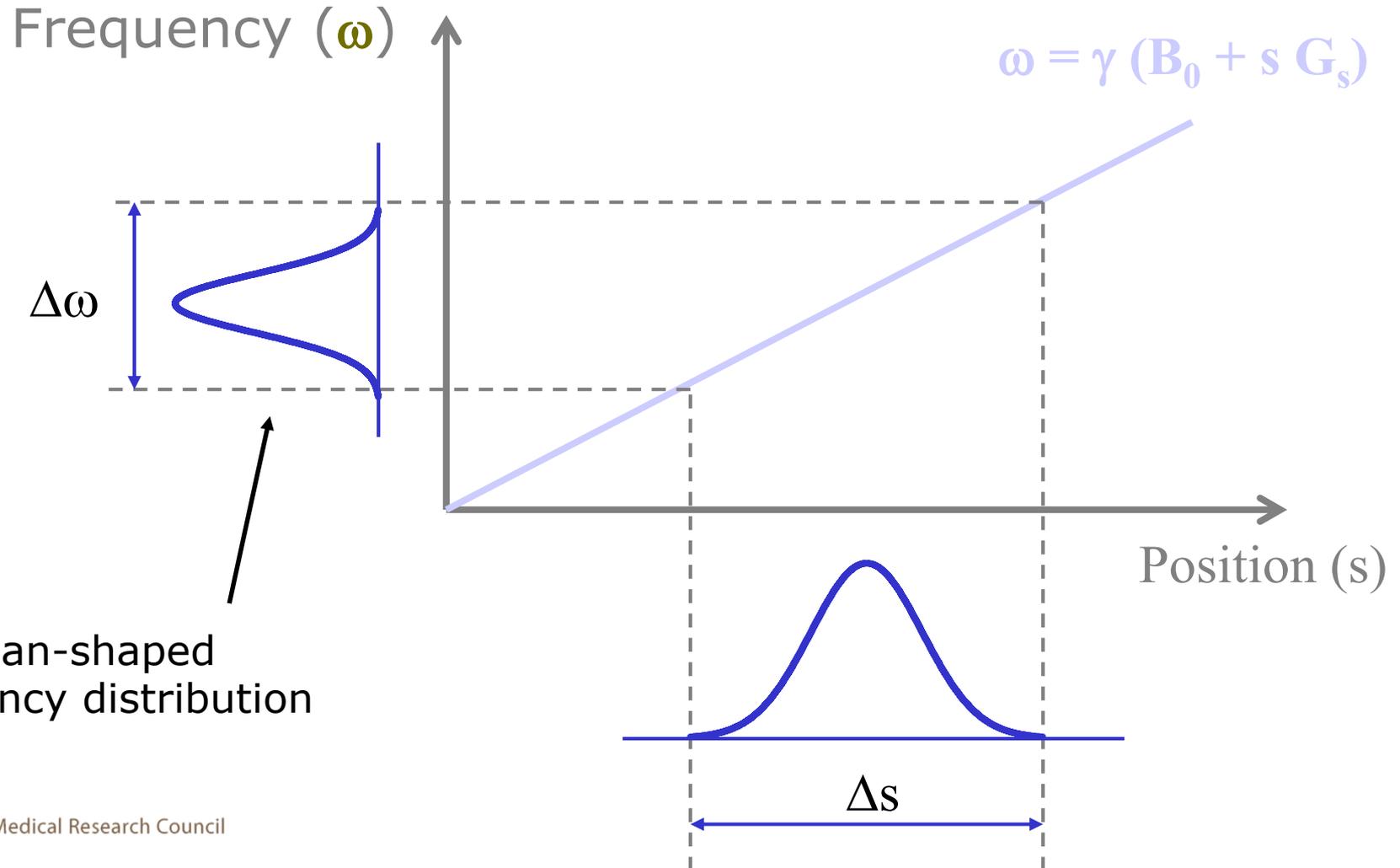
$$\omega = \gamma (\mathbf{B}_0 + s \mathbf{G}_s)$$

# Slice profile



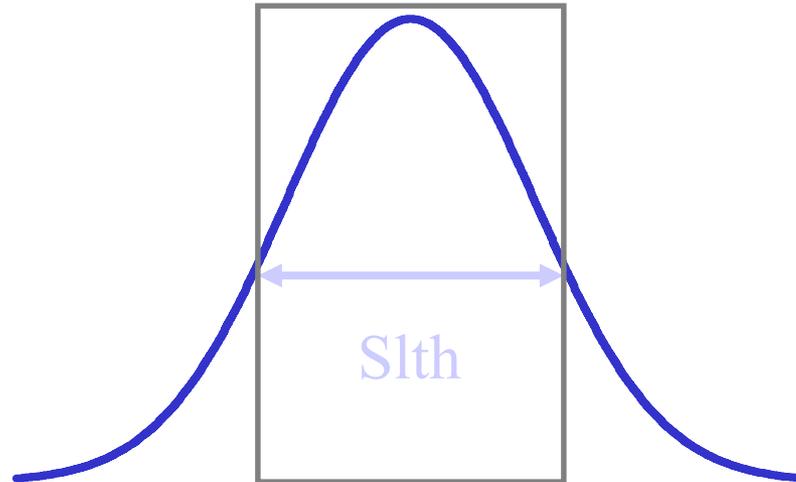
A rectangular-shaped frequency distribution only exists in theory

# Slice profile



# Slice thickness

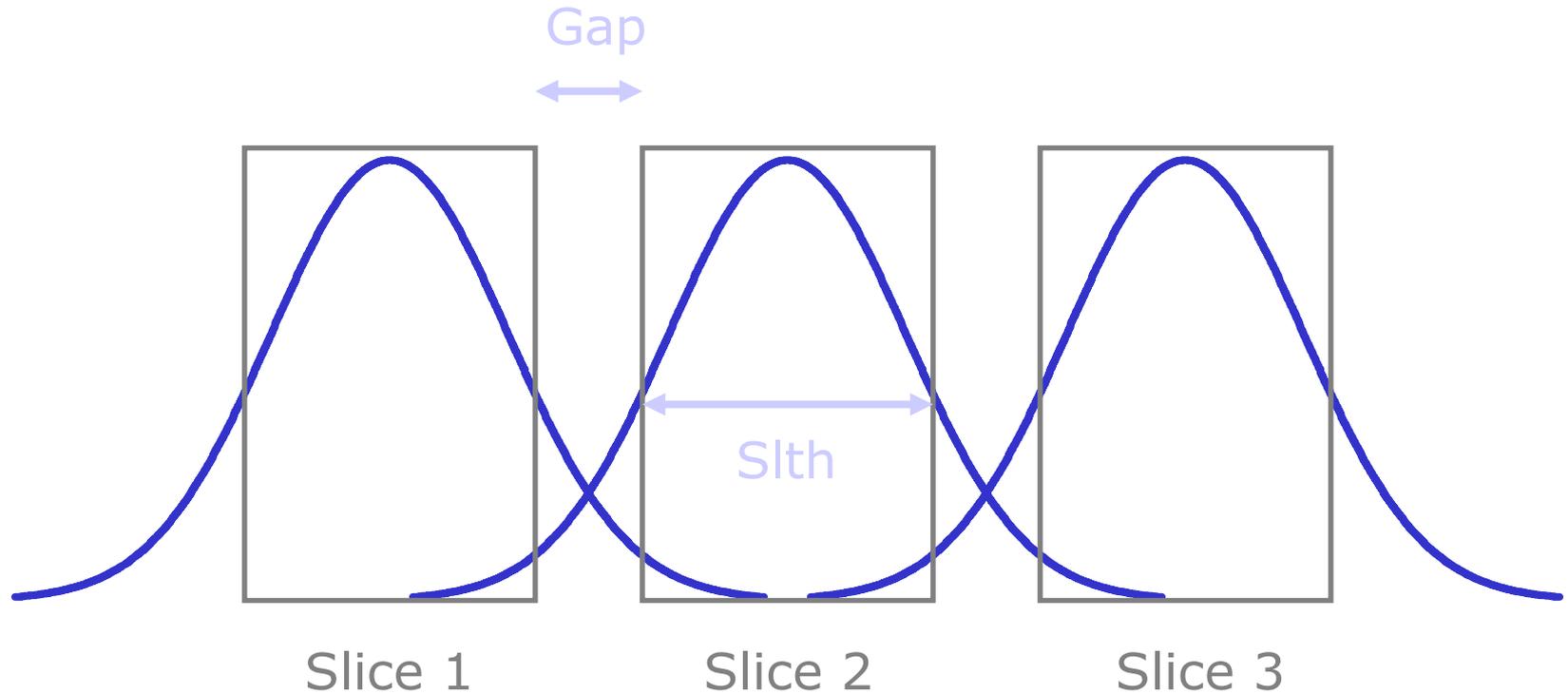
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$Slth =$  Full width at half maximum of the slice profile

# Multi-slice MRI

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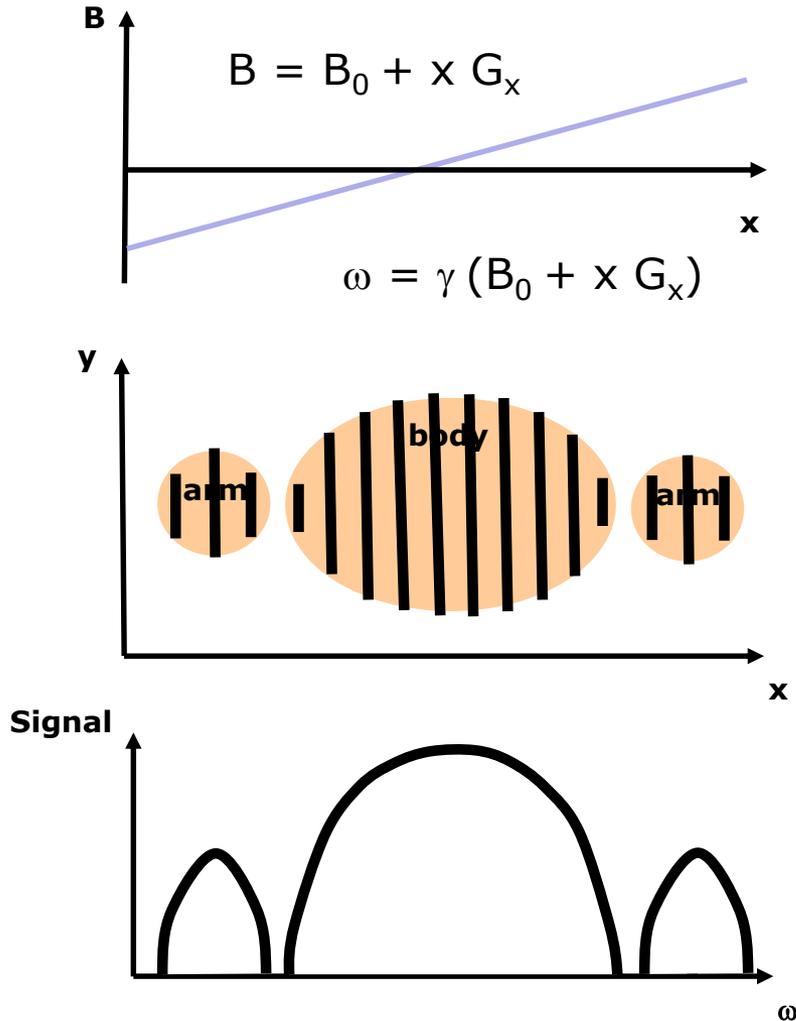


Tissue in the inter-slice gap contributes to the signal of the adjacent slices

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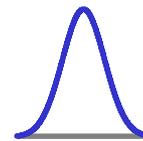
# Frequency and phase encoding

# Frequency encoding

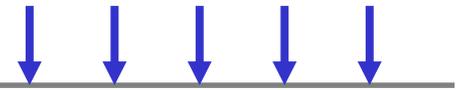


## Pulse sequence (so far)

Slice Selective excitation



Signal acquisition (digital sampling)

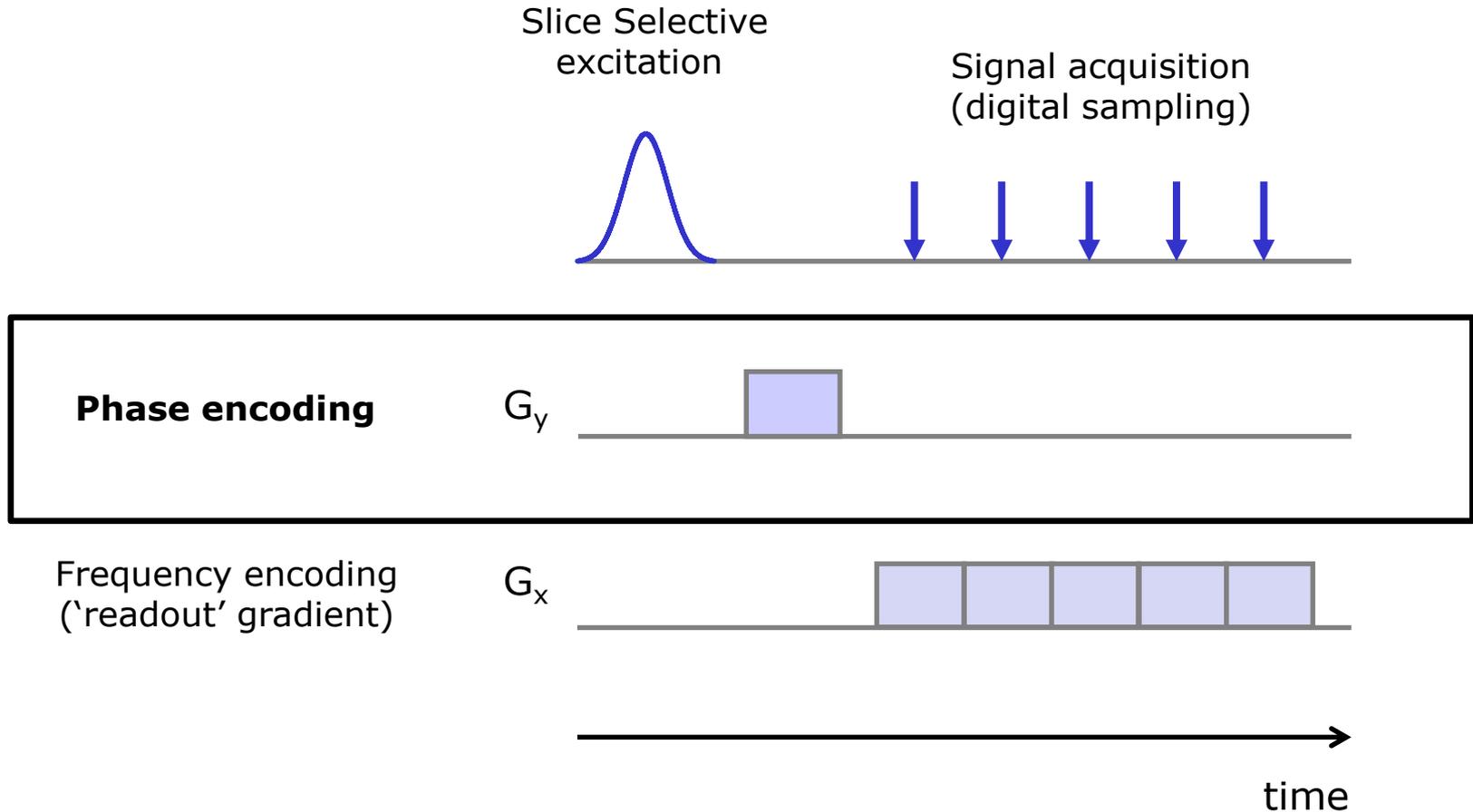


$G_x$

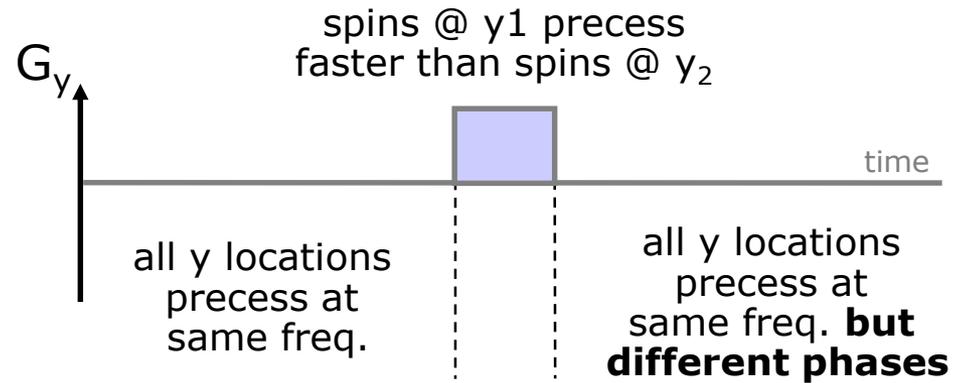
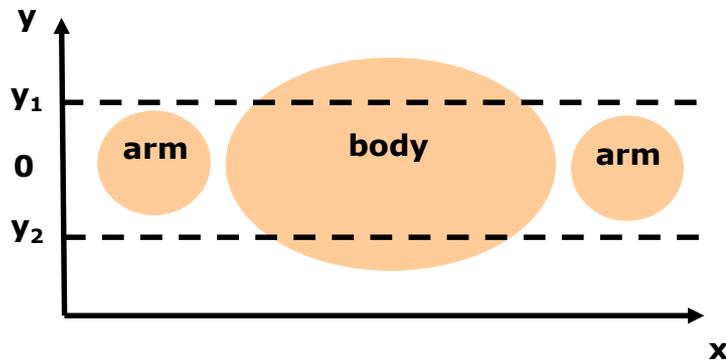


time

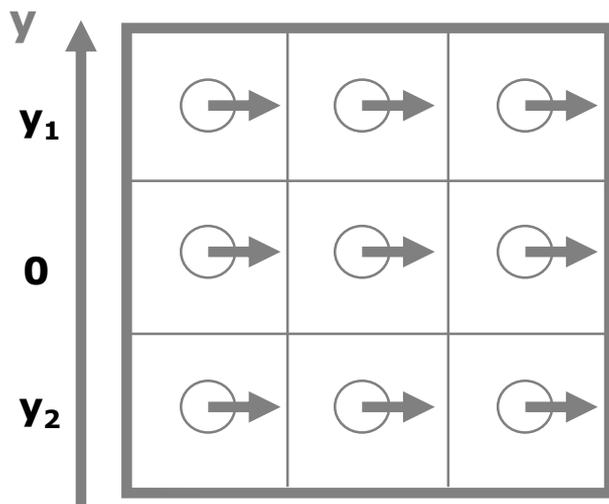
# Phase encoding



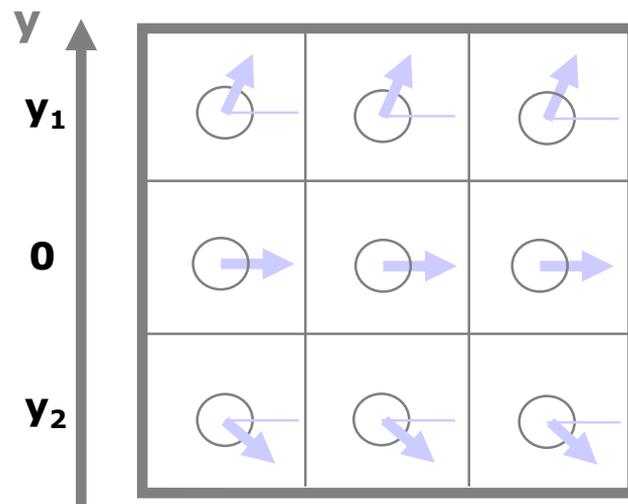
# How does phase encoding translate into spatial information?



After RF



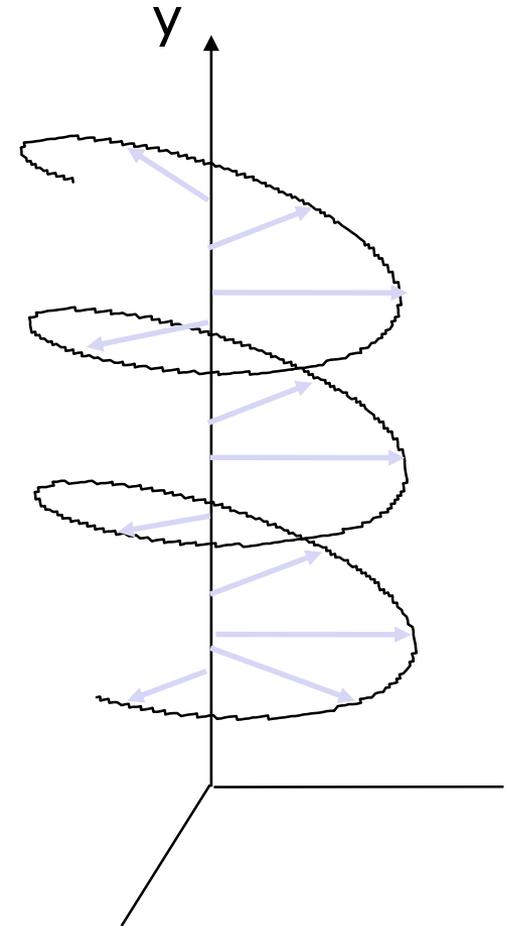
After the phase encoding gradient



# How does phase encoding translate into spatial information?

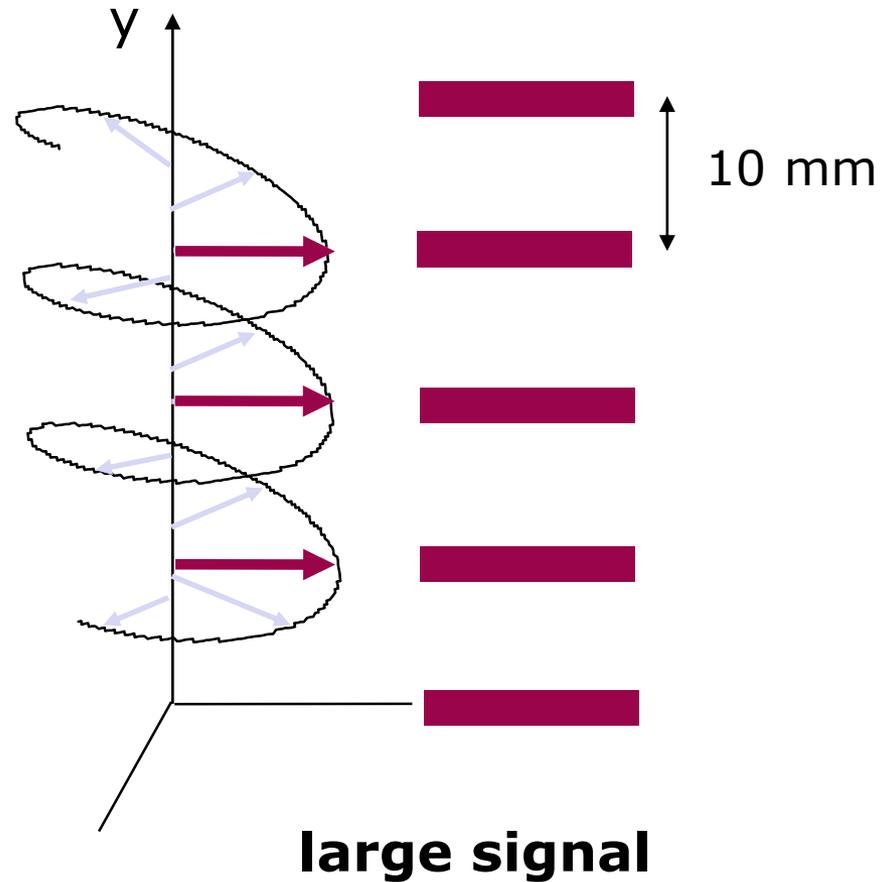
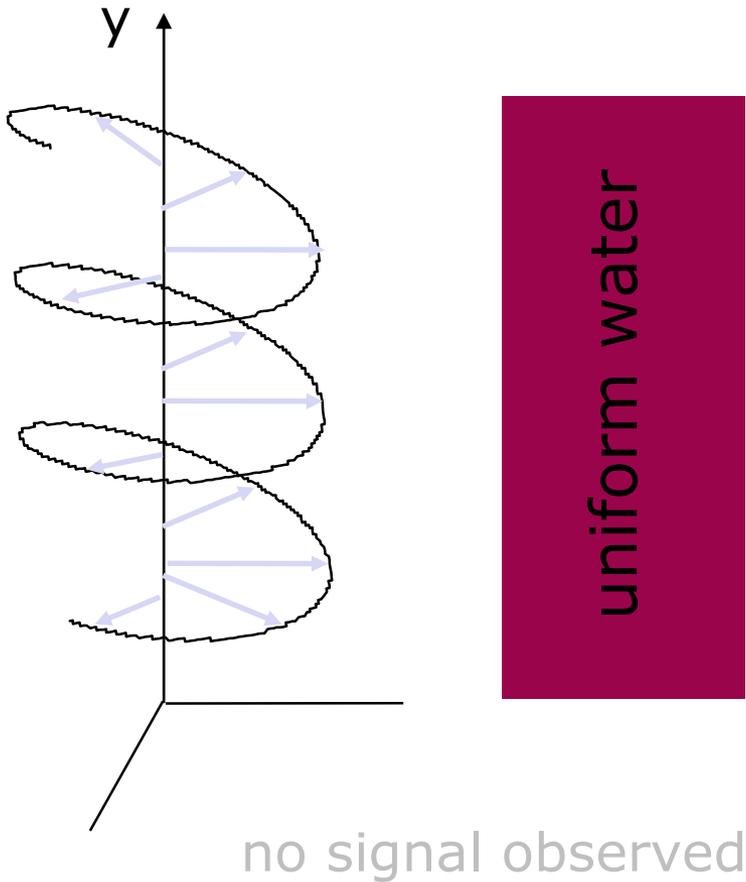
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- The magnetization in the xy plane is wound into a helix directed along y axis.
- Phases are 'locked in' once the phase encode gradient is switched off.



From L. Wald

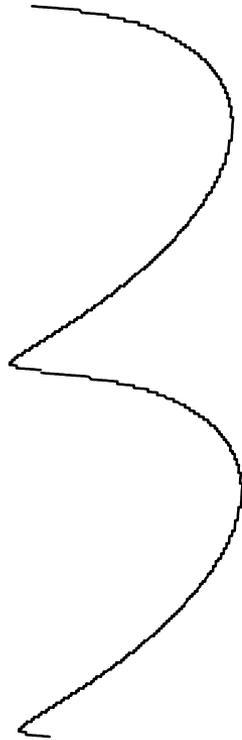
# Signal after phase encoding



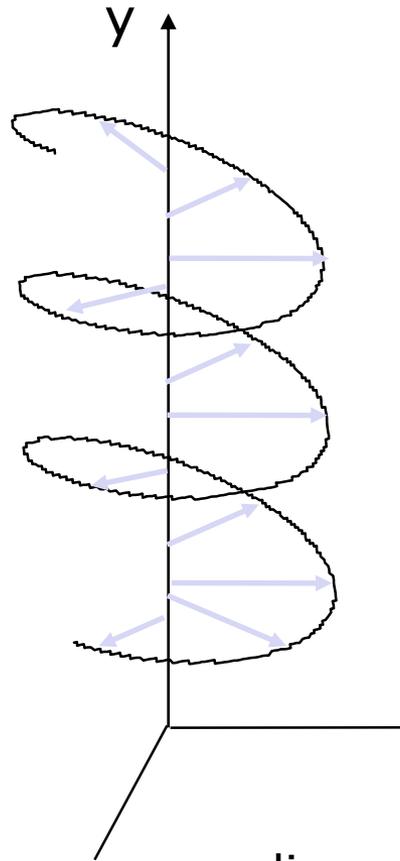
From L. Wald

# Gradient area and helix shape

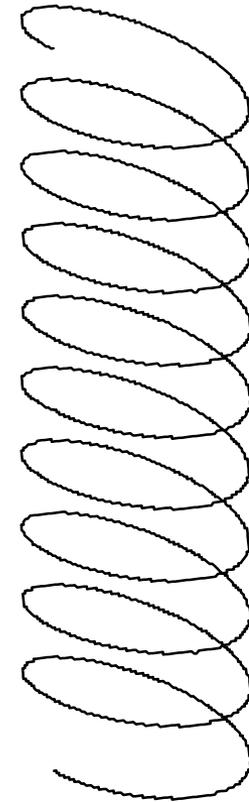
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small area



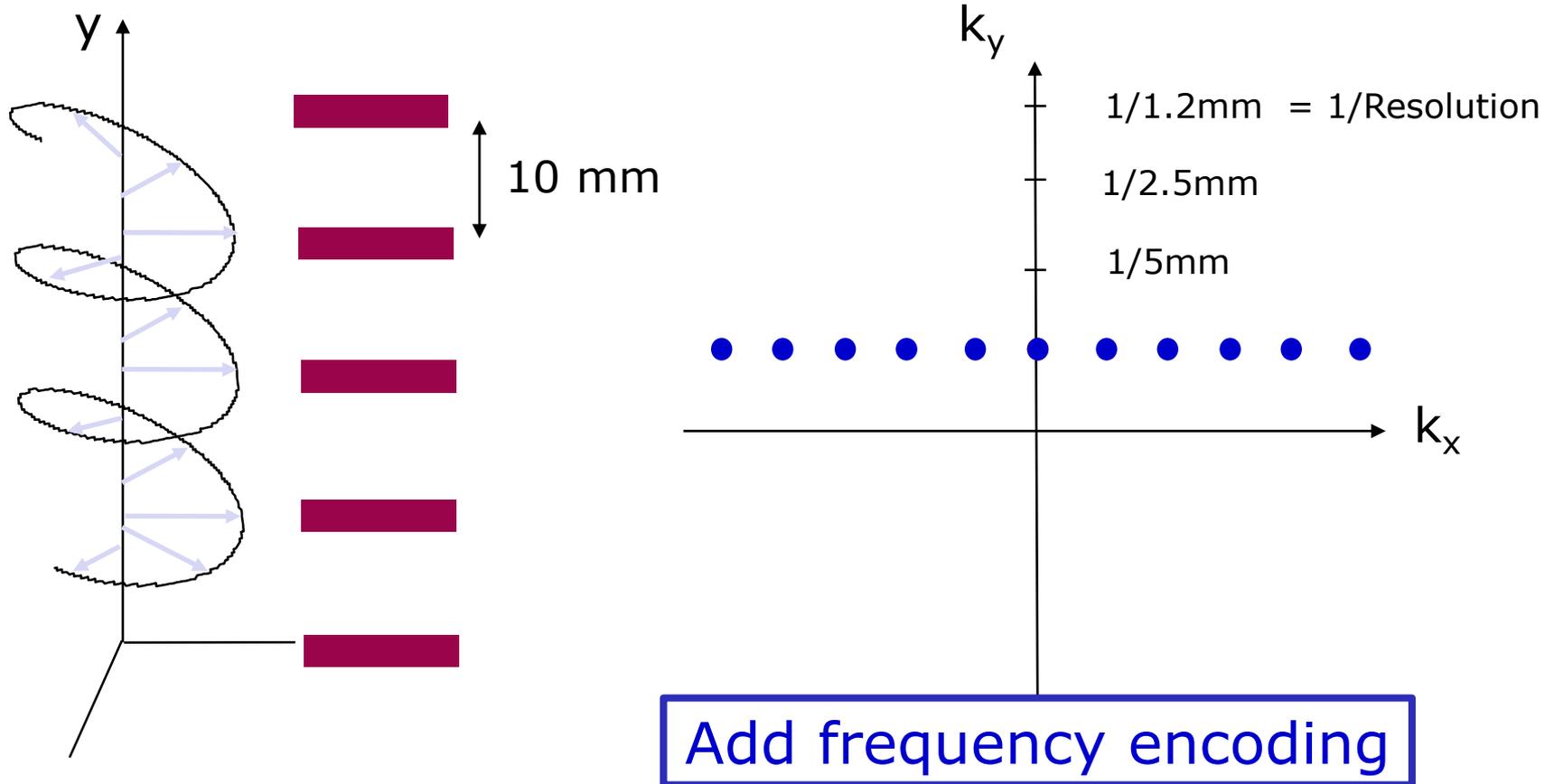
medium area



large area

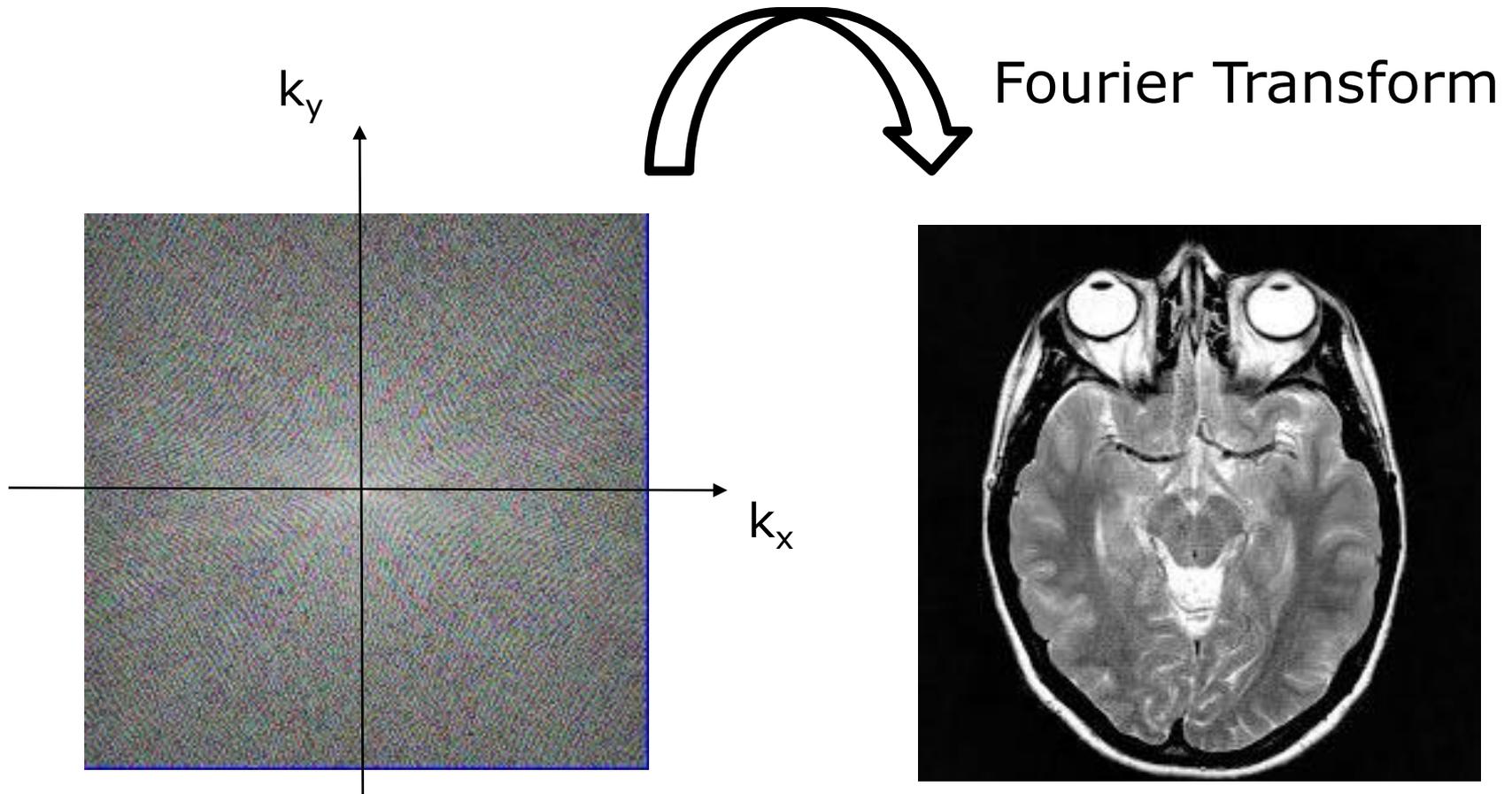
From L. Wald

# Signal intensity measured at a spatial frequency



# Image reconstruction and k-space

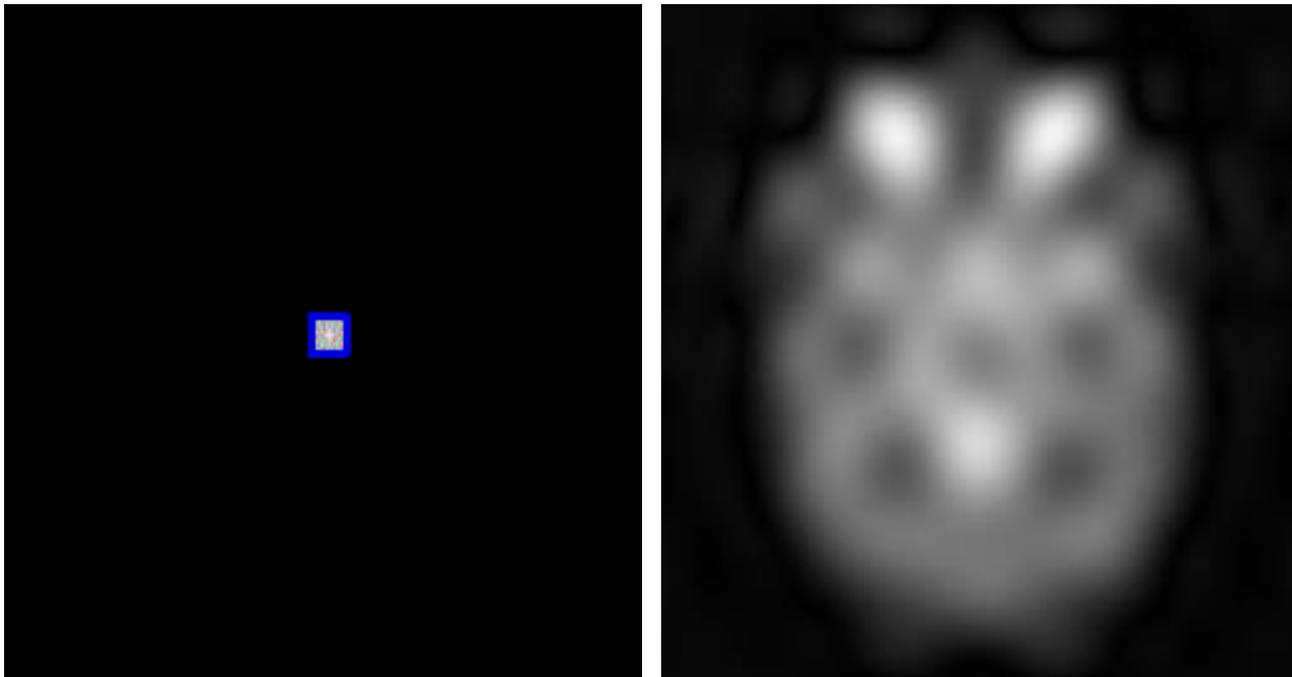
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# Spatial frequency and contrast

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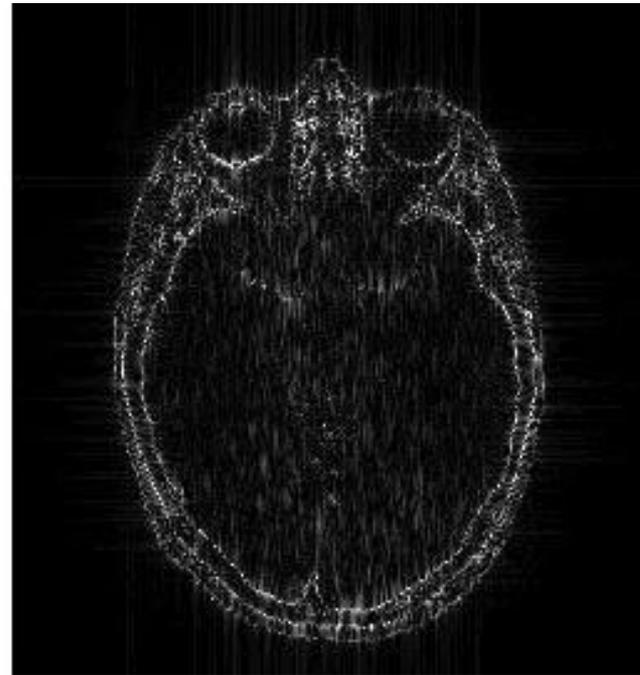
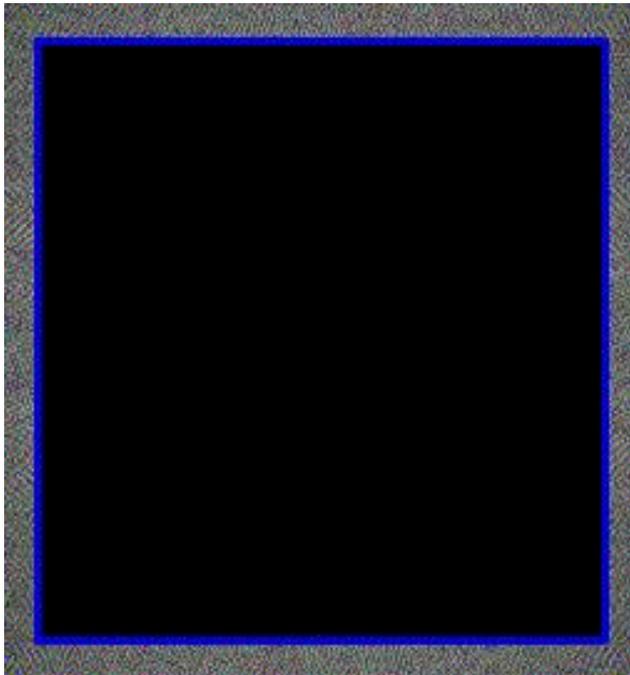
**Centre of k-space:** low spatial frequency data have the highest amplitude, giving the greatest changes in grey levels (contrast).



# Spatial frequency and contrast

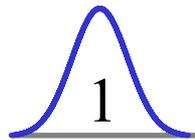
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**Periphery of k-space:** high spatial frequency data sharpens the image as they encode the edges (rapid changes of image signal as a function of position)

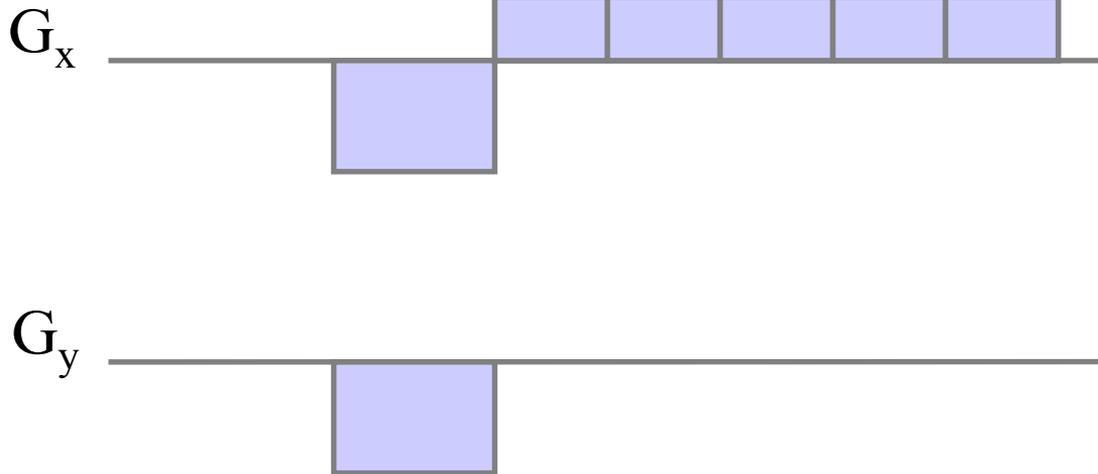
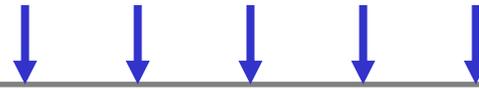


# k-space acquisition - FLASH

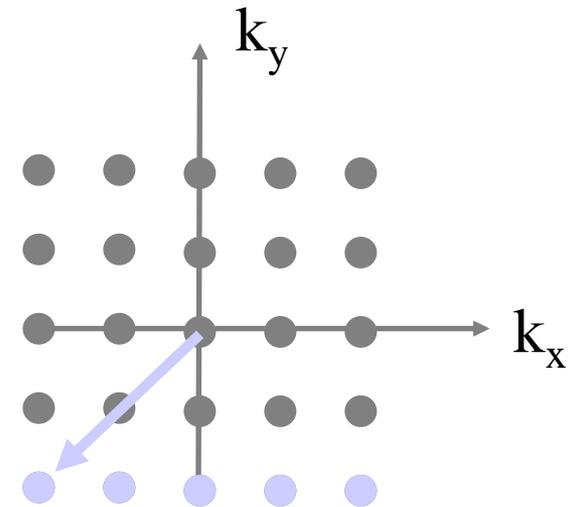
Selective excitation



Signal acquisition  
(digital sampling)

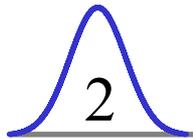


*K* space

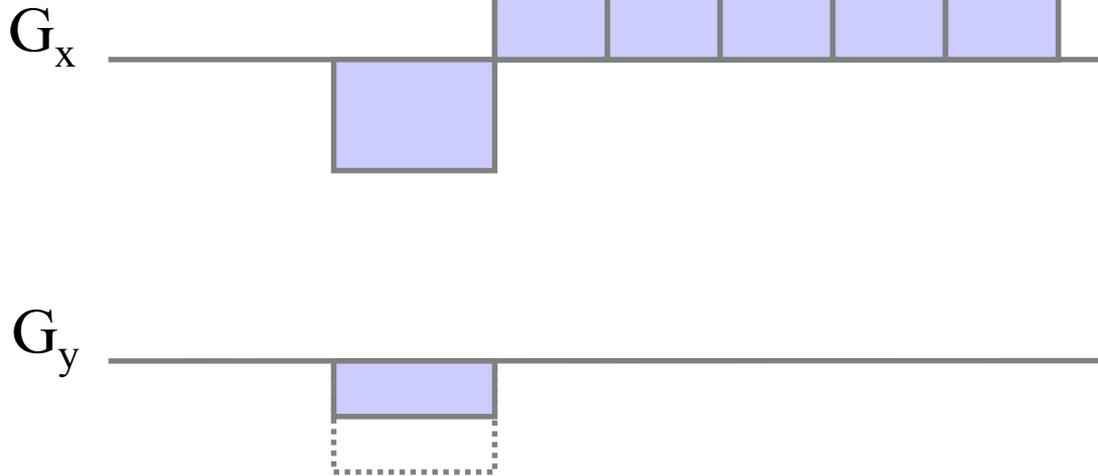
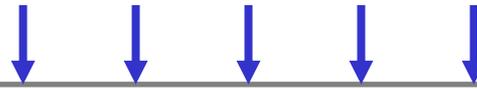


# k-space acquisition - FLASH

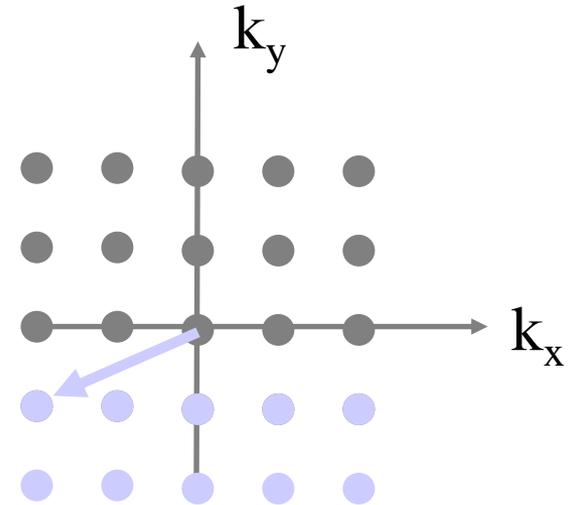
Selective excitation



Signal acquisition  
(digital sampling)

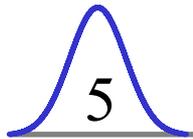


*K* space

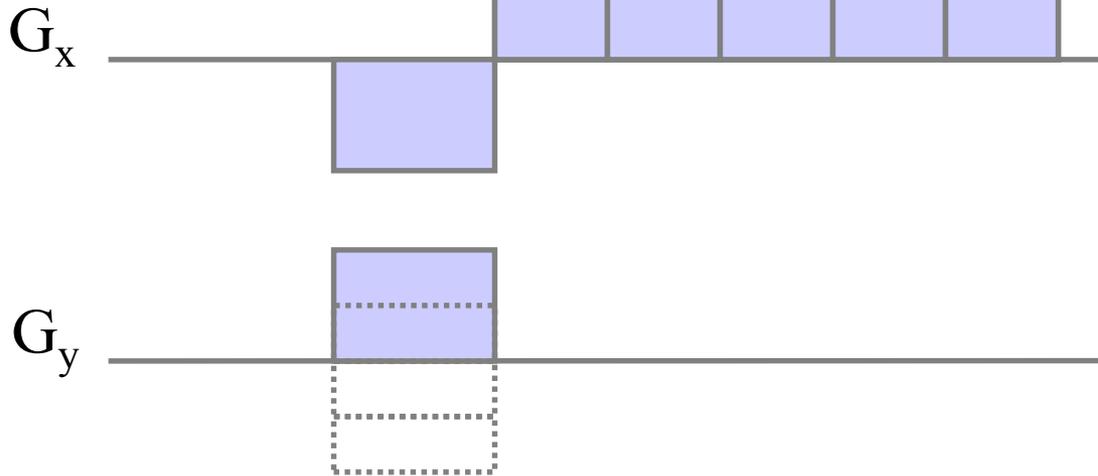
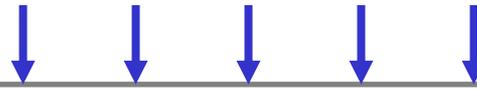


# k-space acquisition - FLASH

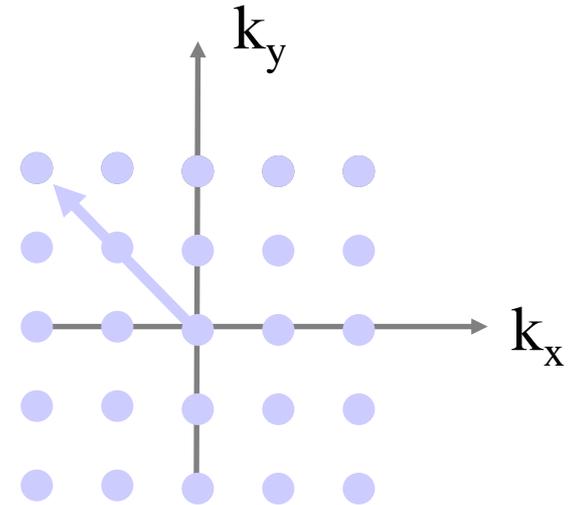
Selective excitation



Signal acquisition  
(digital sampling)

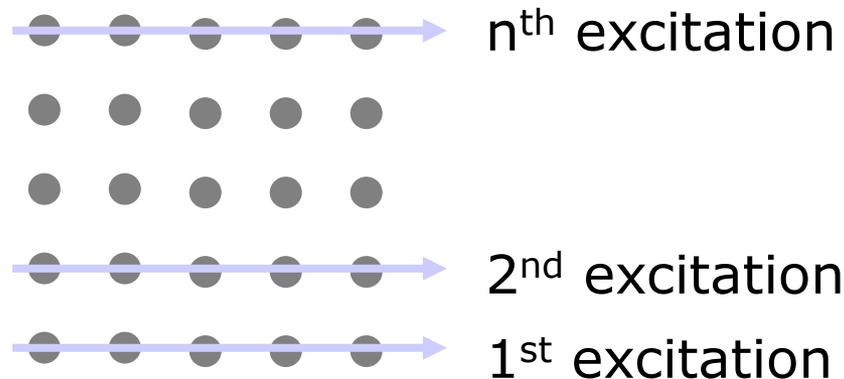


*K* space



# k-space acquisition - FLASH

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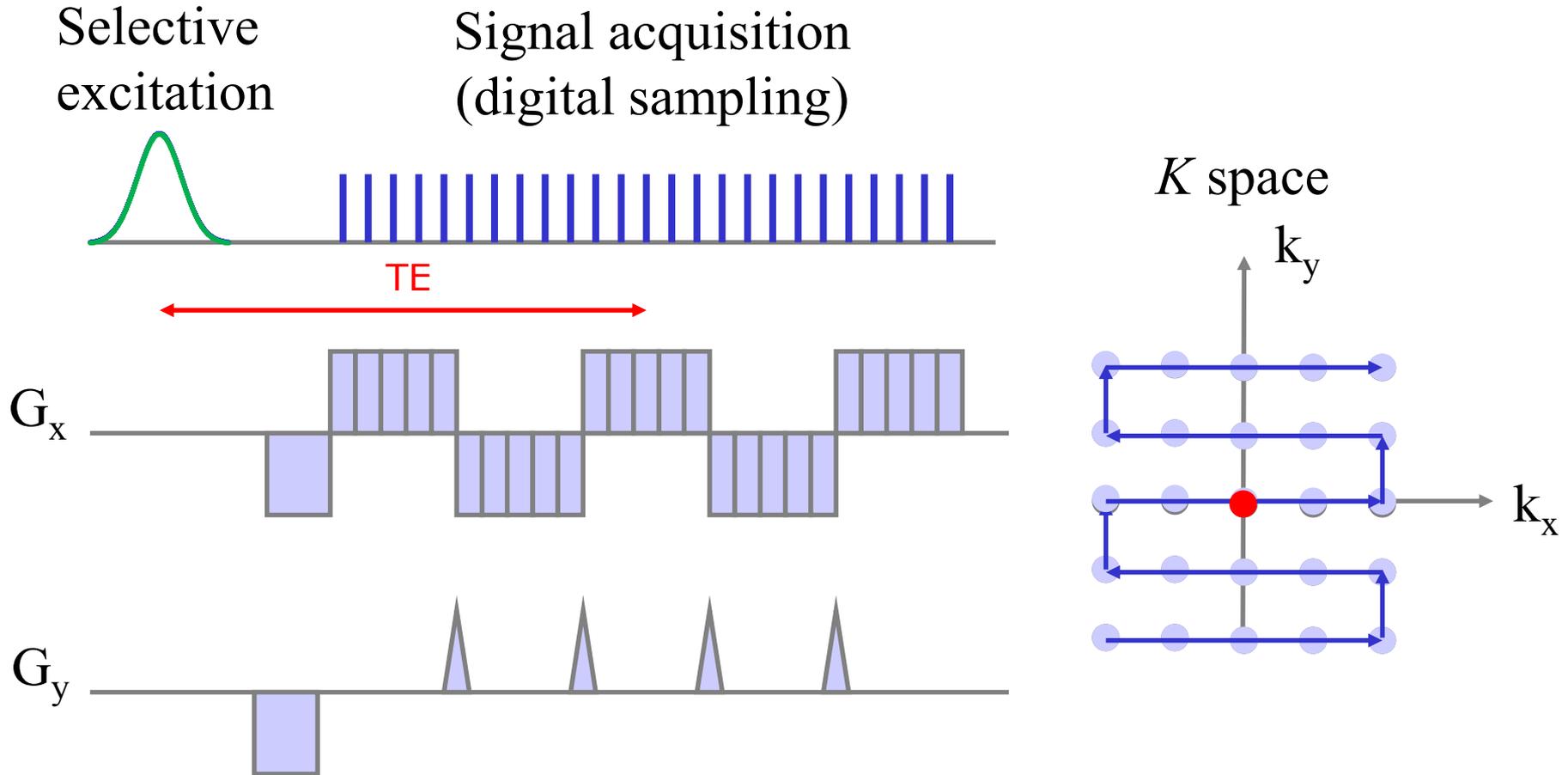


Problem: This sequence is rather slow

- $K$  space is sampled line by line
- After each excitation one must wait for the longitudinal magnetization to recover

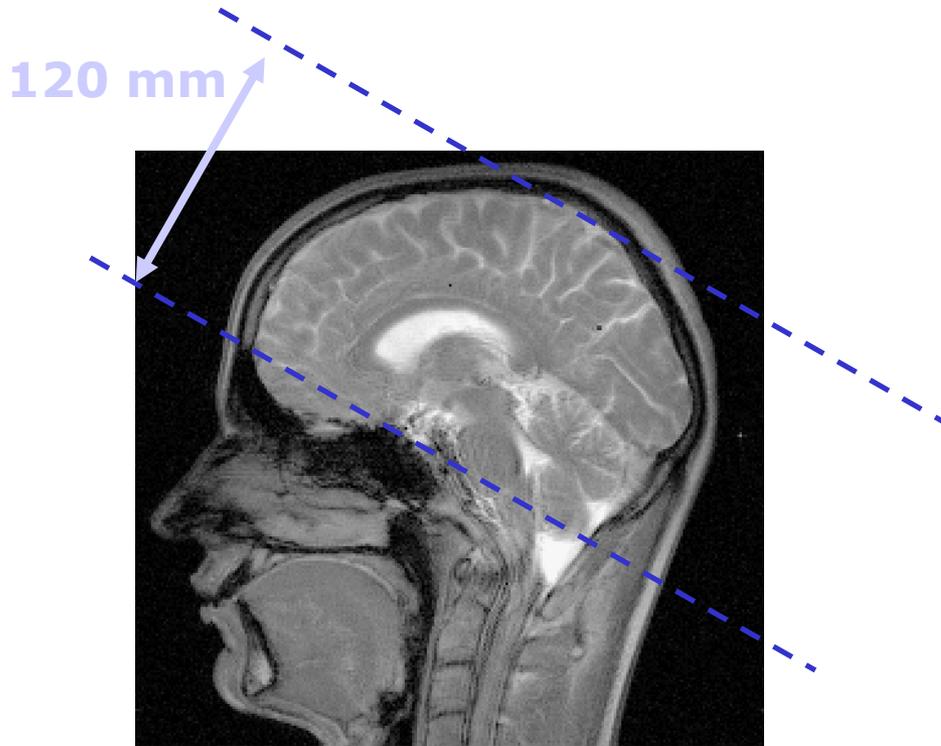
Example:  $n = 256$ ,  $TR = 2s$   $\Rightarrow T = n TR = 8.5$  min

# Echo Planar Imaging (EPI)



# EPI at the CBU

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How many slices ?

$$\frac{120 \text{ mm}}{3 \text{ mm} + 0.75 \text{ mm}} = 32$$

And the minimum TR ?

$$32 * 62.5 \text{ ms} = 2000 \text{ ms}$$

**Questions?**