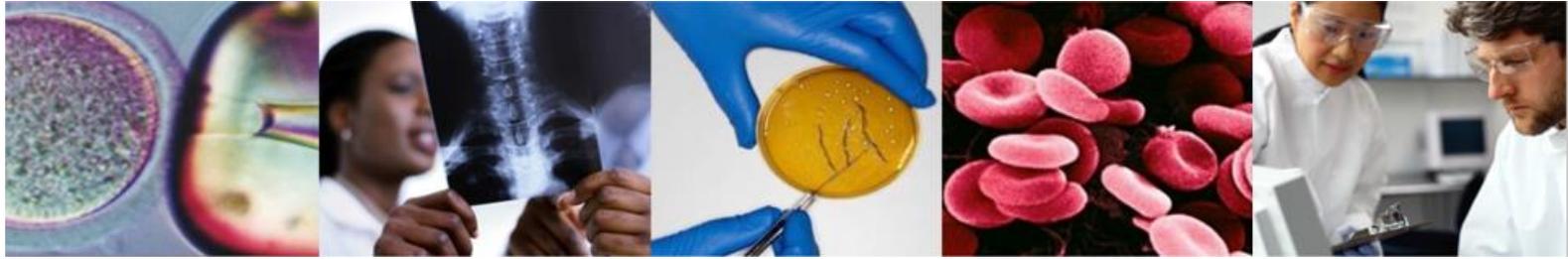


MRC

Cognition and
Brain Sciences Unit

75th ANNIVERSARY 1944 - 2019

 UNIVERSITY OF
CAMBRIDGE



EEG/MEG 2: Head Modelling and Source Estimation

Olaf Hauk

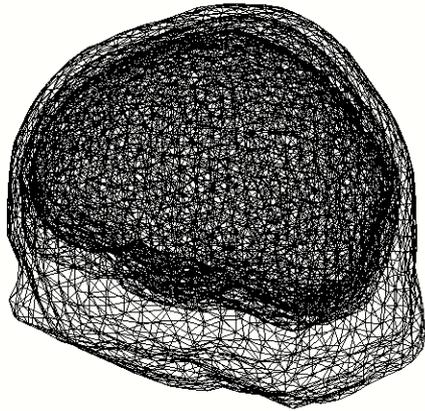
olaf.hauk@mrc-cbu.cam.ac.uk

Introduction to Neuroimaging Methods, 2.4.2019

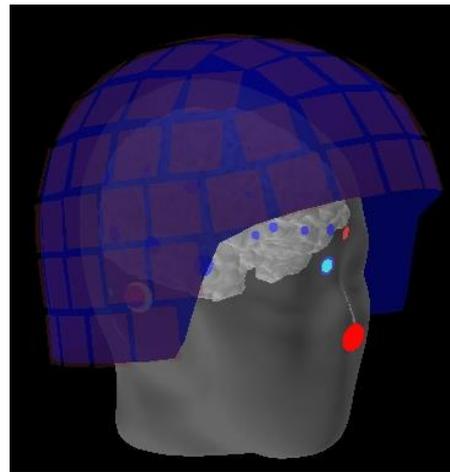


Ingredients for Source Estimation

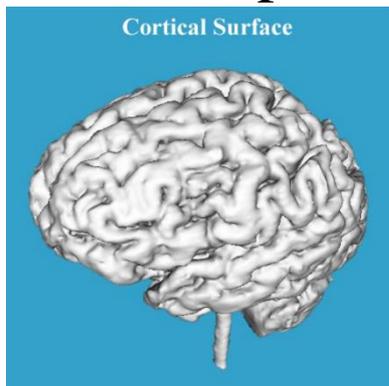
Volume Conductor/
Head Model



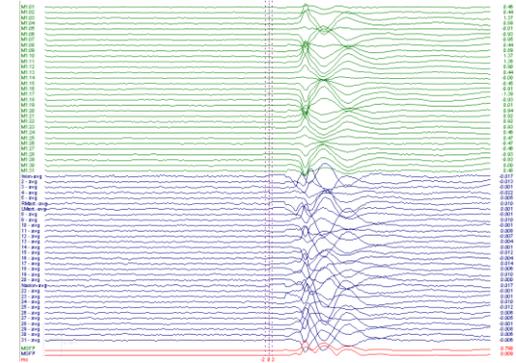
Coordinate
Transformation



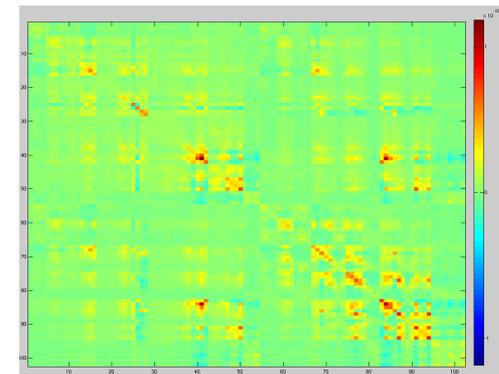
Source Space



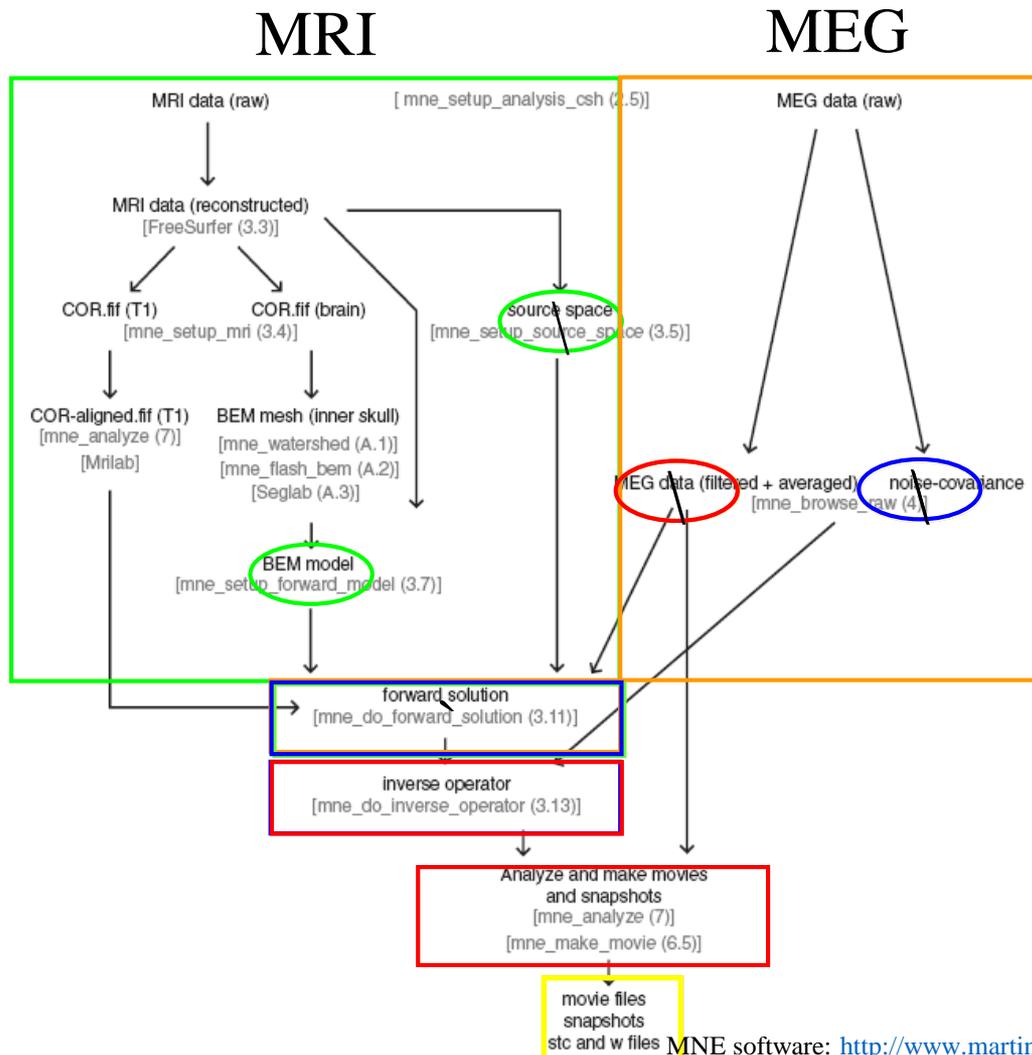
MEG data



Noise/Covariance Matrix



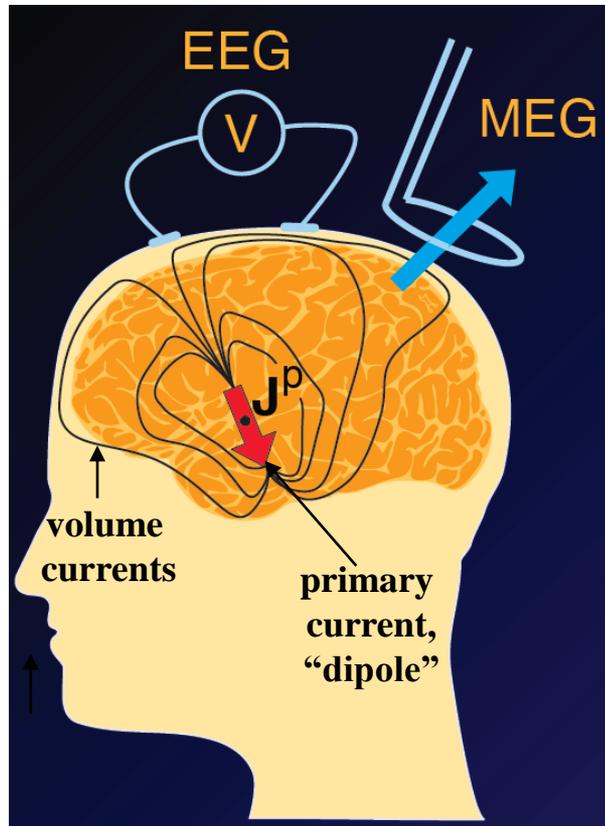
The Path to the Source



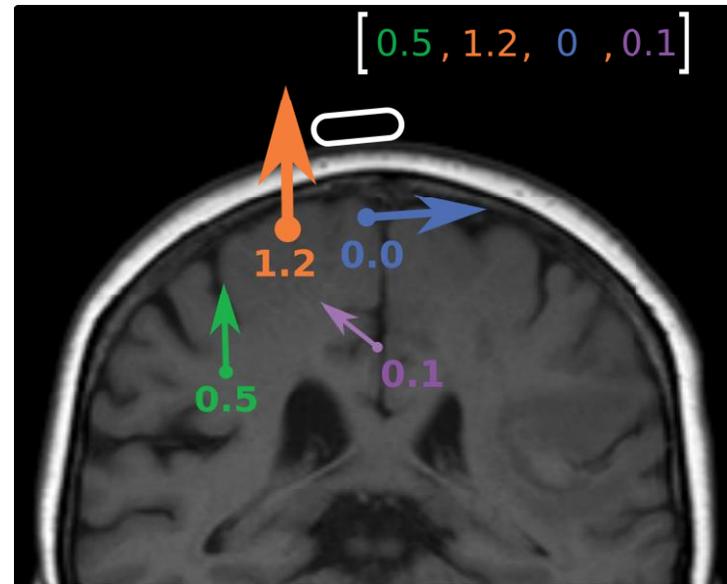
Practice

The EEG/MEG Forward Problem

EEG/MEG measure the primary sources indirectly



Sensors are differently sensitive to different sources

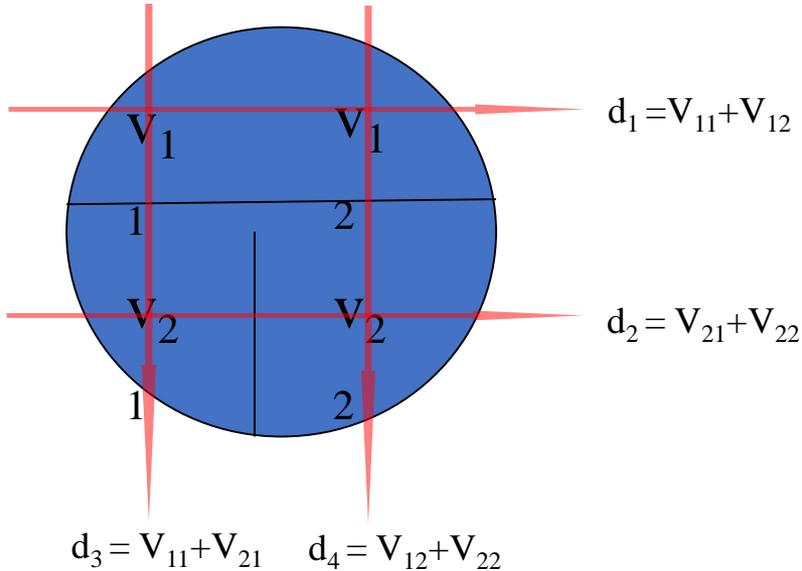


“Leadfield”

Hauk, Stenroos, Tredner. In: Supek S, Aine C (eds), “Magnetoencephalography: From Signals to Dynamic Cortical Networks, 2nd Ed.”

Why Inverse "Problem"?

Tomography (CT, fMRI...)



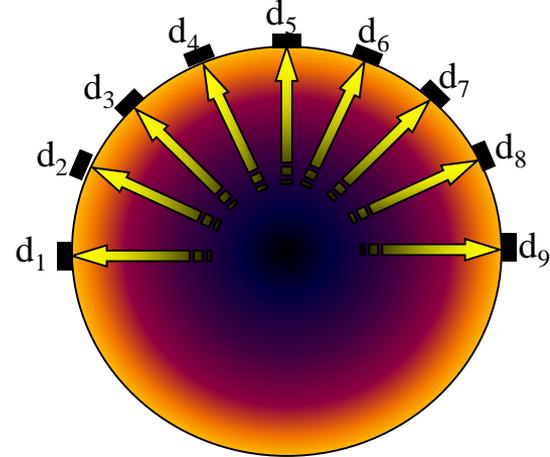
$$d_1 = V_{11} + V_{12}$$

$$d_2 = V_{21} + V_{22}$$

$$d_3 = V_{11} + V_{21}$$

$$d_4 = V_{12} + V_{22}$$

EEG/MEG



$$d_1 = V_{11} + V_{12} + V_{13} + V_{14} \dots$$

$$d_2 = V_{21} + V_{22} + V_{23} + V_{24} \dots$$

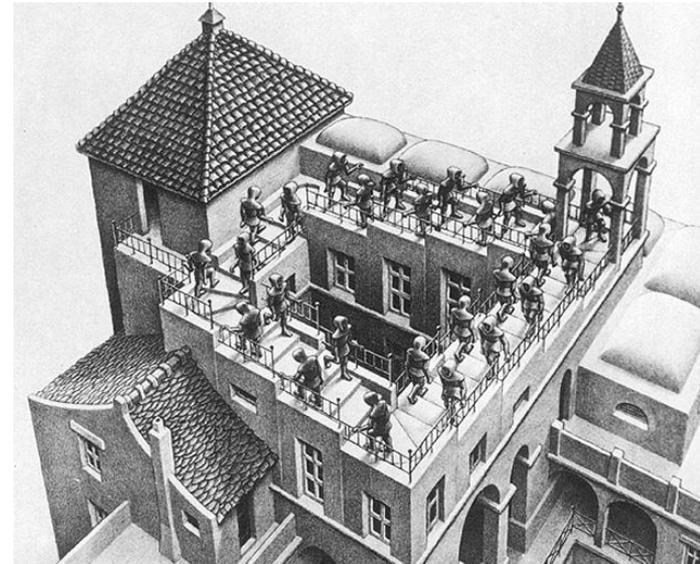
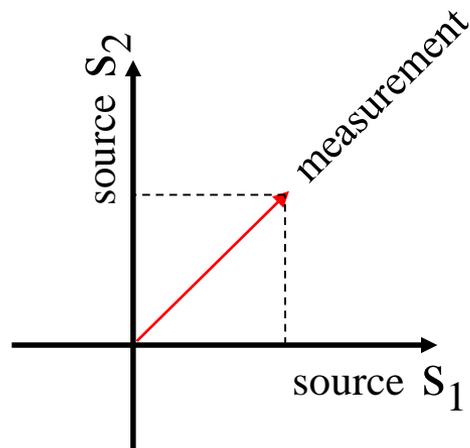
Information is lost during measurement

Cannot be retrieved by mathematics

Inherently limits spatial resolution



Why Inverse “Problem”?



M.C. Escher

In “signal space”, we see a faint shadow of activity in “source space”.

If you are not shocked by the EEG/MEG inverse problem...
... then you haven't understood it yet.

(freely adapted from Niels Bohr)

Non-Uniquely Solvable Problem

What is the solution to

$$x_1 + x_2 = 1$$

Maybe

$$x_1 = 0 ; x_2 = 1 \quad ?$$

$$x_1 = 1 ; x_2 = 0 \quad ?$$

$$x_1 = 1000 ; x_2 = -999 \quad ?$$

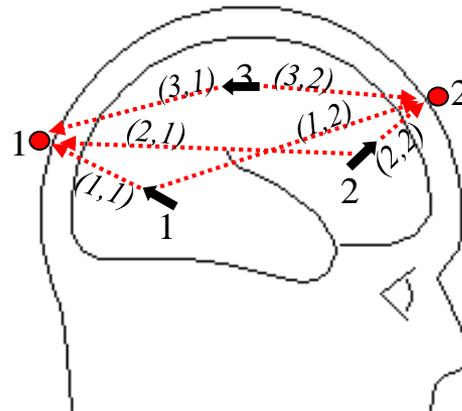
$$x_1 = \pi ; x_2 = (1-\pi) \quad ?$$

The minimum norm solution is:

$$x_1 = 0.5 ; x_2 = 0.5$$

with $(0.5^2 + 0.5^2)=0.5$ the minimum norm among all possible solutions.

Non-Uniquely Solvable Problem



“Minimum Norm Solution”

data	“leadfield”	dipoles	?	dipoles	inverse	data
$\begin{matrix} \bullet \\ \bullet \end{matrix} \begin{pmatrix} d_1 \\ d_2 \end{pmatrix}$	$= \begin{pmatrix} 0.5 & 0 & 0.3 \\ 0 & 1 & -0.3 \end{pmatrix}$	$\begin{pmatrix} j_1 \\ j_2 \\ j_3 \end{pmatrix}$	$\xrightarrow{\text{inversion}}$	$\begin{pmatrix} j_1 \\ j_2 \\ j_3 \end{pmatrix}$	$= \begin{pmatrix} 1.5034 & 0.1241 \\ 0.2483 & 0.9379 \\ 0.8276 & -0.2069 \end{pmatrix}$	$* \begin{pmatrix} d_1 \\ d_2 \end{pmatrix$

MNE produces solution with minimal power or “norm”:

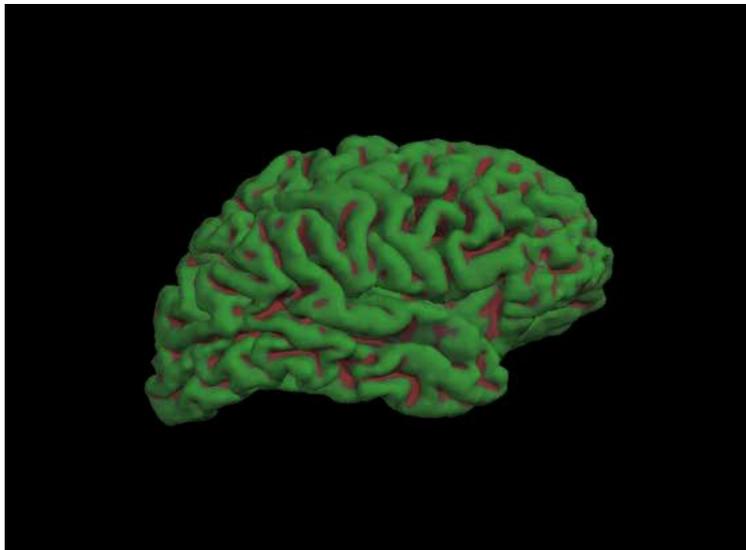
$$(j_1^2 + j_2^2 + j_3^2)$$

Practice



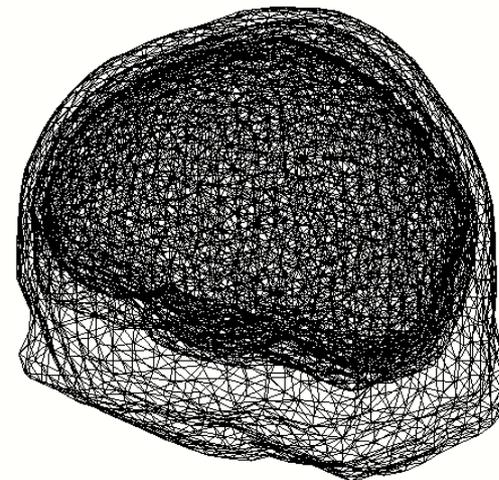
MRI Preprocessing: Source Space and Head Model

Source Space,
e.g. grey matter, 3D volume



<http://www.cogsci.ucsd.edu/~sereno/movies.html>

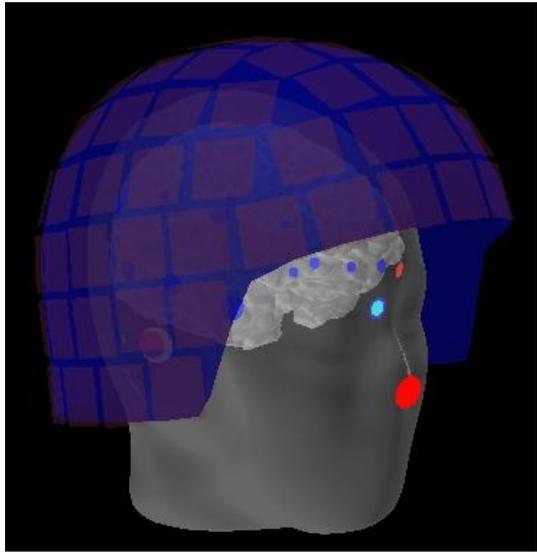
Volume Conductor/Head Model
e.g. sphere, 1- or 3-compartments from MRI



Sometimes “standard head models” are used, when no individual MRIs available.
SPM uses the same “canonical mesh” as source space for every subjects, but adjusts it individually.

Coregistration of EEG/MEG and MRI Spaces

Coordinate Transformation



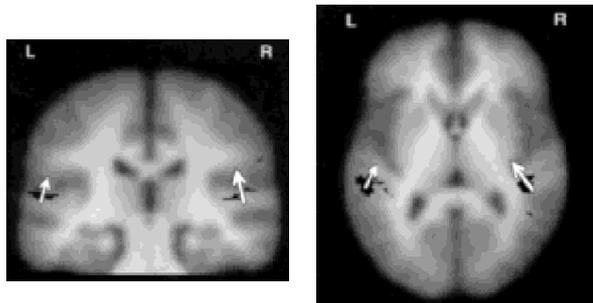
Practice



Source Estimation Approaches

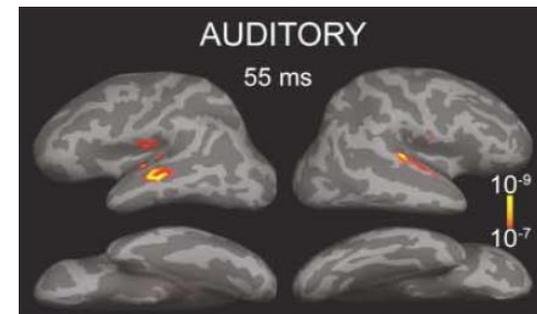
“Dipole Fitting”

1. Assume there are only a few distinct sources
2. Iteratively adjust the location, orientation and strength of a few dipoles...
3. ...until the result best fits the data



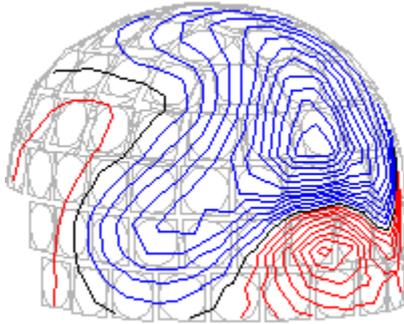
“Distributed Sources”

1. Assume sources are everywhere (e.g. distributed across the whole cortex)
2. Find the distribution of source strengths that explains the data...
3. ...AND fulfils other constraints

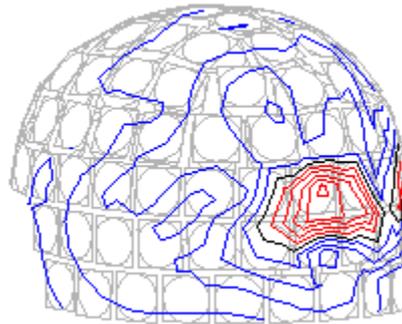




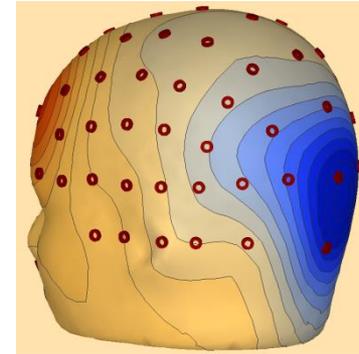
Visually Evoked Activity ~ 100 ms



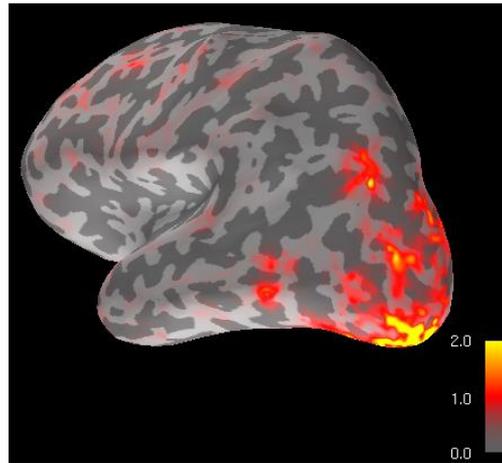
Magnetometers



Gradiometers



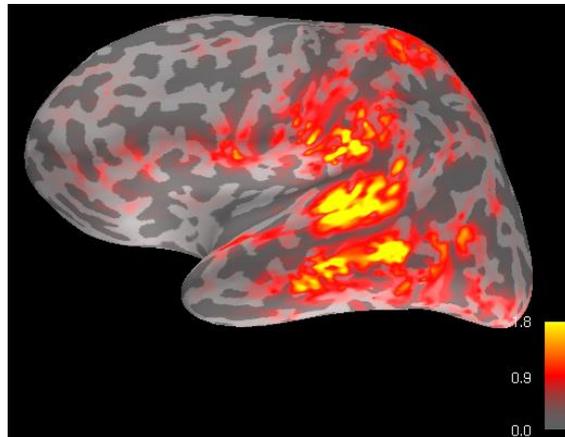
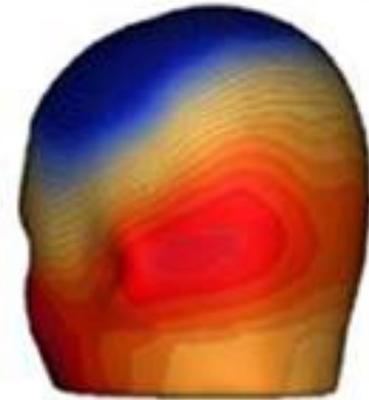
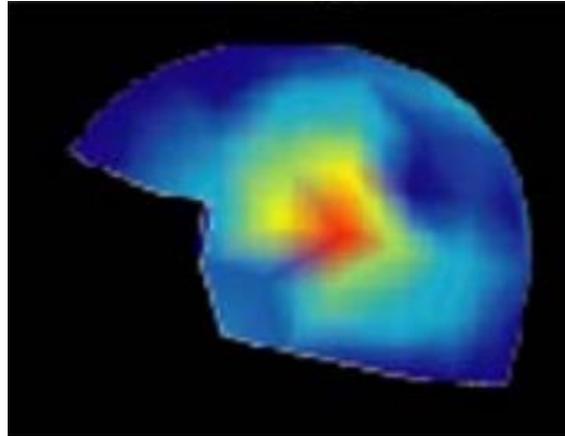
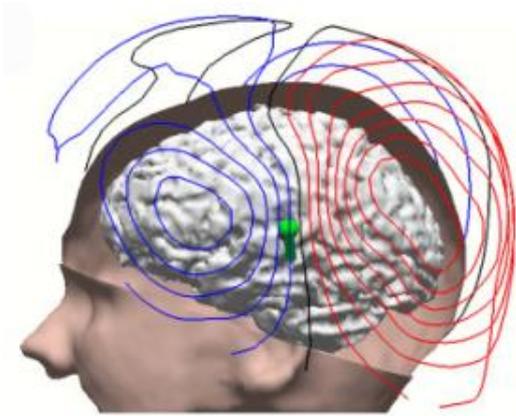
EEG



Minimum Norm Estimate

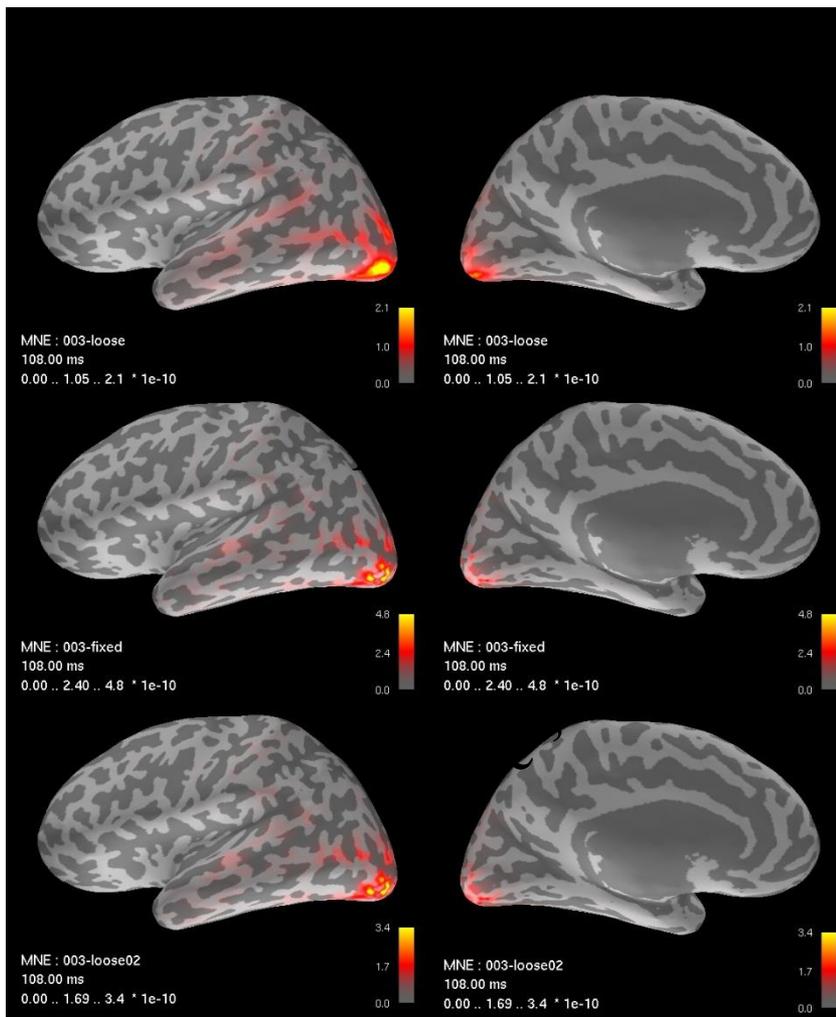
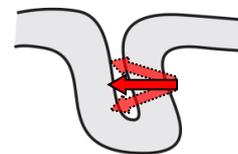
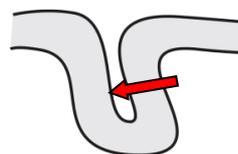
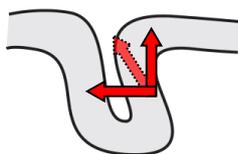


Auditorily Evoked Activity



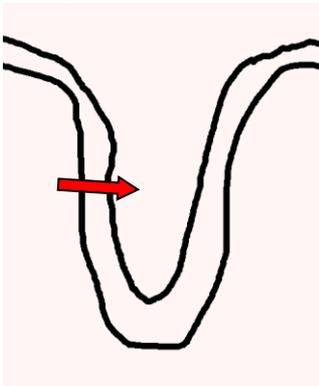
Minimum Norm Estimate

Source Orientation Constraints

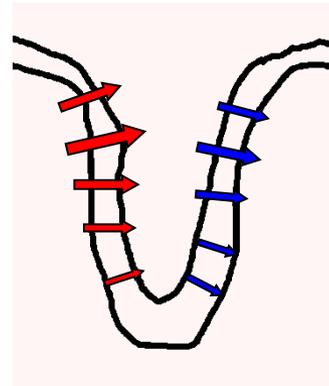


Direction of Current Flow

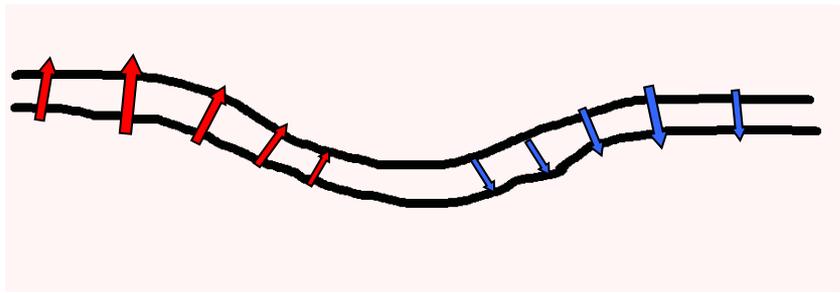
Dipole Source



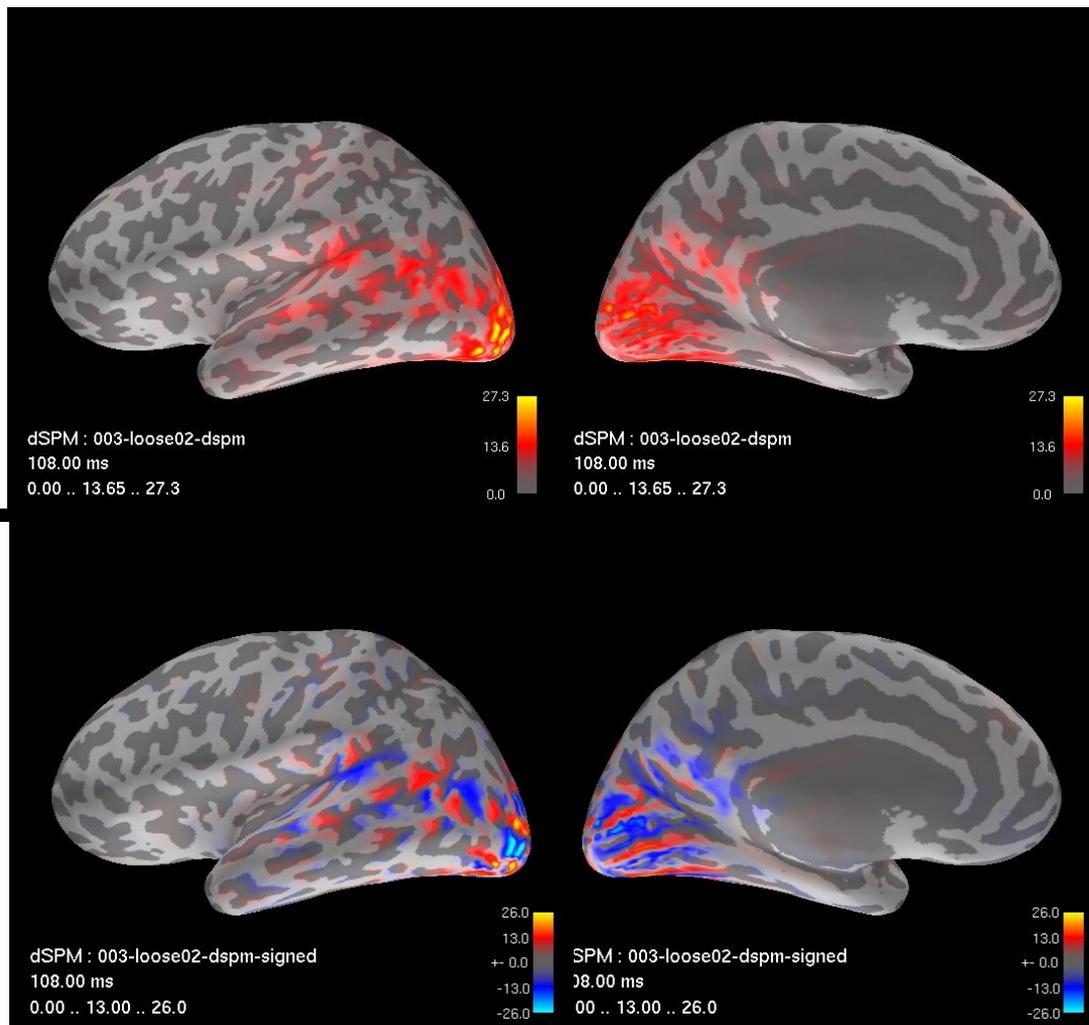
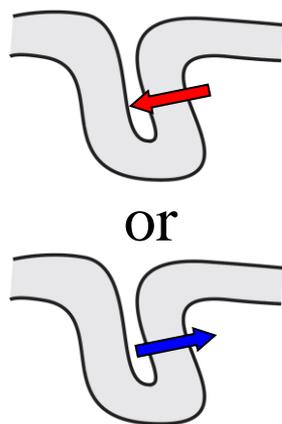
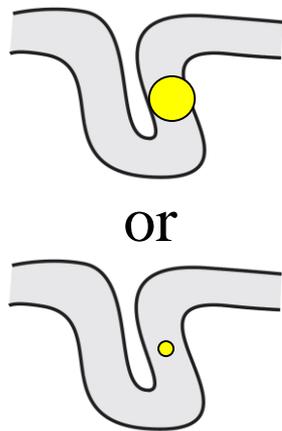
Distributed Source



Distributed Source, Inflated Surface



Direction of Current Flow

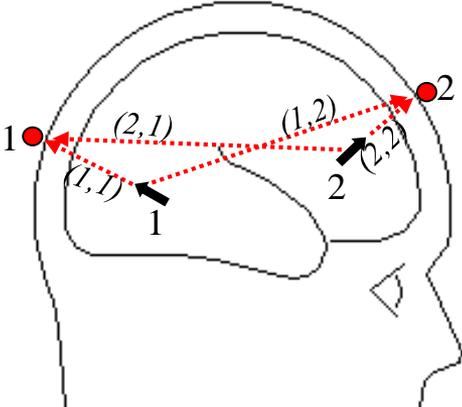


Practice

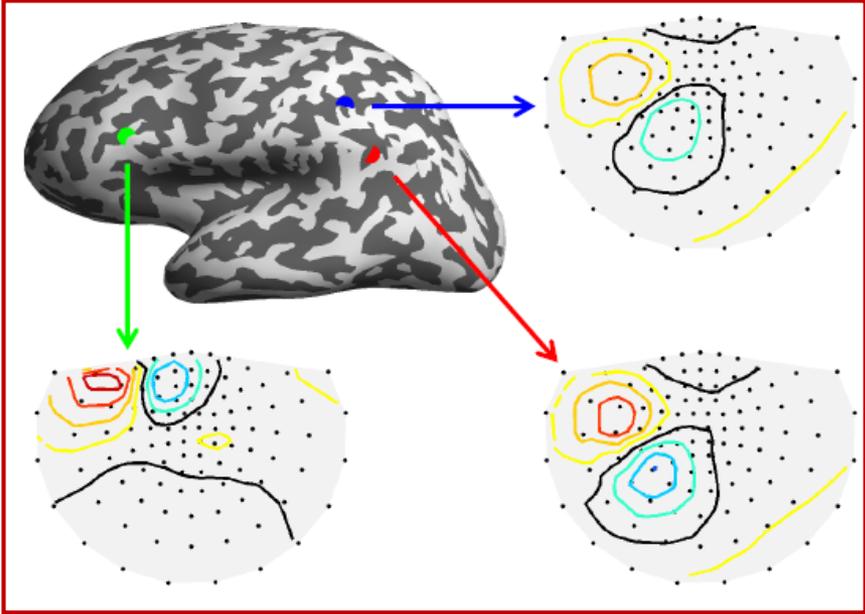
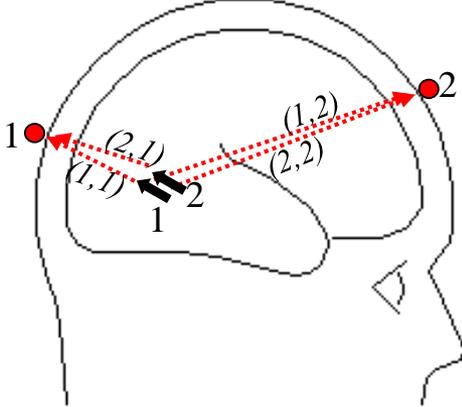


(In)Stability – Sensitivity to Noise

Stable



Unstable



Similar topographies are difficult to distinguish, especially in the presence of noise.

Practice



Noise covariance

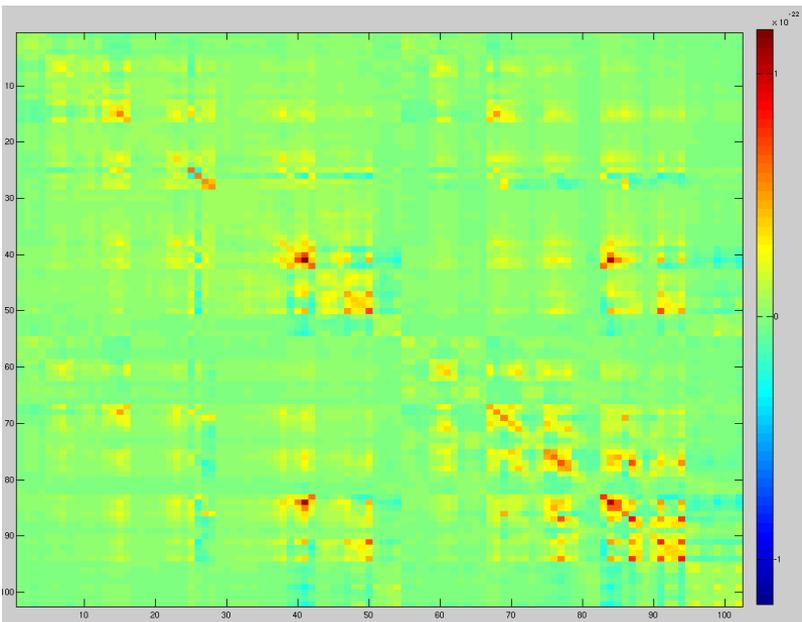
Some channels are noisier than others

⇒ They should get different weights in your analysis

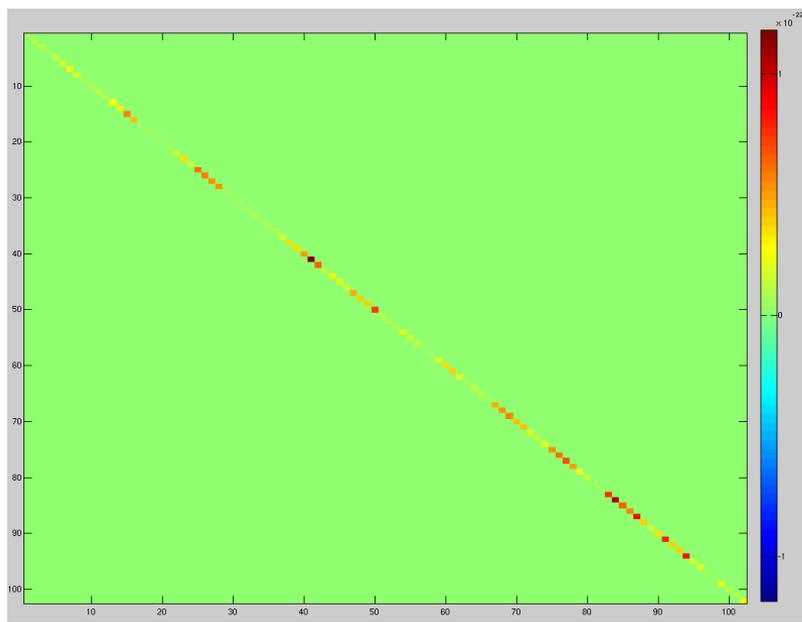
Sensors are not independent

⇒ Sensors that carry the same information should be downweighted relative to more independent sensors

(Full) Noise Covariance Matrix



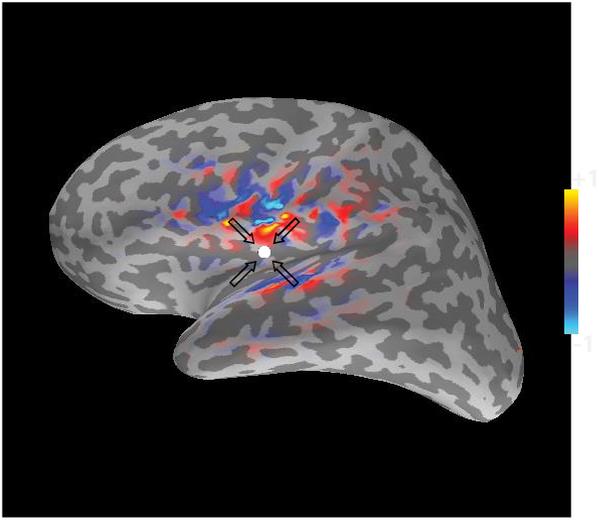
(Diagonal) Noise Covariance Matrix
(contains only variance for sensors)



Practice

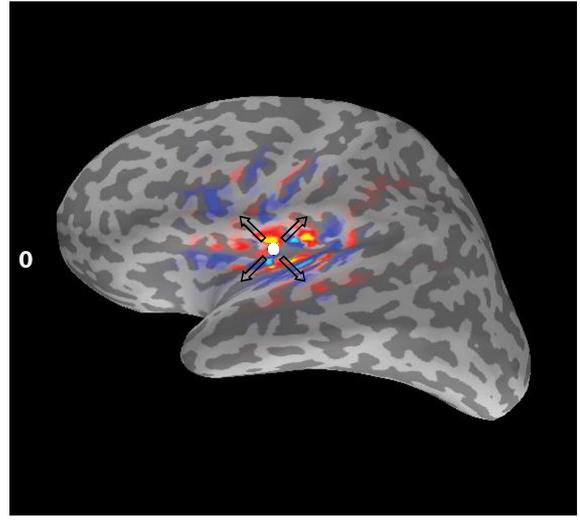
Spatial Resolution: Point-Spread and Cross-Talk/Leakage

Cross-Talk Function (CTF)



How other sources may affect the estimate for this source

Point-Spread Function (PSF)



How this source affects estimates for other sources

Spatial Resolution of Source Estimation

Spatial resolution depends on:

- modeling assumptions
- number of sensors (EEG/MEG or both)
- source location
- source orientation
- signal-to-noise ratio
- head modeling

=> difficult to make general statement

Spatial Resolution – A Naïve Estimate

With n sensors:

-> n independent measurements

-> n independent parameters estimable

-> at best separate activity from n brain regions

Sensors are not independent -> ~ 50 degrees of freedom

Volume of source space:

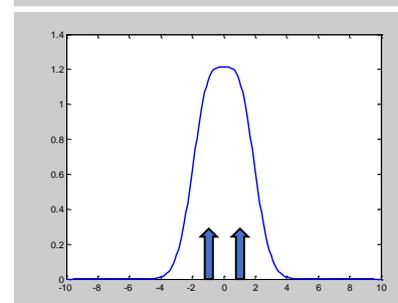
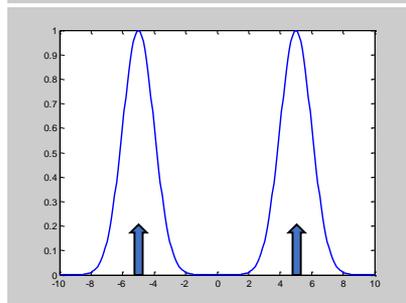
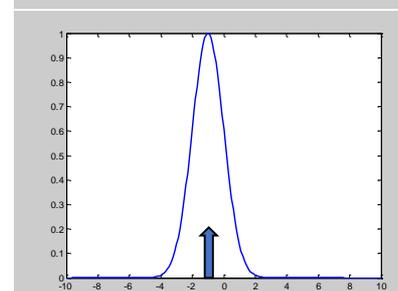
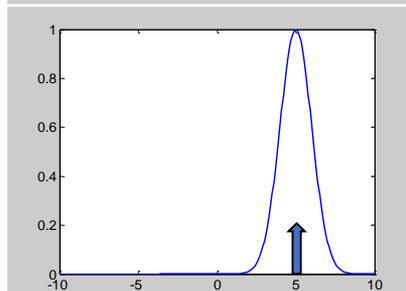
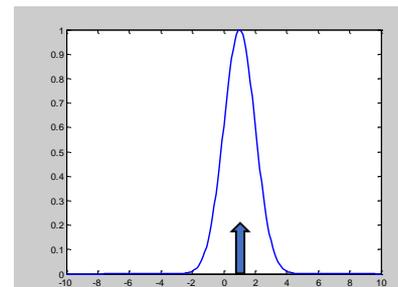
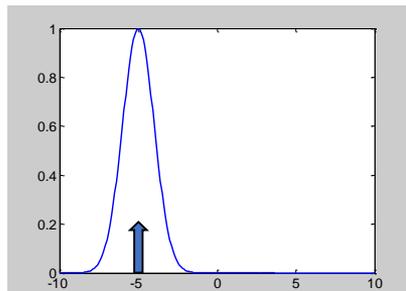
Sphere 8cm minus sphere 4 cm: volume $\sim 1877 \text{ cm}^3$

“Resel”: $38 \text{ cm}^3 \rightarrow \underline{3.4}^3 \text{ cm}^3$

The spatial resolution of the measurement is inherently limited!



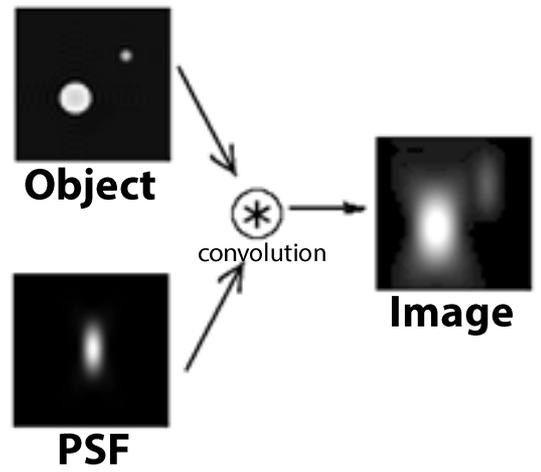
Linear Methods – Superposition Principle



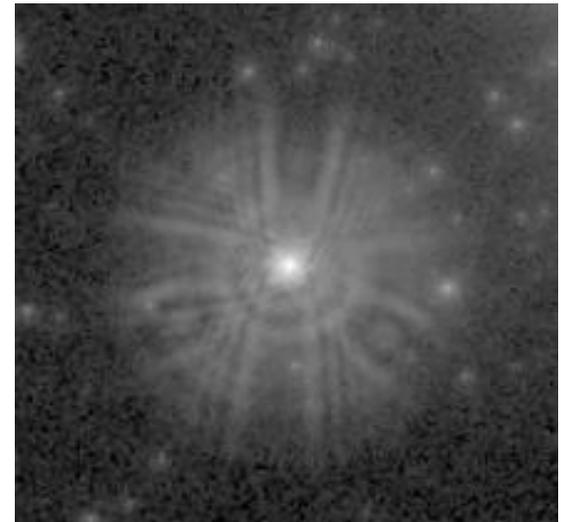
If you know the behaviour for point sources,
you can predict the behaviour for complex sources

Linear Methods – Superposition Principle

Microscopy



Astronomy

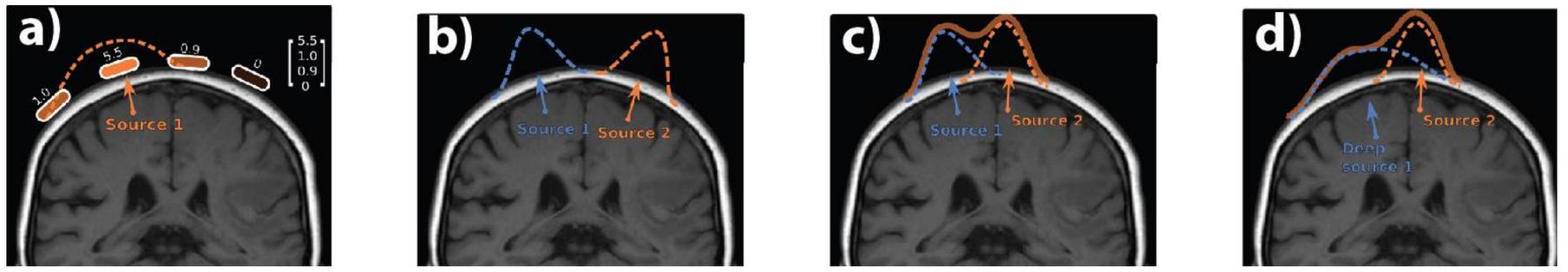


Linear Methods – Superposition Principle

Superposition In Sensor Space



Superposition In Source Space

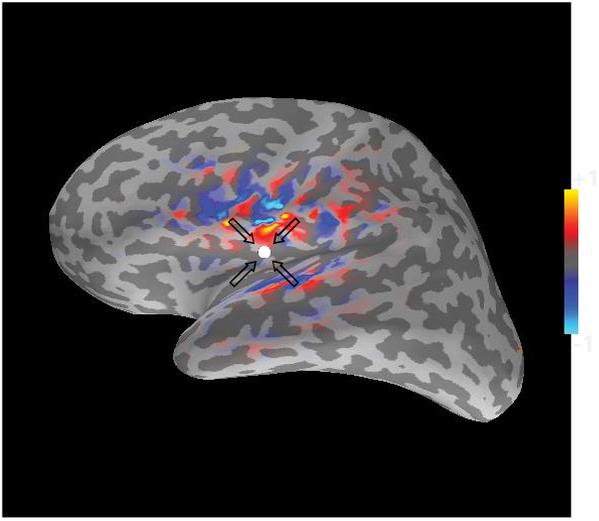


Practice



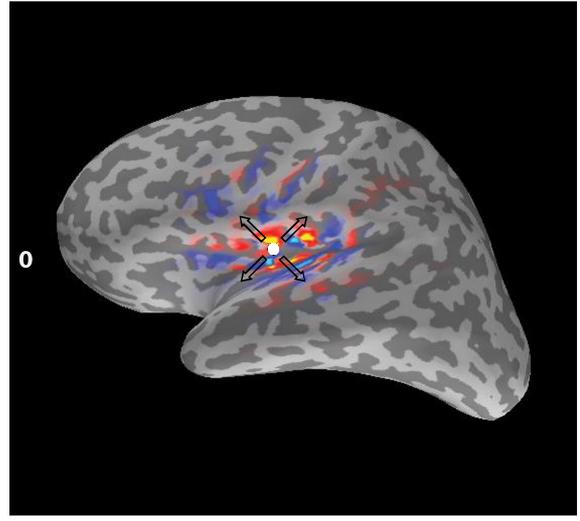
Spatial Resolution: Point-Spread and Cross-Talk/Leakage

Cross-Talk Function (CTF)



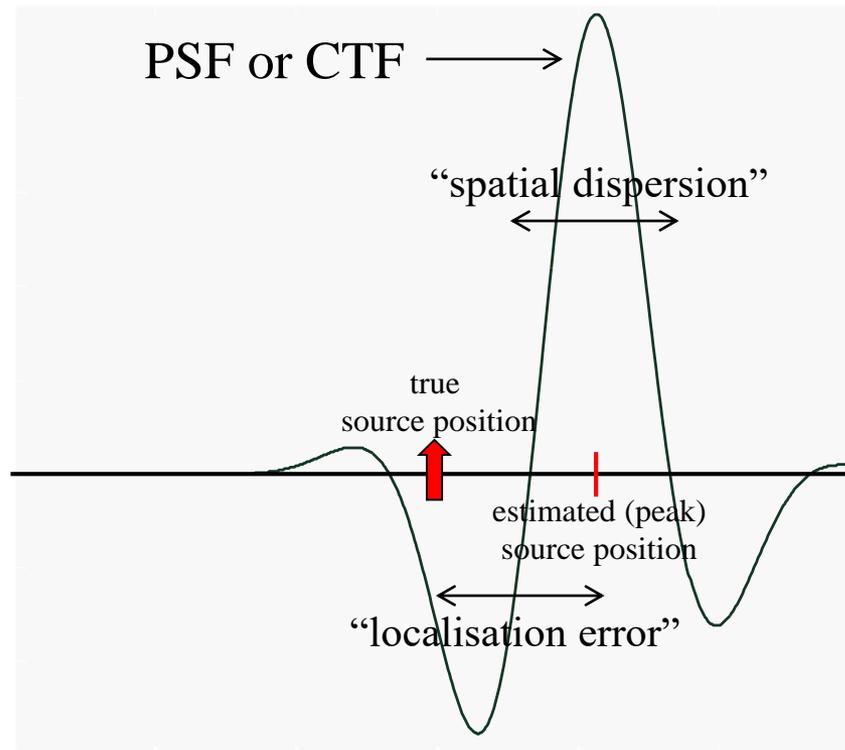
How other sources may affect the estimate for this source

Point-Spread Function (PSF)



How this source affects estimates for other sources

Quantifying “Resolution”

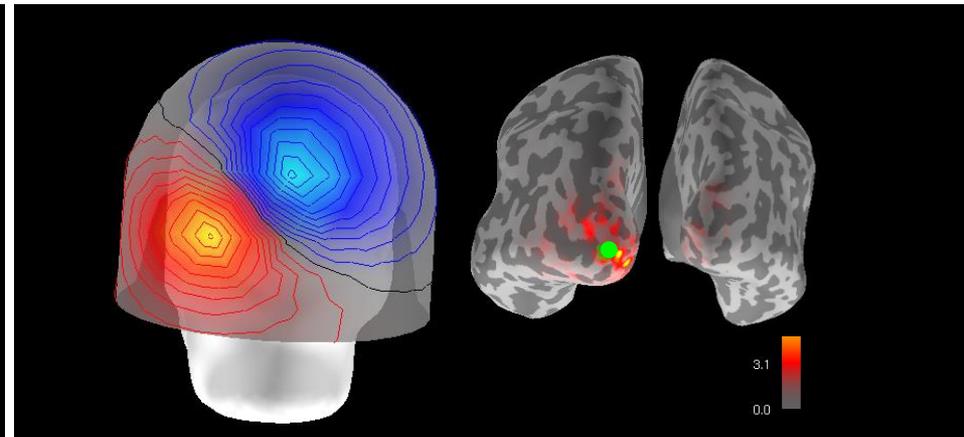
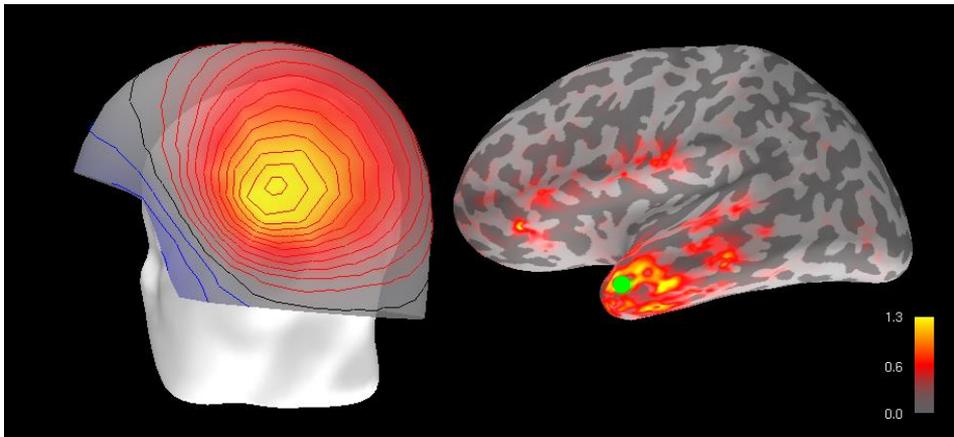


It’s not just “peak localisation” that counts,
but also spatial extent of the distribution (“resolution”)

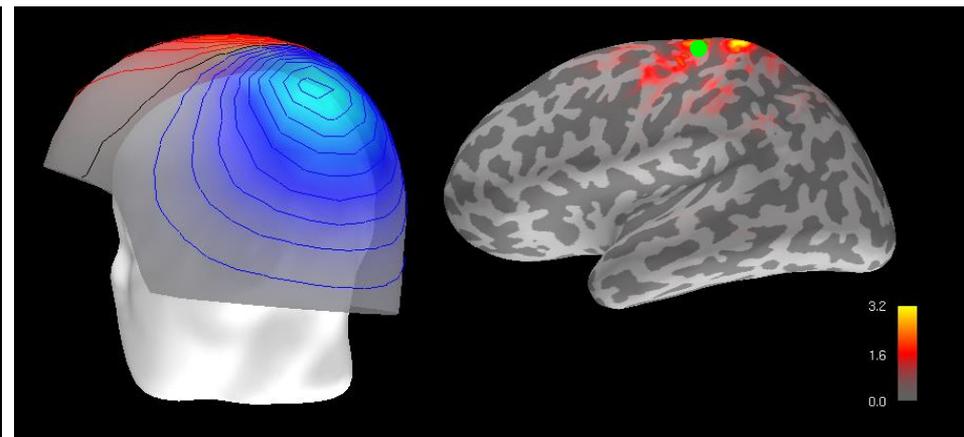
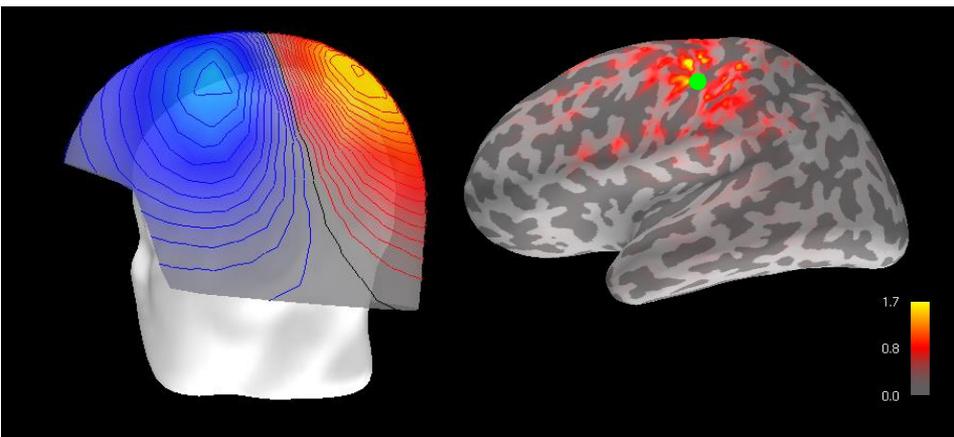


PSFs and CTFs for Some ROIs

For MNE, PSFs and CTFs turn out to be the same



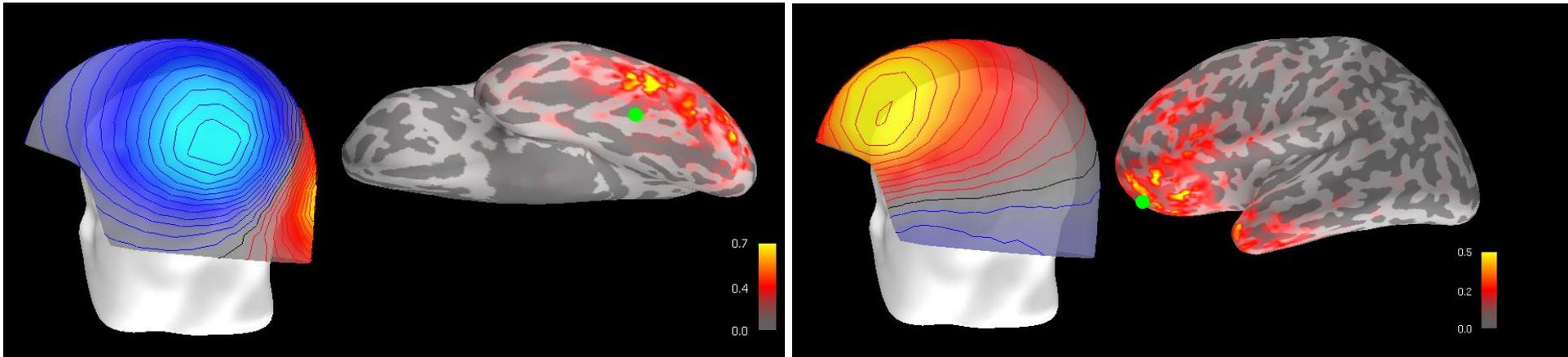
Good



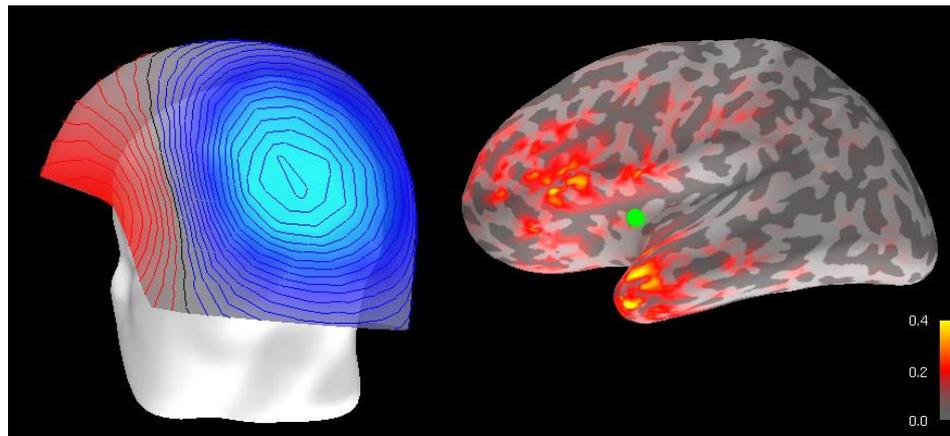


PSFs and CTFs for Some ROIs

For MNE, PSFs and CTFs turn out to be the same



Less good



Comparing Methods

Different methods make different compromises.

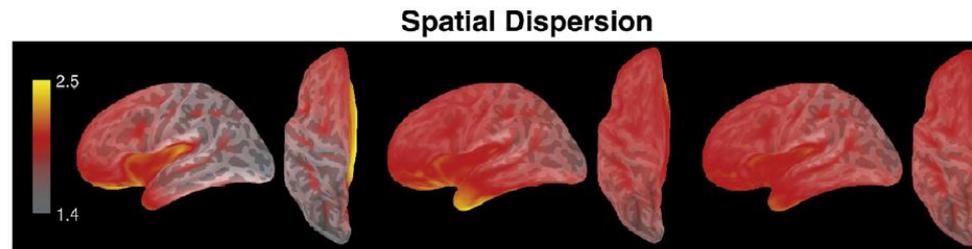
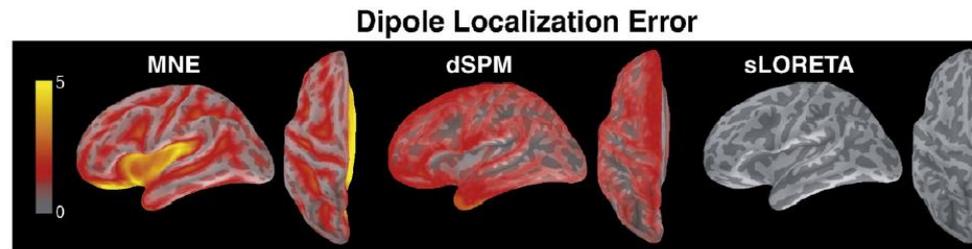
There is no “best” method – best for what?

One should compare methods for the same purpose and under the same assumptions.

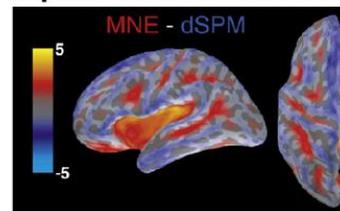
Difficult to generalize results from one example or data set

=> Important to understand the principles

Methods Comparison



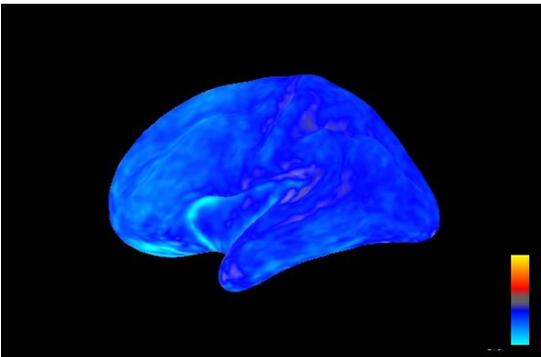
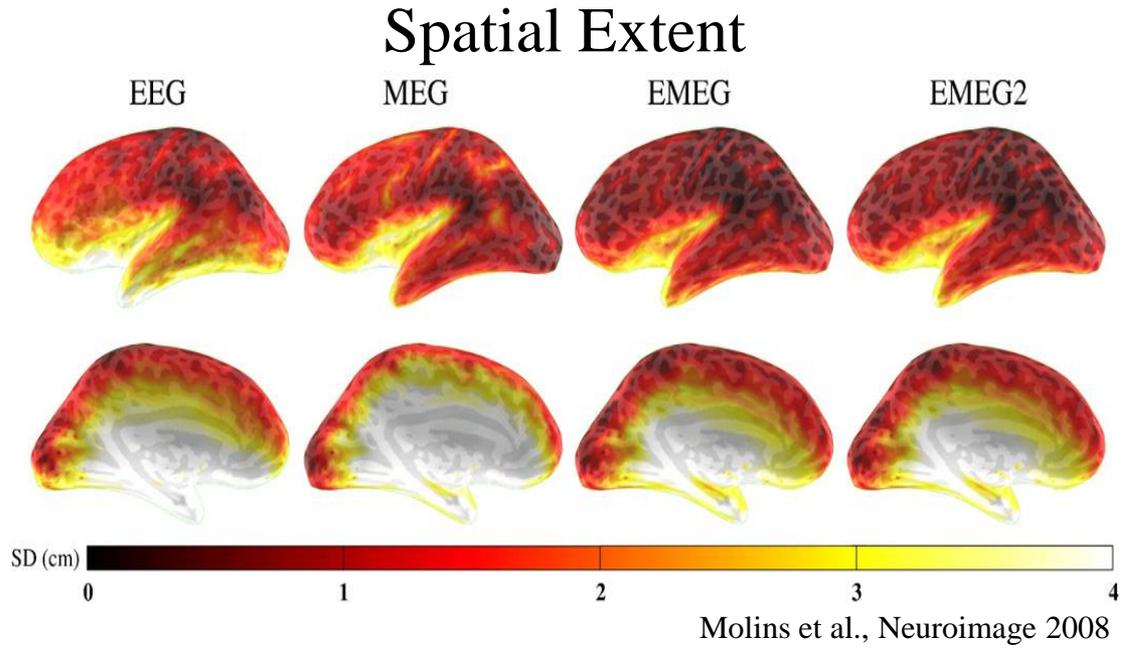
Dipole Localization Error



Spatial Dispersion



Combining EEG and MEG Increases Resolution

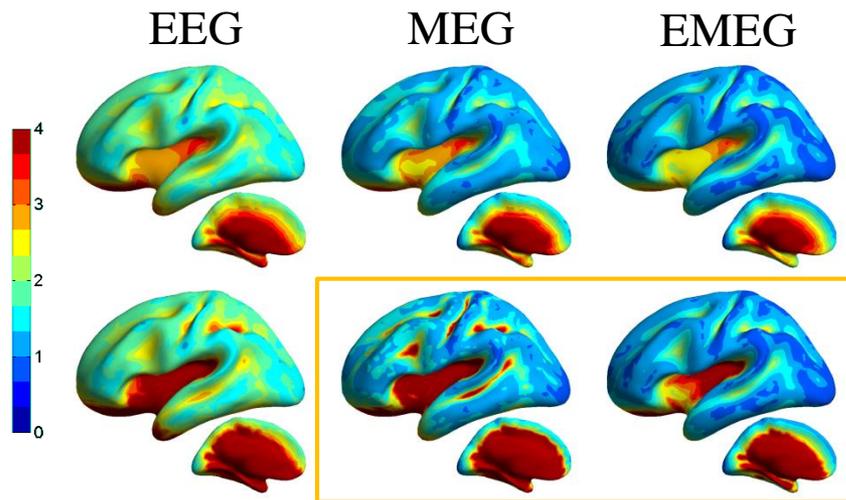


Stenroos&Hauk, in prep

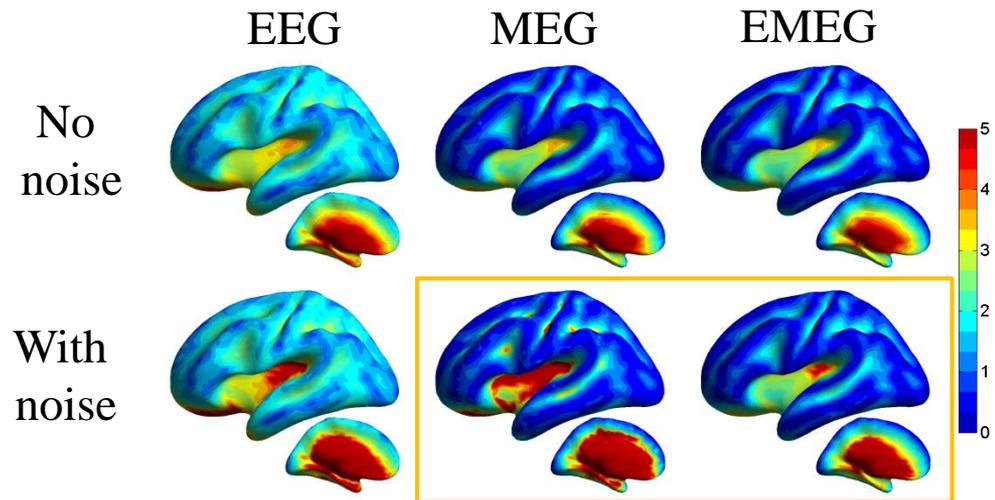
Combining EEG and MEG Improves Resolution

...especially in the presence of (correlated) noise

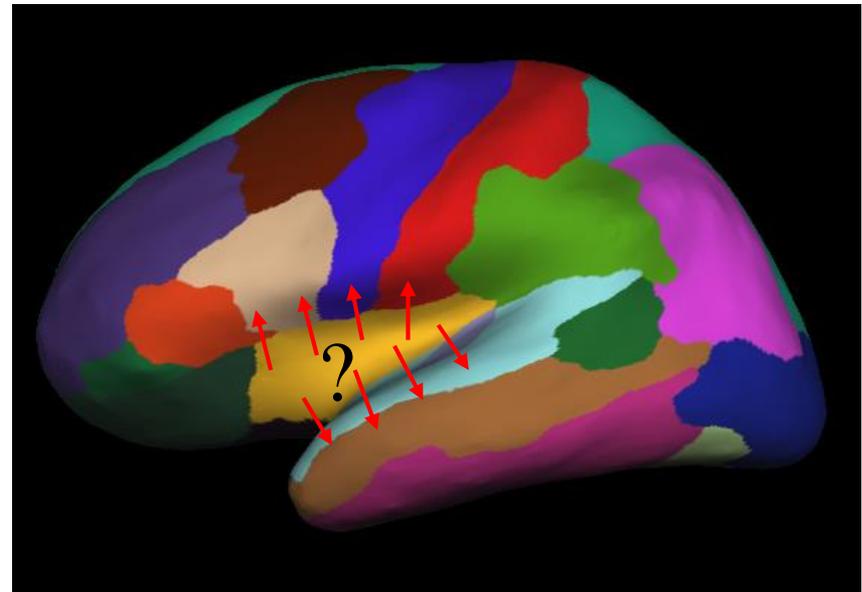
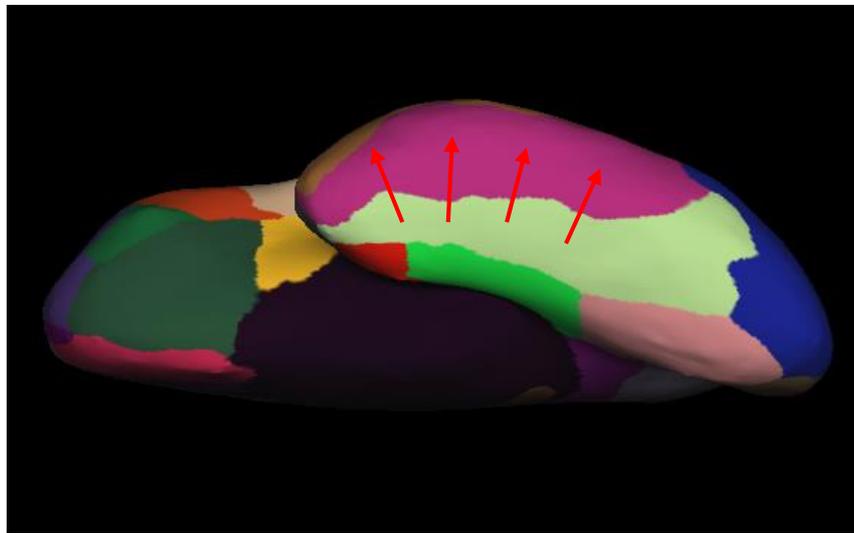
Spatial Deviation (cm)



Localisation Error (cm)



Localisation Bias Has Consequences for ROI analysis



Desikan-Killiany Atlas parcellation

The End Of #2

Please leave your feedback.